Solved Examples

JEE Main/Boards

Example 1: The disintegration rate of a certain radioactive sample at any instant is 4750 dpm. Five minutes later, the rate becomes 2700 dpm. Calculate half-life of sample.

Sol: Comparative rates are given, as we know rate of disintegration is proportional to no.of atoms substitute the value of N and N_0 in the rate equation and calculate integration constant. From integration constant it is easy to calculate half-life of the sample.

$$\begin{aligned} r_{0} &= 4750 \text{ dpm}, \quad r_{t} = 2700 \text{ dpm} \\ \therefore \quad \frac{r_{0}}{r_{t}} &= \frac{N_{0}}{N_{t}} = \frac{4750}{2700} ; \qquad \lambda = \frac{2.303}{t} \log \frac{N_{0}}{N} \\ \therefore \quad \lambda = \frac{2.303}{5} \log \frac{4750}{2700} = 0.113 \text{ min} - 1 \\ \therefore \quad t_{1/2} &= \frac{0.693}{\lambda} = \frac{0.693}{0.113} = 6.13 \text{ min} \end{aligned}$$

Example 2: It is known that 1 g of ²²⁶Ra emits 11.6×10^{17} atoms of α per year. Given the half-life of ²²⁶Ra be 1600 year. Compute the value of Avogadro's no.

Sol:
$$\therefore$$
 Rate = λN_0 (No. of atoms in 1 g Ra) = (Av. No./226)
 $\therefore 11.6 \times 10^{17} = \frac{0.693}{1600} \times \frac{\text{AvogadroNumber}}{226}$
 \therefore Avogadro No. = 6.052 $\times 10^{23}$

Example 3: Half-life of an element is t second. Calculate the percentage left undecayed in t/2 sec.

Sol: $\frac{t}{2} = \frac{2.303 \times t}{0.693} \times \log \frac{N_0}{N}$ ∴ $\frac{N_0}{N} = 1.414$ or N = 0.707 × N₀ or 70.7%

Example 4: At a certain instant, a piece of radioactive material contains 10¹² atoms. The half-life of material is 30 days. Calculate the number of disintegration in the first second.

Sol: The disintegration number of atoms in first second means the initial rate of decay.

i.e., Rate = $-(dN / dt) = \lambda N_0$

Where N_0 is initial number of atoms.

Given, $N_0 = 10^{12}$ atoms and $t_{1/2} = 30 \times 24 \times 60 \times 60$ sec

 \therefore Rate = 0.693×10¹²/(30×24×60×60) = 2.674×10⁵ disintegration per second.

Example 5: At radioactive equilibrium, the ratio between two atoms of radioactive elements A and B are 3.1×10^9 : 1. If half-life period of A is 2×10^{10} years, what is half-life of B?

Sol: Use the relation between no. of atoms, integration constant and half-life.

$$\frac{N_A}{N_B} = \frac{\lambda_B}{\lambda_A} = \frac{t_{1/2A}}{t_{1/2B}}$$

At radioactive equilibrium; $A \rightarrow B$

$$\frac{N_A}{N_B} = \frac{\lambda_B}{\lambda_A} = \frac{t_{1/2A}}{t_{1/2B}} \qquad \qquad \because \quad \frac{3.1 \times 10^9}{1} = \frac{2 \times 10^{10}}{t_{1/2B}}$$

:
$$t_{1/2B} = 6.45$$
 year

Example 6: Write equations for the following transformation:

(a)
$${}^{14}_{7}N(n,p)$$
 (b) ${}^{39}_{19}K(n,\alpha)$

Sol: (a)
$${}^{14}_7$$
N+ 1_0 n \longrightarrow ${}^{14}_6$ C+ 1_1 H
(b) ${}^{39}_{19}$ K+ 1_0 n \longrightarrow ${}^{36}_{17}$ Cl+ 4_2 He

Example 7: Write equations for:

(a) Position emission by ${}^{18}_{9}$ F (b) β -emission by ${}^{35}_{16}$ S (c) α -emission by ${}^{235}_{92}$ U (d) Nuclear fusion (e) Gamma rays emission from ${}^{13}_{7}$ N (f) β^+ -emission by ${}^{22}_{11}$ Na **Sol:** (a) ${}^{18}_{9}$ F \longrightarrow ${}^{18}_{8}$ O + ${}^{0}_{+1}$ e (b) ${}^{35}_{16}$ S \longrightarrow ${}^{35}_{17}$ Cl + ${}^{0}_{-1}$ e (c) ${}^{235}_{92}$ U \longrightarrow ${}^{231}_{90}$ Th + ${}^{4}_{2}$ He (d) ${}^{2}_{1}$ H + ${}^{3}_{1}$ H \longrightarrow ${}^{4}_{7}$ He + ${}^{0}_{0}$ n + 17.6 MeV (e) ${}^{13}_{7}$ N \longrightarrow ${}^{13}_{7}$ N + γ (f) ${}^{22}_{11}$ Na \longrightarrow ${}^{22}_{10}$ Ne + ${}^{0}_{+1}$ e

Example 8: One g of $^{198}_{79}$ Au (t_{1/2} = 65 hrs) decays by β -emission to produced stable Hg.

(i) Write the nuclear reaction for process

(ii) How much Hg will be present after 260 hrs?

Sol: (i) The nuclear reaction is ${}^{198}_{79}$ Au $\longrightarrow {}^{198}_{80}$ Hg+ ${}^{0}_{-1}$ e (ii) Given, t_{1/2} = 65 hour;

T = 260 hour and amount of Au = 1 g

 \therefore T = t_{1/2} × n \therefore n = 260/65 = 4

Therefore, amount left undecayed = $N_0/2^4 = 1/2^4 = (1/16) g$

: Amount of Au decayed = [1 - (1/16)] = (15/16) g

: 198 g Au on decay gives 198 g Hg

 $\therefore \frac{15}{16} \text{ g Au on decay gives } \frac{198 \times 15}{16 \times 198} = \frac{15}{16} \text{gHg}$

Example 9: One of the hazards of nuclear explosion is the generation of ⁹⁰Sr and its subsequent incorporation in bones. This nuclide has a half-life of 28.1 years. Suppose one microgram was absorbed by a new-born child, how much ⁹⁰Sr will remain in his bones after 20 year?

Sol: Here we are provided with half-life period and initial amount of the sample.

By substituting the value in equation of radioactive decay amount of sample present at that time can be calculated.

Given $t_{1/2} = 28.1$ year; $N_0 = 10^{-6}$ g t = 20 year; N = ? Qt $= \frac{2.303}{\lambda} \log \frac{N_0}{N}$ $\therefore 20 = \frac{2.303 \times 28.1}{0.693} \log \frac{10^{-6}}{N}$ $\therefore N = 6.1 \times 10^{-7}$ g

Example 10: 54.5 mg Na₃PO₄ contains ³²P (15.6%) and ³¹P atoms. Assuming only ³²P atoms are radioactive, calculate the rate of decay for the given sample of Na₃PO₄. The half-life period for ³²P = 14.3 days; mol. wt. of Na₃PO₄ = 161.2.

Sol: First find out mole of ³²P preset in the given sample of Na₃PO₄ from mole calculate no of atoms present

(no. of atom present = mole x Avogadro no)

And then by using rate and integration constant relationship calculate the rate.

Mole of Na₃PO₄ = $\frac{54.5 \times 10^{-3}}{161.2}$ Mole of P-atoms = $\frac{54.5 \times 10^{-3}}{161.2}$ \therefore Mole of ³²P atoms = $\frac{54.5 \times 10^{-3}}{161.2} \times \frac{15.6}{100} = 5.27 \times 10^{-5}$ \therefore Atom of ³²P = $5.27 \times 10^{-5} \times 6.023 \times 10^{23}$ Now, Rate= λ .

$$N = \frac{0.693}{14.3 \times 24 \times 60 \times 60} \times 5.27 \times 10^{-5} \times 6.023 \times 10^{23}$$

Rate = 1.78×10^{13} dps.

JEE Advanced/Boards

Example 1: A sample of radioactive substance shows an intensity of 2.3 millicurie at a time t and an intensity of 1.62 millicurie 600 seconds later. What is half-life and average life of radioactive material?

Sol: In order to find out the half-life and average life of radioactive material we have to first calculate integration constant using equation for radioactive decay.

$$\begin{aligned} r_{1} &= 2.3 \times 10^{-3} \text{ curie, when } t = t_{1} \\ r_{2} &= 1.62 \times 10^{-3} \text{ curie, when } t = (600 + t_{1}) \text{ sec} \\ \frac{r_{1}}{r_{2}} &= \frac{2.3 \times 10^{-3}}{1.62 \times 10^{-3}} = \frac{N_{1}}{N_{2}} \end{aligned}$$

Now,
$$\lambda = \frac{2.303}{t} \log \frac{N_1}{N_2} = \frac{2.303}{600} \log \frac{2.3}{1.62} = 5.84 \times 10^{-4} \text{ sec}^{-1}$$

$$\therefore t_{1/2} = \frac{0.693}{\lambda} = \frac{0.693}{5.84 \times 10^{-4}} = 1186.15 \text{ second}$$

Also,
$$\tau = \frac{1}{\lambda} = \frac{1}{5.84 \times 10^{-4}} = 1712.33$$
 second

Example 2: How much energy would be evolved per hour from 1 curie of ¹⁴C source if all the energy of beta decay were imprisoned? Atomic masses of ¹⁴C and ¹⁴N are 14.00324 and 14.00307 amu respectively.

Sol: Using the relation for binding energy and mass defect calculate the energy term. And the calculated value of binding energy calculate energy would be evolved per hour from 1 curie of ¹⁴C source

$$^{14}_{6}C \longrightarrow ^{14}_{7}N + ^{0}_{-1}e$$

Δm = 14.00324– 14.00307 = 0.00017 amu

- : Energy produced during this decay of 1 atom
- = Δm × 931.478 MeV = 0.00017 × 931.478 MeV

= 0.158 MeV = 0.158 × 10⁶ eV

 $= 0.158 \times 10^{6} \times 1.602 \times 10^{-19}$ J $= 2.54 \times 10^{-14}$ J

Now 1 curie of ^{14}C means decay of 3.70 \times 10 10 dps. Thus, energy produced during decay of 1 curie mass of ^{14}C

= $3.70 \times 10^{10} \times 2.53 \times 10^{-14} \text{ Js}^{-1}$ = $9.36 \times 10^{-4} \text{ J}$

: Energy produced in 1 hr = $9.36 \times 10^{-4} \times 60 \times 60 = 3.37$ J

Example 3: What amount of energy is evolved by a curie of Rn (an α -emitter) (a) in one hour (b) its mean life? Given KE of one α -particles is 5.5 MeV and $\lambda = 2 \times 10^{-6} \text{ sec}^{-1}$

Sol: For Rn: Rate = λN_0 (::Rn=1 curie; Rate = 3.7×10^{10} dps)

 $3.7 \times 10^{10} = 2 \times 10^{-6} \times N_0$

 \therefore N₀ i.e., Number of atom of Rn at t = 0

 $= 1.85 \times 10^{16}$ atoms

(a) Let amount of Rn left after 1 hr be N

$$\therefore t = \frac{2.303}{\lambda} \log \frac{N_0}{N}$$

60 × 60 = $\frac{2.303}{2 \times 10^{-6}} \log \frac{1.85 \times 10^{16}}{N}$

∴ N = 1.837 × 10¹⁶

Thus, number of α formed = Number of Rn decayed (Rn is an α -emitter)

$$= N_0 - N = (1.85 \times 10^{16}) - (1.837 \times 10^{16}) = 0.013 \times 10^{16}$$

- \therefore Energy evolved = 0.013 × 10¹⁶ × 5.5 MeV
- $= 0.013 \times 10^{16} \times 5.5 \times 10^{6} \,\mathrm{eV}$
- $= 0.013 \times 10^{22} \times 5.5 \times 1.602 \times 10^{-19} \text{ J} = 114.5 \text{ J}$

(b) Let amount of Rn left after t = $(1/\lambda)$ is N, then

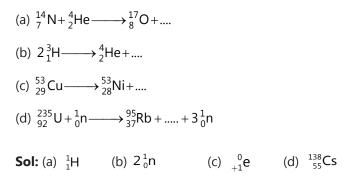
$$\frac{1}{\lambda} = \frac{2.303}{\lambda} \log \frac{1.85 \times 10^{16}}{N}$$
$$N = 0.6806 \times 10^{16}$$
Again number of a forma

Again number of α formed = N₀ – N

 $= 1.85 \times 10^{16} - 0.6806 \times 10^{16} = 1.1694 \times 10^{16}$

: Energy released = $1.1694 \times 10^{16} \times 5.5 \times 10^{6} \times 1.602 \times 10^{-19}$ J = 1.03×10^{4} J

Example 4: Complete the following nuclear reactions:



Example 5: The isotopic masses of ${}_{1}^{2}H$ and ${}_{2}^{4}He$ are 2.0141 and 4.0026 amu respectively. Calculate the quantity of energy liberated when two moles of ${}_{1}^{2}H$ undergo fission to form1 mole of ${}_{2}^{4}He$. The velocity of light in vacuum is 2.998 × 10⁸ m/sec.

Sol: Fusion reaction is $2_1^2 H \longrightarrow {}^4_2 He + energy$ Mass defect = 2 × Mass of ${}^2_1 H -$ Mass of ${}^4_2 He$ = 2 × 2.0141 – 4.0026 = 0.0256 amu

 $= 2 \times 2.0141 = 4.0020 = 0.0250$ and

:. Energy liberated during fusion of 2 atoms of ${}^{2}_{1}H = \Delta mc^{2}$

 $= 0.0256 \times 1.66 \times 10^{-27} \times (2.998 \times 10^8)^2 \text{ J} = 3.8 \times 10^{-12} \text{ J}$

Energy liberated during fusion of 2 N atoms of ${}_{1}^{2}$ H to give N atoms (or 1 mole ${}_{2}^{4}$ He) = 3.8 × 10⁻¹² × 6.023 × 10²³ = 2.3 × 10¹² J

Example 6: The radioactive disintegration of $^{239}_{94}$ Pu and α -emission process is accompanied by the loss of 5.24 MeV/dis. If t_{1/2} of $^{239}_{94}$ Pu is 2.44 × 10⁴ years, calculate the energy released per year from 1.0 g sample of $^{239}_{94}$ Pu in kJ.

Sol: First calculate the rate of disintegration and by multiplying it with energy lost during α emission will give us the value of energy released per year from 1.0 g sample of $^{239}_{94}$ Pu in kJ.

 $Rate = \lambda N = \frac{0.693 \times 6.023 \times 10^{23}}{2.44 \times 10^4 \times 239} = 7.157 \times 10^{16} \text{ dis/year}$

 \therefore Loss in energy per year = 5.24 × 7.157 × 10¹⁶ MeV

 $= 5.24 \times 7.157 \times 10^{16} \times 10^{6} \text{ eV}$

 $= 5.24 \times 7.157 \times 10^{16} \times 10^{6} \times 1.602 \times 10^{-19} \times 10^{-3} \text{ kJ} = 60.08 \text{ kJ}$

Example 7: A certain radioisotope ${}^{A}_{Z}X$ (t_{1/2}=10 day) decays to give ${}^{A-4}_{Z-2}Y$. If one g-atom ${}^{A}_{Z}X$ is kept in a sealed vessel, how much He will accumulate in 20 day at STP?

Sol: The nuclear reaction is ${}_{Z}^{A}X \longrightarrow {}_{Z-2}^{A-4}Y + {}_{2}^{4}He$ Given, $t_{1/2} = 10$ day; T = 20 day; $N_0 = 1$ g-atoms \therefore n = 2 (\because $n = T/t_{1/2}$) \therefore Amount left in 2 halves $= 1/2^2 = \frac{1}{4}$ g-atom \therefore Amount of X decayed in 2 halved $= \left(1 - \frac{1}{4}\right) = \frac{3}{4}$ g-atom or Amount of He formed = $\frac{3}{4}$ g-atom

(Since, 1 g-atom of X gives 1 g-atom of He)

:. Volume of He formed = $\frac{3}{4} \times 22400 = 16800$ mL at STP

Example 8: A radioactive isotope ${}^{m}_{z}A$ (t_{1/2} = 10 day) decays to give ${}^{m-12}_{Z-6}B$ stable atom along with α -particles. If m g of A are taken and kept in a sealed tube, how much He will accumulate in 20 day at STP?

Sol: The nuclear reaction is ${}_{Z}^{m}A \longrightarrow {}_{Z-6}^{m-12}B + 3 {}_{2}^{4}He$ Given, $t_{1/2} = 10$ day; t = 20 day, $N_{0} = mg = 1$ g-atom $\therefore n = 2$ ($\because n = T/t_{1/2}$) \therefore Amount left in 2 halves= $(1/2)^{2} = \frac{1}{4}$ g-atom

: Amount of A decayed in 2 halves

 $=\left(1-\frac{1}{4}\right) = \frac{3}{4}$ g-atom

: 1 g-atom of A gives 3 moles of He at STP

 $\therefore \frac{3}{4}$ g-atom of A give $3 \times \frac{3}{4}$

moles of He at STP = (9/4) moles of He at STP

:. Volume of He at STP = $(9/4) \times 22.4$ litre = 50.4 litre at STP

Example 9: The rate of decay of a radioactive sample is 3.02×10^6 dpm at time 10 mins and 1.20×10^6 dpm at a time 20 mins. Evaluate the decay constant, half-life and average life of sample.

Sol:
$$r_1 = \lambda . N_1$$
, $r_2 = \lambda . N_2$
 $\therefore \frac{r_1}{r_2} = \frac{N_1}{N_2} = \frac{3.02 \times 10^6}{1.20 \times 10^6} = 2.52$
Also, $10 = \frac{2.303}{\lambda} \log \frac{N_0}{N_1}$ $20 = \frac{2.303}{\lambda} \log \frac{N_0}{N_2}$
By eqs. (ii) - (i)
 $20 - 10 = \frac{2.303}{\lambda} \left[\log \frac{N_0}{N_2} - \log \frac{N_0}{N_1} \right]$
 $10 = \frac{2.303}{\lambda} \left[\log \frac{N_1}{N_2} \right] = \frac{2.303}{\lambda} \log 2.52$
 $\therefore \lambda = 0.092 \min^{-1}$

$$t_{1/2} = \frac{0.693}{\lambda} = \frac{0.693}{0.092} = 7.50 \text{ min}$$
$$T_{av} = \frac{1}{\lambda} = \frac{1}{0.092} = 10.87 \text{ min}$$

Example 10: Two radioactive nuclides P and Q have their decay constant in the ratio 3: 2. One mole of each is taken separately and allowed to decay, for a time interval of three times of the half-life of A. If 0.2 mole of P are left, what moles of Q will be left?

Sol: Let decay constant λ_{p} and λ_{Q} be 3a and 2a respectively.

$$t_{1/2} \text{ of } P = \frac{0.693}{3a}; \quad t_{1/2} \text{ of } Q = \frac{0.693}{2a}$$

At T = 3 × $t_{1/2}$ of;
$$P = \frac{3 \times 0.693}{3a} = \frac{0.693}{a}$$

 $\therefore T = \frac{2.303}{\lambda} \log \frac{a}{a-x}$
For P: $\frac{0.693}{a} = \frac{2.303}{2a} \log \frac{1}{n_p}$
For Q: $\frac{0.693}{a} = \frac{2.303}{2a} \log \frac{1}{n_q}$

$$= \frac{1}{\log \frac{1}{n_Q}} = \frac{1}{2} \quad \text{Or } \log \frac{1}{n_p} = \frac{1}{2} \log \frac{1}{n_Q}$$
$$\log \frac{1}{n_p} = \log \left(\frac{1}{n_Q}\right)^{3/2}$$

Or
$$n_{p} = (n_{Q})^{2/3}$$
 if $n_{p} = 0.2$, then $n_{Q} = 0.09$

JEE Main/Boards

Exercise 1

Q.1 One mole of A present in a closed vessel undergoes decay as: ${}_{Z}^{m}A \longrightarrow {}_{Z-2}^{m-8}B + 2 \begin{pmatrix} 4\\2 \end{pmatrix} What will be the volume of helium gas collected at STP after 20 days (t_{1/2} of A = 10 days)?$

Q.2 ¹³¹I has half-life period 13.3 hours, after 79.8 hours, what fraction of ¹³¹I will remain?

Q.3 With what velocity should an α -particle travel towards the nucleus of a copper atom so as to arrive at a distance of 10⁻¹³ meters from the nucleus of the copper atom?

Q.4 A radioactive isotope ${}_{z}^{m}A$ (t_{1/2} = 10 day) decays to give ${}_{z-6}^{m-12}B$ stable atom along with α -particles. If m g of A are taken and kept in a sealed tube, how much He will accumulate in 20 days at STP?

Q.5 A solution contains 1 millicurie of L-phenyl alanine ¹⁴C (uniformly labelled) in 2.0 mL solution. The specific activity of labeled sample is given as 150 millicurie/millimol. Calculate: (A) the concentration of the sample in the solution in mol/litre.

(B) The activity of the solution in terms of counting per minute/mL at a counting efficiency of 80%.

Q.6 $^{40}_{19}$ K consists of 0.012% of the potassium in nature. The human body contains 0.35% potassium by weight. Calculate the total radioactivity resulting from $^{40}_{19}$ K decay in a 75 kg human. Half-life for $^{40}_{19}$ K is 1.3 × 10⁹ year.

Q.7 A follows a parallel path I order reaction giving B and C. If the initial concentration of A is 0.25 M, calculate the concentration of C λ_{2} after 5 hours of reaction.



[Given: $\lambda_1 = 1.5 \times 10^{-5} \text{ s}^{-1}$, $\lambda_2 = 5 \times 10^{-6} \text{ s}^{-1}$]

Q.8 Calculate the energy associated with the following nuclear reaction:

Q.9 On analysis, a sample of uranium was found to

contain 0.277 g of $_{82}$ Pb²⁰⁶ and 1.667 g of $_{92}$ U²³⁸. The halflife period of U²³⁸ is 4.51 × 10⁹ yrs. If all the lead were assumed to have come from decay of $_{92}$ U²³⁸, what is the age of the earth?

Q.10 A certain radioisotope ${}^{A}_{Z}X$ (t_{1/2}=10 day) decays to give ${}^{A-4}_{Z-2}Y$ If one g-atom ${}^{A}_{Z}X$ is kept in a sealed vessel, how much He will accumulate in 20 day at STP?

Exercise 2

Single Correct Choice Type

Q.1 Atoms ${}_{7}X^{A}$, ${}_{8}Y^{B}$ and ${}_{9}Z^{17}$ are such that ${}_{8}Y$ is an isobar of ${}_{7}X$ and atom ${}_{9}Z^{17}$ is isotone of ${}_{8}Y$. Mass no. of X and no. of neutrons in Y are respectively as follows:

Q.2 The number of neutrons accompanying in the formation of ${}_{54}X^{139}$ and ${}_{38}Sr^{194}$ by the absorption of slow neutron by ${}_{92}U^{235}$ followed by nuclear fission is:

(A) 0	(B) 1	(C) 2	(D) 3
-------	-------	-------	-------

Q.3 The activity of a radioactive nuclide (X¹⁰⁰) is 6.023 curie at a certain time 't'. If its disintegration constant is $3.7 \times 10^4 \text{ s}^{-1}$ the mass of X after t sec is:

(A) 6.022×10 ⁶ g	(B) 10 ⁻¹³ g
(C) 10 ⁻¹⁵ g	(D) 10 ⁻¹⁷ g

Q.4 The half-life of ${}_{6}C^{14}$ is 5730 years. What fraction of its original C¹⁴ would be left after 22920 years of storage? (A) 0.50 (B) 0.25 (C) 0.125 (D) 0.0625

Q.5 A radioactive sample had an initial activity of 56 dpm. After 69.3 minutes, it was found to have an activity of 28 dpm. Find the number of atoms in a sample having an activity of 100 dpm.

(A) 693	(B) 100	(C) 1000	(D) 10,000

Q.6 A sample of radioactive substance is found 90% of its initial amount after one day. What % of the original sample can be found after 3 days?



Q.7 The present activity of the hair of Egyptian mummy is 1.75 dpm. $t_{1/2}$ of ${}_{6}C^{14}$ is 5770 years and disintegration rate of fresh sample of C^{14} is 14 dpm. Find out the age of the mummy,

(A) 23080 years	(B) 138480 years
(C) 11998.3 years	(D) 17313.6 years

Q.8 20% of the initial weight of a radioactive element undergoing decay is left after certain period of time r. How many such periods should elapse from the start for 50% of the element to be left over?

(A) 3 (B) 4 (C) 5 (D) None

Q.9 The half-life of Tc⁹⁹ is 6.0 hrs. The total residual activity in a patient 30 hrs after receiving an injection containing Tc⁹⁹ must be more than 0.01 μ C_i, What is the maximum activity (in μ C_i) that the sample injected can have?

(A) 0.16 (B) 0.32 (C) 0.64 (D) 0.08

Q.10 A pure radio-chemical preparation was observed to disintegrate at the rate of 2140 counts/minutes at 12.35 P.M. At 3.55 P.M. of the same day, the disintegration rate of the sample was only 535 count/minutes. What is the half-life of the material?

Q.11 A radioactive substance decays 25% in 10 minutes. If at start there are 4×10^{20} atoms present, after what time will the number of atoms be reduced to 10^{20} atoms?

(A) 10.98 min (B) 21.97 min (C) 48.19 min (D) None

Q.12 The time of decay for a nuclear reaction is given by $t = 4t_{1/2}$. The relation between the mean life (T) and time of decay (t) is given by:

(A) 2 Tln 2 (B) 4Tln 2 (C) 2T⁴ln 2 (D)
$$\frac{1}{T_2}$$
 ln 2

Q.13 Two radio isotopes A and B of atomic weight X and Y are mixed in equal amount by weight. After 20 days, their weight ratio is found to be 4: 1. Isotope A has a half-life of 1 day. The half-life of isotope B is:

(A) 1.11 $\frac{y}{x}$ day	(B) 0.11
(C) 0.6237 day	(D) 1.11 day

Q.14 Two radioactive nuclides A and B have half-lives 50 mins and 10 mins respectively. A fresh sample contains the nuclide of B to be eight times that of A. How much time should elapse so that the number of nuclides of A becomes double of B?

(A) 30	(B) 40	(C) 50	(D) 100
(,,) 50		(c) 50	(0) 100

Q.15 A radioactive nuclide is produced at a constant rate of α per second. Its decay constant is λ If N₀ is the no. of nuclei at time t = 0, then max. number of nuclei possible are:

(A)
$$N_0$$
 (B) α/λ (C) $N_0 + \frac{\alpha}{\lambda}$ (D) $\frac{\lambda}{\sigma} + N_0 s$

Q.16 An analysis of the rock shows that the relative number of Sr^{87} and Rb^{87} ($t_{1/2} = 4.7 \times 10^{10}$ years) atoms is 0.05. What is the age of the rock? Assume all Sr^{87} to be formed from Rb^{87} only,

(A) 7.62 x 10 ⁹ year	(B) 1.43 x 10 ⁹ year
(C) 3.28 x 10 ⁹ year	(D) 4.32 x 10 ⁸ year

Q.17 There are two radio nuclei A and B. A is a α -emitter and B is β -emitter, their disintegration constants are in the ratio of 1: 2. What should be the number of atoms of two at time t = 0, so that probability of getting α and β -particles are same at time t = 0

Q.18 A radioactive substance (parent) decays to its daughter element, the age of the radioactive substance (t) is related to the daughter (D)/parent (p) ratio by the equation:

(A)
$$t = \frac{1}{\lambda} ln \left(1 + \frac{p}{d} \right)$$

(B) $t = \frac{1}{\lambda} ln \left(1 + \frac{d}{p} \right)$
(C) $t = \frac{1}{\lambda} ln \left(\frac{d}{p} \right)$
(D) $t = \frac{1}{\lambda} ln \left(\frac{p}{d} \right)$

The decay follows two parallel paths: What are the decay constants (λ) for Th and Fr respectively?

(A) 0.03087, 0.00063

Q.19 C²²⁷ has a half-life of 22 years.

(B) 0.00063,	0.03087	

(C) 0.02, 0.98 (D) None of these

Q.20₈₄Po²¹⁸ (t_{1/2} = 183 secs) decay to ₈₂Pb (t_{1/2} = 161 secs) by α -emission, while Pb²¹⁴ is an a β -emitter. In an experiment starting with 1 mole of pure Po²¹⁸, how much time would be required for the number of nuclei of ₈₂Pb²¹⁴ to reach maximum?

Previous Years' Questions

Q.1 The radionuclide $^{234}_{90}$ Th undergoes two successive β decays followed by one α -decay. The atomic number and the mass number respectively of the resulting radionuclide are **(2003)**

(A) 92 & 234 (B) 94 & 230 (C) 90 & 230 (D) 92 & 230

Q.2 A photon of hard gamma radiation knocks a proton out of $^{24}_{12}$ Mg nucleus to form (2005)

(A) The isotope of parent nucleus

(B) The isobar of parent nucleus

(C) The nuclide ²³₁₁Na

(D) The isobar of ²³₁₁Na

Q.3 The reaction which disintegrates neutrons or neutron is emitted (which completes first) (2005)

(A) $_{96}Am^{240} + _{2}He^{4} \rightarrow _{97}Bk^{244} + _{+1}e^{0}$	(B) $_{15}P^{30} + _{14}Si^{30} + _{1}e^{0}$
(C) ${}_{6}C^{12} + {}_{1}H^{1} \rightarrow_{7}N^{13}$	(D) $_{13}AI^{27} + _{2}He^{4} + _{15}P^{30}$

Q.4 Consider the following nuclear reactions.

${}^{238}_{92}M \longrightarrow {}^{x}_{y}N + 2{}^{4}_{2}He; {}^{x}_{y}N \rightarrow {}^{A}_{B}L + 2\beta^{+}$			
The number of neutrons in the element L is		(2004)	
(A) 140	(B) 144	(C) 142	(D) 146
Q.5 β-particle	e is emitted in r	adioactivity by	(2004)
(A) Conversion of proton to neutron			

(B) From outermost orbit

(C) Conversion of neutron to proton

(D) α -particle is not emitted

Q.6 A freshly prepared radioactive source of half-life 2 hours emits radiations of intensity which is 64 times the permissible safe level. The minimum time after which it would be possible to work safely with this source is **(1988)**

(A) 6 hours (B) 12 hours (C) 24 hours (D) 128 hours

Q.7 The half-life period of a radioactive element is 140 days. After 560 days, one gram of the element will reduce to (1999)

(A) 1/2 g
(B) 1/4 g
(C) 1/8 g
(D) 1/16 g
Q.8 Disintegration constant for a radioactive substance is 0.58 hr⁻¹. Its half-life period is (2004)
(A) 8.2 hr
(B) 5.2 hr
(C) 1.2 hr
(D) 2.4 hr

Q.9 Radium has atomic weight 226 and a half-life of

1600 years. The number of disintegrations produced per second from 1 g are: (1990)

(A) 4.8×10¹⁰ (B) 9.2×10⁶ (C) 3.7×10¹⁰ (D) Zero

Q.10. The half-life of a radioisotope is four hours. If the initial mass of the isotope was 200 g, the mass remaining after 24 hours undecayed is **(2004)**

(A) 3.125 g (B) 2.084 g (C) 1.042 g (D) 4.167 g

Q.11 In the transformation of $^{238}_{92}U$ to $^{234}_{92}U$, if one emission is an α -particle, what should be the other emission(s) (2006)

(A) Two β⁻	(B) Two β⁻ and one β⁺

(C) One β^- and one γ (D) One β^+ and one β^-

Q.12 Carbon-14 dating method is based on the fact that (1997)

- (A) Carbon-14 fraction is the same in all objects
- (B) Carbon-14 is highly insoluble
- (C) Ratio of carbon-14 and carbon-12 is constant
- (D) All of these

Q.13Which of the following nuclear reactions will
generate an isotope(2007)

- (A) Neutron particle emission (B) Positron emission
- (C) α -particle emission (D) β -particle emission

Q.14 The half-life of a radioactive isotope is three hours. If the initial mass of the isotope were 256 g, the mass of it remaining undecayed after 18 hours would be **(2003)**

(A) 4.0 g (C) 12.0 g (B) 8.0 g (D) 16.0 g

JEE Advanced/Boards

Exercise 1

Q.1 α -particle accelerated by 3 × 10⁵ volt bombarded a boron target. This resulted in the nuclear reaction. ${}_{2}^{4}\text{He} + {}_{5}^{10}\text{B} \longrightarrow {}_{6}^{13}\text{C} + {}_{1}^{1}\text{H} + \gamma$

If the combined energy of ¹³C and ¹H is 5×10^5 eV, calculate energy, frequency and g of g-rays. 1×10^5 eV energy is used in penetration of the nucleus. Given H = 1.008 amu.He = 4.0026 amu, B = 10.0129 amu, C = 13.0036 amu and 1 amu = 931 MeV.

Q.2 1 g-atom of ²²⁶Ra is placed in an evacuated tube of volume 5 litres. Assuming that each ²²⁶₈₈Ra nucleus is an α -emitter and all the contents are present in the tube, calculate the total pressure of gases and partial pressure of He collected in tube at 27° C after the end of 800 years. t_{1/2} of Ra is 1600 years. Neglect the volume occupied by undecayed Ra.

Q.3 The rate of decay of a radioactive sample is 3.02×10^6 dpm at time 10 mins and 1.20×10^6 dpm at a time 20 mins. Evaluate the decay constant, half-life and average life of the sample.

Q.4 A solution contains a mixture of isotopes of ${}_{x}A_{1}(t_{1/2} = 14 \text{ day}) \text{ and } {}_{x}A_{2}(t_{1/2} = 25 \text{ day})$. The total activity is 1 curie at t = 0. The activity reduces by 50% in 20 days. Find:

(A) The initial activities of ${}_{x}A_{1}$ and ${}_{x}A_{2}$

(B) The ratio of their initial no. of nuclei.

Q.5 For the following sequential reaction

 $A \xrightarrow{\lambda_1} B \xrightarrow{\lambda_2} C$

find out the concentration of C at time t = 1 day, given the $\lambda_{1'}$ =1.8 × 10⁻⁵ s⁻¹ and λ_2 = 1.1 × 10⁻² s⁻¹and initial molar concentration of A is 1.8 M.

Q.6 A radioactive isotope decays as

$${}^{m}_{Z}A \longrightarrow {}^{m-4}_{Z-2}B \longrightarrow {}^{m-4}_{Z-1}C$$

The half-lives of A and B are 10 months and 6 months respectively. Assuming that initially only A was present, will it be possible to achieve radioactive equilibrium for B. If so what would be the ratios of A and B at equilibrium? What would happen if the half-lives of A and B were 6 months and 10 months respectively?

Q.7 A sample of pitch blende is found to contain 50% uranium and 2.425% lead. Of this lead only 93% was Pb²⁰⁶ isotope. If the disintegration constant is 1.52×10^{-10} yr⁻¹, how old could be the pitch blende deposits?

Q.8 A sample contains two radioactive nuclei x and y with half-lives 2 hours and 1 hour respectively. The nucleus x-decays to y and y-decays into a stable nucleus z. At t = 0 the activities of the components in the same were equal. Find the ratio of the number of the active nuclei of y at t = 4 hours to the number at t = 0.

Q.9 ⁶⁴Cu (half-life-12.8 hrs) decays by β^- -emission (38%), β^+ -emission (19%) and electron capture (43%). Write the decay products and calculate partial half-lives for each of the decay processes.

Q.10 Tritium ${}_{1}^{3}$ T (an isotope of H) combines with fluorine to form a weak acid TF which ionizes to give T⁺. Tritium is radioactive and is a β -emitter. A freshly prepared dilute aqueous solution of TF has a pT (equivalent of pH) of 1.7 and freezes at -0.372°C. If 600 mL of freshly prepared solution were allowed to stand for 24.8 years, calculate: (i) lonization constant of TF.

(ii) Charge carried by β -particles

Emitted by tritium in Faraday.

[Given: K_f for $H_2 O = 1.86$, $t_{1/2} (T) = 12.4$ yrs.]

Q.11 The half-life of ²¹²Pb is 10.6 hours. It undergoes decay to its daughter (unstable) element ²¹²Bi of half-life 60.5 minutes. Calculate the time at which the daughter element will have maximum activity.

Q.12 Prove that time required for 99.9% decay of a radioactive species is almost ten times its half-life period.

Q.13 The sun radiates energy at the rate of 4×10^{26} J sec⁻¹. If the energy of fusion process is 27 MeV, calculate the amount of hydrogen that would be consumed per day for the given process. 4_1^1 H $\longrightarrow \frac{4}{2}$ He+ 2_1^0 e.

Exercise 2

Single Correct Choice Type

Q.1 Upon irradiating californium with neutrons, a scientist discovered a new nuclide having mass number of 250 and a half-life of 30 min. After 90 min. of irradiation, the observed radioactivity T due to nuclide was 100 dis/min. How many atoms of the nuclide were prepared initially?

(A) 2.4×10^4 (B) 3.46 × 10⁴ (C) 1900 (D) 800

Q.2. A radioactive isotope X with half-life of 6.93×10^9 years decays to Y which is stable. A sample of rock from the moon was found to contain both the elements X and Y in the mole ratio1: 7. What is the age of the rock?

(A) 2.079×10^{10} years	(B) 1.94×10^{10} years
(C) 1.33×10^9 years	(D) 10 ¹⁰ years

Q.3 The average (mean) life of a radio nuclide which decays by parallel path is

$A \xrightarrow{\lambda_1} B;$	$\lambda_1 = 1.8 \times 10^{-2}$	sec ⁻¹	
$2A \xrightarrow{\lambda_2} B; \ \lambda_2 = 10^{-3} \text{ sec}^{-1}$			
(A) 52.63 sec	(B) 500 sec	(C) 50 sec	(D) None

Q.4 The radioactive decay $_{_{83}}\text{Bi}^{_{211}} \rightarrow {}_{_{81}}\text{TI}^{_{207}}\text{, takes place}$ in 100 L closed vessel at 27°C. Starting with 2 moles of $_{83}$ Bi²¹¹ (t_{1/2} = 130 secs), the pressure development in the vessel after 520 secs will be:

(A) 1.875 atm	(B) 0.2155 atm
(C) 0.4618 atm	(D) 4.618 atm

Q.5 A fresh radioactive mixture containing short lived species A and B. Both emitting α -particles initially of 8000 α -particles per minute. 20 minutes later, they emit at the rate of 3500 α -particles per minute. If the half-lives of the species A and B are 10 minutes and 500 hours respectively, then the ratio of activities of A:B in the initial mixture was:

(A) 4:6 (B) 6: 4 (C) 3:4 (D) 3: 1

Q.6 In order to determine the volume of blood in an animal, 1.0 mL sample of solution of 10³ dpm of ₁H³ is injected into the animal blood stream. After sufficient time for circulatory equilibrium to be established, 2 mL of blood is found to have activity to 10 dpm. The volume of blood in animal is:

(A) 199 mL (B) 198 mL (C) 200 mL (D) 20 mL

Q.7. The ratio of the activities of two radio nuclides X and Y in a mixture at time t = 0 was found to be 4: 1. After two hours, the ratio of the activities becomes 1: 1. If the $t_{1/2}$ of radio nuclide X is 20 mins then $t_{1/2}$ [in minutes] of radio nuclide Y is:

(A) 10 (B) 20 (C) 30 (D) 40

Q.8. Find the age of an ancient Egyptian wooden article (in years) from the given information.

(i) Activity of 1 g of carbon obtained from ancient wooden article = 7 counts/min/g

(ii) Activity of 1 g carbon obtained from fresh wooden sample = 15.4 counts per min/g

(iii) Percentage increase in level of C¹⁴ due to nuclear explosions in the past 100 years is 10%

(iv) $t_{1/2} \text{ of }_{6}C^{14} = 5770 \text{ years}$	
(A) 5.770 × 10 ³	(B) 16.87 × 10 ³

(C) 2488 (D) None of these

Multiple Correct Choice Type

Q.9 Select the correct statement(s):

(A) α -particles are simply helium atoms

(B) γ -rays travel with higher speed as compare to α -particle and have higher ionization power as compared to b-particles.

(C) A loss of β -particles results in the production of isobars

(D) β -particles are considered as the best bombarding particles

Q.10 Select the correct statement(s):

(A) In the reaction ${}_{92}U^{235} + {}_{0}n^1 \rightarrow {}_{56}Ba^{140} + 2 {}_{0}n^1 + x,$ produced x is ₂₆Kr⁹⁴

(B) In the reaction $_{11}Na^{23} + z \rightarrow _{12}Mg^{23} + _{0}n^{1}$ the bombarding particle z is deuteron

(C) Very large amounts of energy is produced during nuclear fission and nuclear fusion

(D) In a fission reaction, a loss in mass occurs releasing a vast amount of energy

Q.11 Select the correct statement(s):

(A) SI unit of radioactivity is Becquerel (Bq)

(B) 1 Ci = 3.7×10^7 Bq

(C) $_{3}\text{Li}^{7} + _{1}\text{H}^{1} \longrightarrow _{2}\text{He}^{4}$ is (P, α) type reaction

(D) The half-life of a particular radio active isotope is a characteristic constant of that isotope

Q.12 Select the correct statement (s):

(A) On bombarding $_7N^{14}$ nuclei with α -particle, the nuclei of the product formed after release of proton would be $_8O^{17}$

(B) Decay constant does not depend upon temperature

(C) Nuclide and its decay product after $\alpha\text{-emission}$ are called isodiaphers

(D) Half-life of radium is 1580 years.

Its average life will be 1097.22 years.

Q.13 In the decay process

 $A \xrightarrow{-\alpha} B \xrightarrow{-\beta} C \xrightarrow{-B} D$

(A) A and B are isobars

(B) A and D are isotopes

(C) B, C and D are isobars

(D) A and C are isotones

Comprehension Type

Paragraph 1: Radioactive disintegration is a first order reaction and its rate depends only upon the nature of the nucleus and does not depend upon external factors like temperature and pressure. The rate of radioactive

disintegration (Activity) is represented as $-\frac{dN}{dt} = \lambda N$

Where λ = decay constant; N = N₀ of nuclei at time t; N₀ = initial no. of nuclei

The above equation after integration can be represented

as
$$\lambda = \frac{2.303}{t} log \left(\frac{N_0}{N} \right)$$

Q.14 Half-life period of U^{237} is 2.5×10^5 years. In how much time will the amount of U^{237} remaining be only 25% of the original amount?

(A) 2.5×10^5 years	(B) 1.25 × 10 ⁵ years
(C) 5 \times 10 ⁵ years	(D) 10 ⁶ years

Q.15 Calculate the half-life period of a radioactive element which remains only 1/16 of its original amount in 4740 years:

(A) 1185 years	(B) 2370 years
(C) 52.5 years	(D) None of these

Q.16 What is the activity in Ci (curie) of 1.0 mole of Plutonium-239? ($t_{1/2}$ = 24,000 years)

(A) 1.49 Ci	(B) 14.9 Ci
(C) 5.513 × 10 ¹¹ Ci	(D) None

Paragraph 2: Size of nucleus was obtained by the equation $r = R_0 A^{1/3}$, where r is the radius of nucleus of mass number A and R_0 is a constant whose value is equal to 1.5×10^{15} metres. (Given 1 amu = 1.66×10^{-24} g)

Q.17 What is the density of a nucleus of mass number A?

(A) $\frac{4}{3}\pi (1.5 \times 10^{-15})^3$	(B) 1.17 × 10 ¹⁷ g/cm ³
(C) 1.17 × 10 ⁻¹⁷ kg/m ³	(D) None of these

Q.18 Nucleus radius of ${}_{6}C^{12}$ is 3 × 10⁻¹⁵ metres. What is the density ratio of d_c / d_{H-Q} ?

(A) 1.76 × 10 ¹⁷	(B) 1.76 × 10 ¹⁴
(C) 17.6 × 10 ⁷	(D) 17.6 × 10 ¹⁷

Match the Columns

Q.19

Column I	Column II
(A) Isotones	(p) ₁₉ Pa ²³⁴ & ₉₀ Th ²³⁴
(B) Isobars	(q) ₆ C ¹² & ₆ C ¹⁴
(C) Isotopes	(r) $_{19}$ K ³⁹ and ₉ F ¹⁹
(D) Isodiaphers	(s) $_{18}$ Ar ³⁹ and $_{19}$ K ⁴⁰

Q.20

Column I	Column II
(A) α -emission no.	(p) Change in mass
(B) β-emission	(q) No change in atomic no and mass no
(C) γ-emission decreases	(r) Atomic no.
(D) β ⁺ (Positron)	(s) Atomic no. increases

Previous Years' Questions

Q.1 If uranium (mass number 238 and atomic number 92) emits an α -particle, the product has mass number and atomic number (1981)

(A) 236 and 92	(B) 234 and 90
(C) 238 and 90	(D) 236 and 90

Q.2 An isotope of Ge_{32}^{76} is		(1984)
(A) Ge ⁷⁷ ₃₂	(B) As ⁷⁷ ₃₃	

(C) Se ⁷⁷ ₃₄	(D) Se ⁷⁸ ₃₄

Q.3 The radiation from a naturally occurring radioactive substance, as seen after deflection by a magnet in one direction, are (1984)

(A) Definitely alpha rays

(B) Definitely beta rays

(C) Both alpha and beta rays

(D) Either alpha rays or beta rays

Q.4 $^{27}_{13}AI$ is a stable isotope $^{29}_{13}AI$ is expected to decay by (1996)

nission
1

(C) Positron emission (D) Proton emission

Q.5 The number of neutrons accompanying the formation of ${}^{139}_{54}$ Xe and ${}^{94}_{38}$ Sr from the absorption of a slow neutron by ${}^{235}_{92}$ U, followed by nuclear fission is

(1999) (A) 0 (B) 2 (C) 1 (D) 3

Q.6 $_{23}$ Na is the more stable isotope of Na. Find out the process by which $^{24}_{11}$ Na can undergo radioactive decay. *(2003)*

(A) β-emission	(B) α -emission
(C) β-emission	(D) K-electron capture

Q.7 A positron is emitted from $^{23}_{11}$ Na. The ratio of the atomic mass and atomic number of the resulting nuclide is (2007)

(A) 22/10 (B) 22/11 (C) 23/10 (D) 23/12

Q.8 The nuclear reactions accompanied with emission of neutron(s) are (1988)

- (A) $^{17}_{13}\text{Al} + ^{4}_{2}\text{He} \longrightarrow ^{30}_{15}\text{P}$
- (B) ${}^{12}_{6}C + {}^{1}_{1}H \longrightarrow {}^{13}_{7}N$
- (C) ${}^{30}_{15}P \longrightarrow {}^{30}_{14}Si + {}^{0}_{1}e$
- (D) ${}^{241}_{96}Am + {}^{4}_{2}He \longrightarrow {}^{244}_{97}Bk + {}^{0}_{1}e$

Q.9 Decrease in atomic number is observed during (1998)

(A) Alpha emission	(B) Beta emission
(C) Positron emission	(D) Electron capture

Read the following questions and answer as per the direction given below:

(A) Statement-I is true; statement-II is true; statement-II is the correct explanation of statement-I.

(B) Statement-I is true; statement-II is true; statement-II is not the correct explanation of statement-I.

(C) Statement-I is true; statement-II is false.

(D) Statement-I is false; statement-II is true.

Q.10 Statement-I: Nuclide $^{30}_{13}AI$ is less stable than $^{40}_{20}Ca$.

Statement-II: Nuclides having odd number of protons and neutrons are generally unstable. (1998)

Q.11 The number of neutrons emitted when $^{235}_{92}$ U undergoes controlled nuclear fission to $^{142}_{54}$ Xe and $^{90}_{38}$ Sr is (2010)

Q.12 $_{92}X^{234} \xrightarrow{-7\alpha}_{-6\beta}$ Y. Find out atomic number, mass number of y and identify it. (2004)

Q.13 The total number of α and β particles emitted in the nuclear reaction $_{_{92}}U^{_{238}} \rightarrow _{_{82}}Pb^{_{214}}$ is (2009)

(A) Statement I is true; statement-II is true; statement-II is the correct explanation of statement-I.

(B) Statement-I is true; statement-II is true; statement-II is not the correct explanation of statement-I.

(C) Statement-I is true; statement-II is false.

(D) Statement-I is false; statement-II is true.

Q.14 Statement-I: The plot of atomic number (y-axis) versus number of neutrons (x-axis) for stable nuclei shows a curvature towards x-axis from the line of 45° slope as the atomic number is increased.

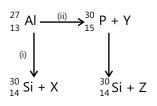
Statement-II: Proton-proton electrostatic repulsions begin to overcome attractive forces involving protons and neutrons and neutrons in heavier nuclides. *(2008)*

Q.15 Given that the abundances of isotopes ⁵⁴Fe, ⁵⁶Fe and ⁵⁷Fe are 5%, 90% and 5% respectively, the atomic mass of Fe is **(2009)**

(A) 55.85	(B) 55.95
(C) 55.75	(D) 56.05

(2012)

Q.16 Bombarment of aluminum by aparticle leads to its artificial disintegration in two ways, (i) and (ii) as shown. Products X, Y and Z respectively are, (2011)



(A) Proton, neutron, positron(B) Neutron, positron, proton

(C) Proton, positron, neutron

(D) Positron, proton, neutron

Q.17 The periodic table consists of 18 groups. An isotope of copper, on bombarment with protons, undergoes a nuclear reaction yielding element X as shown below. To which group, element X belongs in the periodic table?

$$^{30}_{15}$$
Cu $+^{1}_{1}$ H $\rightarrow 6^{1}_{0}$ n + α + 2^{1}_{1} H + X

Q.18 In the nuclear transmutation(2013) ${}^9_4Be + X \longrightarrow {}^8_4Be + Y$ (A) (γ, n) (B) (p, D)(C) (n, D)(D) (γ, p)

Q.19 A closed vessel with rigid walls contains 1 mol of $^{238}_{92}$ U and 1 mol of air at 298 K. Considering complete decay of $^{238}_{92}$ U to $^{206}_{82}$ Pb, the ratio of the final pressure to the initial pressure of the system at 298 K is **(2015)**

PlancEssential Questions

JEE Main/Boards

Exercise 1

Q.1 Q.6 Q.11

Exercise 2

Q.2 Q.7 Q.9 Q.15

Previous Years' Questions

Q.4 Q.14

JEE Advanced/Boards

Exercise 1

Q.1 Q.5 Q.10 Q.14

Exercise 2

Q.4 Q.6 Q.8 Q.13

Previous Years' Questions

Q.3

Answer Key

JEE Main/Boards

Exercise 1

Q.1 33.6 litre	Q.2 $\frac{1}{64}$	Q.3 6.3 × 10 ⁶ m sec ⁻¹	Q.4 50.4 litre at STP
Q.5 3.33 × 10 ⁻³ M, 88.8	01	Q.6 4.81 × 10 ⁵ dpm	Q.7 7.56 × 10 ⁻³ M
Q.8 6.70 MeV	Q.9 1.143 × 10 ⁹ years	Q.10 16800mL at STP	

Exercise 2

Single Correct	Choice Type						
Q.1 D	Q.2 D	Q.3 C	Q.4 D	Q.5 D	Q.6	В	Q.7 D
Q.8 D	Q.9 B	Q.10 B	Q.11 C	Q.12 B	Q.13	D	Q.14 C
Q.15 B	Q.16 C	Q.17 A	Q.18 B	Q.19	3 Q.20	В	
Previous Ye	ears' Questio	ons					
Q.1 C	Q.2 C	Q.3 D	Q.4 B	Q.5. C	Q.6 B	Q.7 D	Q.8 C
Q.9 C	Q.10 . A	Q.11 A	Q.12 C	Q.13 A	Q.14 A		
JEE Adv	anced/Bo	ards					
Exercise 1							
Q.1 λ = 3.4 × 1	0 ⁻¹³ m	Q.2 1.443 atm		Q.3 T _{avg} = 10.8	7 min	0	¹ / ₂ = 0.3255
Q.5 [C] _t = 1.42	М	Q.6 1.66		Q.7 t = 3.3 × 1	0 ⁸ year	Q.8 $\frac{[N_y]}{[N_y]}$	$\frac{l_t}{l_0} = 0.25$
Q.9 $t_{1/2}$ for electron	tron capture = 2	9.78 hr		Q.10 0.054 Far	aday	Q.11 22	27.1 min
Q.12 10		Q.13 5.31 × 10) ¹⁹ g				
Exercise 2							
Single Correct	Choice Type						
Q.1 B	Q.2 A	Q.3 C	Q.4 C	Q.5 D	Q.6 A	Q.7 C	Q.8 A
Multiple Corre	ect Choice Type						
Q.9 C	Q.10 A, C, D	Q.11 A, C, D	Q.12 A	, B, C Q.130	В, С		
Comprehensic	on Type						
Paragraph 1:	Q.14 C	Q.15 A	Q.16 B				
Paragraph 2:	Q.17 B	Q.18 B					
Match the Col	umns						
Q.19 A \rightarrow s; B	ightarrow p; C $ ightarrow$ q; E	$D \rightarrow r$	Q.20 A	\rightarrow p, r; B \rightarrow s;	$C \rightarrow q; D \rightarrow$	r	
Previous Ye	ears' Questio	ons					
Q.1 B	Q.2 A	Q.3 D		Q.4 B	Q.5 B		Q.6 A
Q.7 C	Q.8 A,D	Q.9 A, C	C, D	Q.10 B	Q.11 3		Q.12 Y is ₈₄ Po ²⁰⁶
Q.13 8	Q.14 A	Q.15 B		Q.16 A	Q.17 8	(Q.18 A, B

Q.19 9

ENVIRONMENTAL CHEMISTRY

1. ENVIRONMENT AND ENVIRONMENTAL POLLUTION

1.1 Environmental Pollution

It is the effect of undesirable changes in our surroundings that have harmful effects on plants, animals and human beings.

1.2 Pollutant

A substance, which causes pollution, is known as a pollutant. Pollutants can be solid, liquid or gaseous substances present in greater concentration than in natural abundance.

1.3 Classification of Pollutants

- (a) Pollutants can be Natural or Anthropogenic
 - (i) Natural pollutants: These are produced due to natural happenings like volcano eruptions etc.
 - (ii) Anthropogenic pollutants: These are produced due to human activities.
- (b) Pollutants can be Biodegradable or Non-biodegradable
 - (i) **Biodegradable Pollutants:** These are the pollutants which are rapidly broken down by natural processes. Example: discarded vegetables.
 - (ii) Non-biodegradable pollutants: These are the pollutants which are slowly degradable, and remain in the environment in an unchanged form for many decades. For example: DDT, plastic materials, heavy metals, many chemicals, nuclear wastes etc.

1.4 Types of Environmental Pollution

Environmental pollution is of three types.

- (b) Atmospheric pollution:
 - (i) Tropospheric pollution (ii) Stratospheric Pollution
- (b) Water pollution
- (c) Soil and land pollution

2. ATMOSPHERIC POLLUTION

2.1 Atmospheric Pollution: An Introduction

Atmospheric pollution occurs when in the normal composition of the air, a new chemical substance is added or formed and builds up to undesirable proportions causing harm to humans, other animals, vegetation and materials.

2.2 Layers of Atmosphere

Earth's atmosphere can be divided (called atmospheric stratification) into five main layers. From highest to lowest, these layers are:

- (a) Exosphere: > 700 km (> 440 miles)
- (b) Thermosphere: 80 to 700 km (50 to 440 miles)
- (c) Mesosphere: 50 to 80 km (31 to 50 miles)

- (d) Stratosphere: 12 to 50 km (7 to 31 miles)
- (e) Troposphere: 0 to 12 km (0 to 7 miles)

2.3 Tropospheric Pollution

Tropospheric pollution: It is caused because of two types of pollutants:

- (a) Gaseous air pollutants: These are oxides of sulphur, nitrogen and carbon, hydrogen sulphide, hydrocarbons, ozone and other oxidants.
- (b) **Particulate pollutants:** Particulate pollutants are the minute solid particles or liquid droplets in air. These are present in vehicle emissions, smoke particles from fires, dust particles and ash from industries. Examples of particulate pollutants are dust, mist, fumes, smoke, smog etc.

2.4 Gaseous Air Pollutants

2.4.1 Oxides of Sulphur as Pollutant

Sources: Burning of fossil fuels containing sulphur

Harmful effects:

- (a) Causes respiratory diseases e.g., asthma, bronchitis, emphysema in human beings.
- (b) Sulphur dioxide causes irritation to the eyes, resulting in tears and redness.
- (c) High concentration of sulphur dioxide leads to stiffness of flower buds which eventually fall off from plants.

2.4.2 Oxides of Nitrogen as Pollutant

Sources:

- (a) At high altitudes when lightning strikes, dinitrogen and dioxygen combine to form oxides of nitrogen.
- (b) During the burning of fossil fuel in an automobile engine, at high temperature, dinitrogen and dioxygen combine to yield significant quantities of nitric oxide (NO) and nitrogen dioxide (NO₂).

 $N_2(g) + O_2(g) \xrightarrow{1483K} 2 \text{ NO}(g);$ $2\text{NO}(g) + O_2(g) \longrightarrow 2\text{NO}_2(g)$

Harmful effects:

- (a) Damage the leaves of plants and retard the rate of photosynthesis
- (b) Nitrogen dioxide is a lung irritant that can lead to an acute respiratory disease in children
- (c) It is toxic to living tissues also
- (d) Nitrogen dioxide is also harmful to various textile fibers and metals

2.4.3 Hydrocarbons as Pollutant

Source: Incomplete combustion of fuel used in automobiles.

Harmful effect:

- (a) Hydrocarbons are carcinogenic, i.e., they cause cancer
- (b) They harm plants by causing ageing, breakdown of tissues and shedding of leaves, flowers and twigs

2.4.4 Oxides of Carbon as Pollutant

(b) Carbon Monoxide

Source:

- (a) Incomplete combustion of carbon of coal, firewood, petrol, etc.
- (b) By automobile exhaust

Harmful Effects: It is highly poisonous to living beings because of its ability to block the delivery of oxygen to the organs and tissues. It binds to hemoglobin to form carboxyhemoglobin, which is about 300 times more stable than the oxygen-hemoglobin complex. In blood when the concentration of carboxyhemoglobin reaches about 3-4 percent, the oxygen carrying capacity of blood is greatly reduced. This oxygen deficiency, result into headache, weak eyesight, nervousness and cardiovascular disorder.

(c) Carbon Dioxide

Source:

- (a) Respiration
- (b) Burning of fossil fuels for energy
- (c) By decomposition of limestone during the manufacture of cement
- (d) By volcanic eruptions
- (e) Deforestation

Harmful Effects: Causes global warming

2.5 Greenhouse Effect and Global Warming

(a) **Greenhouse effect:** About 75% of the solar energy reaching the earth is absorbed by the earth's surface, which increases its temperature. The rest of the heat radiates back to the atmosphere. Some of the heat is trapped by gases such as carbon dioxide, methane, ozone, chlorofluorocarbon compounds (CFCs) and water vapors in the atmosphere. Thus, they add to the heating of the atmosphere. This causes global warming.

This trapping of the sun's heat near the earth's surface and keeping it warm is called natural greenhouse effect. It maintains the temperature and makes the earth perfect for life.

If the amount of carbon dioxide crosses the delicate proportion of 0.03 percent, the natural greenhouse balance may get disturbed. This may lead to global warming.

- (b) **Green house:** In a greenhouse, visible light passes through the transparent glass and heats up the soil and the plants. The warm soil and plants emit infrared radiations. Since glass is opaque to infrared (heat) radiations, it partly reflects and partly absorbs these radiations. This mechanism keeps the energy of the sun trapped in the greenhouse.
- (c) Global Warming: An increase in the average temperature of the earth's atmosphere (especially a sustained increases that causes climatic changes) which may be caused by additional heat being trapped by greenhouse gases.
- (d) Acid Rain: Normally rain water has a pH of 5.6 due to the presence of H⁺ ions formed by the reaction of rain water with carbon dioxide present in the atmosphere.

$$H_2O(I) + CO_2(g) \implies H_2CO_3(aq); \qquad H_2CO_3(aq) \implies 2H^+ + CO_3^{2^-}$$

(e) Source: Burning of fossil fuels (which contain sulphur and nitrogenous matter) such as coal and oil in power stations and furnaces or petrol and diesel in motor engines produce sulphur dioxide and nitrogen oxides. SO₂ and NO₂ after oxidation and reaction with water are major contributors to acid rain, because polluted air usually contains particulate matter that catalysis the oxidation.

 $2SO_2(g) + O_2(g) + 2H_2O(l) \longrightarrow 2H_2SO_4(aq); 4NO_2(g) + O_2(g) + 2H2O(l) \longrightarrow 4HNO_3(aq)$

(f) Harmful Effects:

- Harmful for agriculture, trees and plants as it dissolves and washes away nutrients needed for their growth.
- Causes respiratory ailments in human beings and animals.
- Affects plant and animal life in aquatic ecosystem when acid rain falls and flows as ground water to reach rivers, lakes etc.
- Corrodes water pipes resulting in the leaching of heavy metals such as iron, lead and copper into the drinking water.
- Damages building and other structures made of stone or metal. The Taj Mahal in India has been affected by acid rain.

2.6 Particulate Pollutants

Particulates in air may be Viable or Non-Viable.

(a) Viable are minute living organisms that are dispersed in the atmosphere.

Example: bacteria, fungi, moulds, algae etc.

- (b) Non-viable particulates may be classified as:
 - (i) **Smoke particulates:** Consist of solid or mixture of solid and liquid particles formed during combustion of organic matter.

Example: cigarette smoke, smoke from burning of fossil fuel, garbage and dry leaves, oil smoke etc.

- (ii) **Dust:** Composed of fine solid particles (over 1mm in diameter), produced during crushing, grinding and attribution of solid materials. Sand from sand blasting, saw dust from wood works, pulverized coal, cement and fly ash from factories, dust storms etc., are some typical examples of this type of particulate emission.
- (iii) **Mists:** Are produced by particles of spray liquids and by condensation of vapors in air. Example: Sulphuric acid mist and herbicides and insecticides that miss their targets and travel through air and form mists.
- (iv) Fumes: Are generally obtained by the condensation of vapors during sublimation, distillation, boiling and several other chemical reactions. Generally, organic solvents, metals and metallic oxides form fume particles.

2.7 Smog

Smoke is a mixture of smoke, dust particles and small drops of fog.

Table 7.3: Classification of smog

	Classical Smog	Photochemical Smog	
1.	It occurs in cool humid climate.	1.	It occurs in warm, dry and sunny climate
2.	It is a mixture of smoke, fog and sulphur dioxide.	2.	Components of photochemical smog result from the action of sunlight on unsaturated hydrocarbons & oxides of nitrogen produced by automobiles and factories.
3	It is also called reducing smog.	3.	It is also called oxidizing smog.

2.7.1 Formation of Photochemical Smog

Burning of fossil fuels

$$\downarrow$$

Emission of a variety of pollutants (hydrocarbons and nitric oxide to troposphere)

At high levels, lead to
$$\downarrow$$

Chain reaction between pollutants and sunlight:

$$2NO(g) + O_{2}(g) \xrightarrow{\text{sunlight}} 2NO_{2}(g)$$

$$NO_{2}(g) \xrightarrow{\text{sunlight}} NO(g) + O(g)$$

$$O(g) + O_{2}(g) \xrightarrow{} O_{3}(g)$$

$$O_{3}(g) + NO(g) \longrightarrow NO_{2}(g) + O_{2}(g)$$

$$\downarrow$$

NO₂ and O₃ are strong oxidizing agents and can react with the unburnt hydrocarbons in the polluted air to produce chemicals such as formaldehyde, acrolein and Peroxyacetyl Nitrate (PAN).

2.7.2 Effects of Photochemical Smog

- Ozone and PAN act as powerful eye irritants.
- Ozone and nitric oxide irritate the nose and throat and their high concentration causes headache, chest pain, and dryness of the throat, cough and difficulty in breathing.
- Photochemical smog leads to cracking of rubber and extensive damage to plant life.
- It also causes corrosion of metals, stones, building materials, rubber and painted surfaces.

2.7.3 Control of Photochemical Smog

- Use of catalytic converters in automobiles, which prevent the release of nitrogen oxide and hydrocarbons to the atmosphere.
- Certain plants e.g., Pinus, Juniparus, Quercus, Pyrus and Vitis can metabolize nitrogen oxide and therefore, their plantation could help in this matter.

2.8 Stratospheric Pollution

Stratospheric pollution is basically due to ozone layer depletion

2.8.1 Formation of Ozone in Stratosphere

 $O_2(g) \xrightarrow{V} O(g) + O(g); \qquad O(g) + O_2(g) \rightleftharpoons O_3(g)$

2.8.2 Depletion of Ozone Layer

Release of chlorofluorocarbon compounds (CFCs), also known as freons lead to their mixing with the normal atmospheric gases and eventually reach the stratosphere.

In stratosphere,
$$CF_2CI_2(g) \xrightarrow{UV} CI(g) + G_2CI(g)$$

 $CI(g) + O_3(g) \longrightarrow CIO(g) + O_2(g)$
 $CIO(g) + O(g) \longrightarrow CI(g) + O_2(g)$

This way, the chlorine radicals are continuously regenerated and cause the breakdown of ozone layer.

2.8.3 Ozone Hole Over Antarctica

In summer season, nitrogen dioxide and methane react with chlorine monoxide and chlorine atoms forming chlorine sinks, preventing much ozone depletion.

 $CIO(g) + NO_2(g) \longrightarrow CIONO_2(g);$ $CI(g) + CH_4(g) \longrightarrow CH_3(g) + HCI(g)$

In winter, special type of clouds called polar stratospheric clouds are formed over Antarctica. These polar stratospheric clouds provide surface on which chlorine nitrate formed gets hydrolysed to form hypochlorous acid.

$$CIONO_2(g) + H_2O(g) \longrightarrow HOCI(g) + HNO_3(g)$$

It also reacts with hydrogen chloride produced to give molecular chlorine.

$$CIONO_2(g) + HCI(g) \longrightarrow CI_2(g) + HNO_3(g)$$

When sunlight returns to the Antarctica in the spring, the sun's warmth breaks up the clouds and HOCl and Cl_2 are photolysed by sunlight.

$$HOCI(g) \xrightarrow{hv} OH(g) + CI(g); \qquad CI_2(g) \xrightarrow{hv} 2CI(g)$$

The chlorine radicals thus formed, initiate the chain reaction for ozone depletion.

2.8.4 Effects of Depletion of the Ozone Layer

With the depletion of ozone layer, more UV radiation filters into troposphere. UV radiations lead to:

- Ageing of skin, cataract, sunburn and skin cancer etc. in human beings
- Killing of many phytoplanktons
- Damage to fish productivity
- Affect the plant proteins which lead to the harmful mutation of cells
- Increases the evaporation of surface water through the stomata of the leaves and decreases the moisture content of the soil
- Increases in UV radiations damage paints and fibres, causing them to fade faster

3. WATER POLLUTION

Water pollution is the contamination of water bodies (e.g. lakes, rivers, oceans, aquifers and groundwater). Water pollution occurs when pollutants are directly or indirectly discharged into water bodies without adequate treatment to remove harmful compounds.

Major water pollutants	Sources	Harmful effects
Pathogens (Micro-organisms)	Domestic sewage	Cause gastrointestinal diseases.
Organic wastes (leaves, grass, trash)	Domestic sewage, animal excreta and waste, decaying animals and plants, discharge from food processing factories	Lead to decreases in concentration of dissolved oxygen in water and lead to death of aquatic life
Plant nutrients	Chemicals fertilizers	
Toxic heavy metals (cadmium, mer- cury, nickel)	Industries and chemical factors	Can damage kidneys, central ner- vous system, liver etc
Sediments	Erosion of soil by agriculture and strip mining	
Pesticides (insecticides, herbicides, fungicides)	Chemicals used for killing insects, fungi and weeds	Leads to eutrophication
Radioactive substances	Mining of uranium containing minerals	
Heat	Water used for cooling in industries	

Table 7.4: Sources and harmful effects of water pollutions

Biochemical Oxygen Demand (BOD): The amount of oxygen required by bacteria to break down the organic matter present in a certain volume of a sample of water is called BOD.

Eutrophication: The process in which nutrient enriched water bodies support a dense plant population, which kills animal life by depriving it of oxygen and results in subsequent loss of biodiversity, is known as eutrophication.

Constituent	Maximum Concentration	Harmful effects of higher concentration
Fluoride	1ppm or 1 mg d m ⁻³	Causes brown mottling of teeth
Lead	50 ppb	Can damage kidney, liver, reproductive system etc
Sulphate	500 ppm	Causes laxative effect
Nitrate	50 ppm	Causes disease such as methemoglobinemia ('blue baby' syndrome)
Metals		
Fe	0.2 ppm	
Al	0.05 ppm	
Mn	0.2 ppm	
Cu	3.0 ppm	

Table 7.5: Major constituents of Drinking Water

Constituent	Maximum Concentration	Harmful effects of higher concentration
Zn	5.0 ppm	
Cd	0.005 ppm	

4. SOIL POLLUTION

Soil pollutions is defined or can be described as the contamination of soil of a particular region. Soil pollution mainly is a result of penetration of harmful pesticides and insecticides, which on one hand serve whatever their main purpose is, but on the other hand bring about deterioration in the soil quality, thus making it contaminated and unfit for use later.

Pesticides: They are basically synthetic toxic chemicals with ecological repercussions.

Herbicides: They are used to kill weeds or undesirable vegetation.

Example: Sodium chlorate (NaClO₃), sodium arsinite (Na₃AsO₃).

5. STRATEGIES TO CONTROL ENVIRONMENTAL POLLUTION

5.1 Water Management

Segregate the waste as biodegradable and non-biodegradable waste

(a) Biodegradable waste:

- (i) Generated by cotton mills, food processing units, paper mills, and textile factories.
- (ii) Management: are deposited in landfills and are converted into compost

(b) Non-biodegradable water:

- (i) Generated by thermal power plants which produce fly ash; integrated iron and steel plants which produce blast furnace slag and steel melting slag
- (ii) Management
 - Recycling
 - Toxic wastes are usually destroyed by controlled incineration

6. GREEN CHEMISTRY

Green chemistry is a strategy to design chemical processes and products that reduces or eliminates the use and generation of hazardous substances. The chemical reactions should be such that the reactants are fully converted into useful environment friendly products by using an environment friendly medium so that there would be no chemical pollutants introduced in the environment.

6.1 Green Chemistry in Everyday Life

Purpose	Earlier	Now
Dry cleaning of clothes	Tetrachloroethene ($CI_2C = CCI_2$) which contaminates the ground water	Liquefied carbon dioxide, with a suitable detergent
Bleaching of Paper	Chlorine gas	Hydrogen peroxide (H_2O_2) with suitable catalyst

Table 7.5: Examples of green chemicals

Solved Examples

JEE Main/Boards

Example 1 Explain giving reasons "The presence of CO reduces the amount of heaemoglobin available in the blood for carrying oxygen to the body cells."

Sol: CO combines with haemoglobin of the red blood corpuscles (RBCs) about 200 times more easily than oxygen to form carboxyhaemoglobin reversibly as follows:

Hb + CO 🗲 HbCO.

Thus, it is not able to combine with oxygen to form oxyhaemoglobin and transport of oxygen to different body cells cannot take place.

Example 2 What is the composition of 'photochemical smog'?

Sol: It is a mixture of a number of irritation causing compounds like $NO_{2^{\prime}}$, $O_{3^{\prime}}$ peroxyacylnitrates (PAN), aldehydes, ketones, hydrocarbons and CO.

Example 3 What is COD? Why is it preferred over BOD? How is it determined?

Sol: COD stands for Chemical Oxygen Demand. It is preferred over BOD (Biochemical Oxygen Demand) because BOD takes a number of days, e.g., BOD5 takes 5 days whereas COD can be determined in a very short time. For method of determination of COD, refer to page 14/28.

Example 4 Give three examples in which green chemistry has been applied.

Sol: (i) In dry cleaning, use of liquefied CO_2 in place of tetrachloroethene

 $(\mathsf{Cl}_2\mathsf{C}=\mathsf{CCl}_2).$

(ii) In bleaching of paper using H_2O_2 in place of chlorine.

(iii) In the manufacture of chemicals like ethanol using environment-friendly chemicals and conditions.

Example 5 A farmer was using pesticides on his farm. He used the produce of his farm as food for rearing fishes. He was told that fishes were not fit for human consumption because large amount of pesticides had accumulated in the tissue of fishes. Explain how did this happen?

Sol: From the soil, the pesticides traveled into the crops produced by the farmer. From the crops, used as food for rearing fish, the pesticides entered into water from where they finally entered into the bodies of the fishes.

Example 6 How can you apply green chemistry for the following:

(i) To control photochemical smog.

(ii) To avoid use of halogenated solvents in dry cleaning and that of chlorine in bleaching.

(iii) To reduce use of synthetic detergents.

(iv) To reduce the consumption of petrol and diesel.

Sol: (i) Refer to 'control of photochemical smog'.

(ii) In dry cleaning, liquefied CO_2 along with a suitable detergent is used and for bleaching, hydrogen peroxide is used which gives better results and is not harmful.

(iii) Soaps should be used in place of detergents because soaps are 100% biodegradable and do not cause any pollution problem. Now a days, soft detergents are available which are biodegradable. They can used in place of 'hard detergents' which are non-biodegradable.

(iv) (a) CNG (Condensed Natural Gas) may be used as it causes much less pollution.

(b) Electrical vehicles should be used which have zero pollution. We expect a large number of electrical cars and two wheelers on the road in near future.

JEE Main/Boards

Exercise 1

Q.1 What are the primary and secondary pollutants of the air?

Q.2 Ozone is a gas heavier than air. Why does ozone layer not settle down near the earth?

Q.3 What are the main components of our environment? Explain each of them briefly

Q.4 What are the different regions of the atmosphere? Explain each of them briefly.

Q.5 As we go up above the earth's surface, does temperature decrease continuously? Explain.

Q.6 What is air pollution? What are the main sources of air pollution? Write a few lines about each of them.

Q.7 What are major air pollutants?

Q.8 What do you understand by?

(i) Mists (ii) Smoke (iii) Fumes and (iv) Dust?

Q.9 Why we should not use Freon as coolants in refrigerating equipment's?

Q.10 How is photochemical smog formed? What are its effects? How can it be controlled?

Exercise 2

(A) CO₂

Single Correct Choice Type

01	Which	of the	following	is the	coldest r	eaion?
Q. I	VVIIICII	or the	TOHOWING	is the	Coluest	egioni

(A) Troposphere (B) Mesosphere

(C) Stratosphere (D) Thermosphere

Q.2 Which of the following is a secondary pollutant?

(B) N₂O (C) SO₂ (D) PAN

Q.3 All are primary pollutants except

(Λ) CO	
(A) SO ₂	(B) H_2SO_4

(C) NO₂ (D) Particulate matter

Q.4 The most abundant hydrocarbon pollutant is

Q.5 The size of particulates of $\textbf{H}_{2}\textbf{SO}_{4}$ fog lies in the range

(A) 5-100 nm	(B) 100-500 nm
(C) 500-1000 nm	(D) 1000-10,000 nm

Q.6 The aromatic compounds present as particulates are

- (A) Benzene (B) Toluene
- (C) Nitrobenzene (D) Polycyclic hydrocarbons

Q.7 'White lung cancer' is caused by

(A) Asbestos (B) Silica (C) Textile (D) Paper

Q.8 Ozone layer is present in

(A) Troposphere (B) stratosphere

(C) Mesosphere (D) Exosphere

Q.9 Depletion of ozone layer causes

(A) Blood cancer	(B) Lung cancer
(C) Skin cancer	(D) Breast cancer

Q.10 Which one of the following is responsible for depletion of the ozone layer in the upper strata of the atmosphere?

(A) Polyhalogens(B) Ferrocene(C) Fullerenes(D) Freons

Q.11 London smog is found in

(A) Summer during day time

(B) Summer during morning time

- (C) Winter during morning time
- (D) Winter during day time

Q.12 Photochemical smog is formed in

(A) Summer during morning time

- (B) Summer during day time
- (C) Winter during morning time
- (D) Winter during day time

Q.13 Which of the following is true about photochemical smog?

- (A) It is reducing in nature
- (B) It is formed in winter
- (C) It is a mixture of smoke and fog
- (D) It causes irritation in eyes

Q.14 The smog is essentially caused by the presence of

(A) O_2 and O_3	(B) O_2 and N_2
(C) Oxides of sulphur and nitrogen	(D) O_3 and N_2

Q.15 Pick up the correct statement:

(A) CO which is a major pollutant resulting from the combustion of fuels in automobiles which plays a major role in photochemical smog

(B) Classical smog has an oxidizing character while the (B) Greenhouse effect is responsible for global warming photochemical smog is reducing in character

(C) Photochemical smog occurs in day time whereas the classical smog occurs in the morning hours

(D) During formation of smog the level of ozone in the atmosphere goes down

(E) Classical smog is good for health but not photochemical smog.

Previous Years' Questions

Q.1 When rain is accompanied by a thunderstorm, the collected rain water will have a pH value (2003)

(A) Slightly higher than that when the thunderstorm is not there

(B) Uninfluenced by occurrence of thunderstorm

(C) Which depends on the amount of dust in air

(D) Slightly lower that that of rain water without thunderstorm

Q.2 The smog is essentially caused by the presence of (2004)

 $(A) O_2 and O_3$ $(B) O_{2} and N_{2}$

(C) Oxides of sulphur and nitrogen $(D) O_2$ and O_2

Q.3 Identify the wrong statements in the following:

(2008)

(A) Chlorofluorocarbons are responsible for ozone layer depletion

(C) Ozone layer does not permit infrared radiation from the sun to reach the earth

(D) Acid rains is mostly because of oxides of nitrogen and sulphur

Q.4 The gas leaked from a storage tank of the Union Carbide plant in Bhopal gas tragedy was (2013)

(A) Methylisocyanate (B) Methylamine

(C) Ammonia (D) Phosgene

Q.5 Assertion: Nitrogen and Oxygen are the main components in the atmosphere but these do not react to form oxides of nitrogen.

Reason: The reaction between nitrogen and oxygen requires high temperature. (2015)

(A) Both Assertion and reason are correct, and the reason is the correct explanation for the assertion.

(B) Both Assertion and reason are correct, but the reason is the not correct explanation for the assertion.

(C) The Assertion is incorrect, but the reason is correct.

(D) Both the Assertion and Reason are incorrect.

Q.6 What is DDT among the following: (2012)

(A) Greenhouse gas

(B) A fertilizer

(C) Biodegradable pollutant

(D) Non-biodegradable pollutant

PlancEssential Questions

JEE Main/Boards

Exercise 1		
Q.2	Q.9	Q.10
Exercise 2		
Q.5	Q.7	Q.10

		A	nswer K	ey			
JEE Main/Boards							
Exercise 2							
Single Correct Choice Type							
Q.1 B	Q.2 D	Q.3 B	Q.4 A	Q.5 C	Q.6 D	Q.7 C	Q.8 B
Q.9 C	Q.10 D	Q.11 C	Q.12 B	Q.13 D	Q.14 C	Q.15 C	
Previous Years' Questions							
Q.1 D	Q.2 C	Q.3 C	Q.4 A	Q.5 A	Q.6 D		

Solutions

JEE Main/Boards

Exercise 1

Nuclear Chemistry

Sol 1: We know that.

N = N₀
$$\left(\frac{1}{2}\right)^n$$
 where, N = remaining mole of A
N = 1 $\left(\frac{1}{2}\right)^n = \frac{1}{4}$

Number of decayed moles $=1 - \frac{1}{4} = \frac{3}{4}$

Number of moles of helium formed

= 2 × number of decayed moles of A = 2 × $\frac{3}{4} = \frac{3}{2}$ Volume of helium at STP = $\frac{3}{2}$ × 22. 4 = 33.6 litre

Sol 2: N = N₀
$$\left(\frac{1}{2}\right)^n$$
 $\therefore \frac{N}{N_0} = \left(\frac{1}{2}\right)^6 = \frac{1}{64}$

Sol 3:
$$\frac{1}{2}$$
mu² = $\frac{1}{4\pi \in_0} \times \frac{2Ze^2}{r}$ or $u^2 = \frac{Ze^2}{\pi \in_0 .m.r}$
 $u_2 = \frac{29 \times (1.6 \times 10^{-19})^2}{3.14 \times 8.85 \times 10^{-12} \times (4 \times 1.672 \times 10^{-27}) \times 10^{-13}}$

 $u = 6.3 \times 10^6 \text{ m sec}^{-1}$

Sol 4: The nuclear reaction ${}_{Z}^{m}A \longrightarrow {}_{Z-6}^{m-12}B + 3\frac{4}{2}He$ Given, $t_{1/2} = 10$ day; t = 20 day, $N_0 = mg = 1$ g-atom n = 2 ($\because n = T/t_{1/2}$) \therefore Amount left in 2 halves = $(1/2)^2 = \frac{1}{4}$ g-atom \therefore Amount of A decayed in 2 halves $= \left(1 - \frac{1}{4}\right) = \frac{3}{4}$ g-atom \therefore 1 g-atom of A gives 3 moles of He at STP $\therefore \frac{3}{4}$ g-atom of A give $3 \times \frac{3}{4}$ moles of He at STP $= \left(\frac{9}{4}\right)$ moles of He at STP = (9/4) moles of He at STP \therefore Volume of He at STP = (9/4) \times 22. 4 litre = 50.4 litre at STP

Sol 5: (a)1 m mole = 150 m curie

m curie = 1/150 m mole Now, concentration = $\frac{\text{m mole}}{\text{V in mL}}$ = $\frac{1}{150 \times 2}$ = 3.33 × 10⁻³ M (b) 1 curie = 3.7 × 10¹⁰ dps = 3.7 × 10¹⁰ × 60 dpm = 3.7 × 10¹⁰ × 60 × (80/100) counting per minute

 \therefore 1 millicurie = 3.7 × 10¹⁰ × 60 × (80/100) × 10⁻³ cpm

:. cpm/mL = $3.7 \times 10^{10} \times 60 \times (80/100) \times (10^{-3}/2)$ = 88.8×10^7 cpm/mL

Sol 6: Total amount of ${}^{49}_{19}$ K = $\frac{0.012}{100} \times \frac{0.35}{100} \times 75 \times 10^3 = 3.15 \times 10^{-2}$ g = $\frac{3.15 \times 10^{-2} \times 6.023 \times 10^{23}}{40} = 4.74 \times 10^{20}$ atoms ∴ Rate = λ × Number of atoms $\frac{0.693}{1.3 \times 10^9 \times 365 \times 24 \times 60} \times 4.74 \times 10^{20}$

Rate = 4.81×10^{5} dpm

Sol 7: $\lambda_{A} = 1_{1} + 1_{2} = 1.5 \times 10^{-5} + 5 \times 10^{-6} = 20 \times 10^{-6} \text{ s}^{-1}$ Also, 2.303 log $\frac{[A]_{0}}{[A]_{t}} = \lambda \times t$ \therefore 2.303 log $\frac{0.25}{[A]_{t}} = 20 \times 0^{-6} \times 5 \times 60 \times 60$ $[A]_{*} = 0.1744 \text{ M}$

: [A] decomposed = $[A]_0 - [A]_1 = 0.25 - 0.1744$ = 0.0756 M

Fraction of C formed

$$= \left[\frac{\lambda}{\lambda_1 + \lambda_2}\right] \times [A]_{decomposed} \times \frac{2}{5}$$
$$= 0.0756 \times \frac{5 \times 10^{-6}}{20 \times 10^{-6}} \times \frac{2}{5} = 7.56 \times 10^{-3} \text{ M}$$

Note that, 5 moles of A are used to give 2 mole of C.

Sol 8: Mass defect

= (26.9815 + 2.0141) - (24.9858 + 4.0026) = 0.0072 amu Energy of the reaction = 0.0072×931 MeV = 6.70 MeV

Sol 9: Moles of
$$U^{218} = \frac{1.667}{238}$$

Moles of $Pb^{206} = \frac{0.277}{206}$
 $N_0 = \frac{1.667}{238} + \frac{0.277}{206}$ and $N = \frac{1.667}{238}$
 $t = \frac{2.303}{\lambda} \log \frac{N_0}{N} = \frac{2.303 \times 4.51 \times 10^9}{0.693} \log_{10} \frac{\frac{1.667}{238} + \frac{0.277}{206}}{\frac{1.667}{238}}$
 $= 1.143 \times 10^9$ years

Sol 10: The nuclear reaction is

^A_ZX $\longrightarrow {A-4 \atop Z-2}^{A-4}$ Y + ${}^{4}_{2}$ He Given, t1/2 = 10 day, T = 20 day; N0 = 1-atoms \therefore n = 2 (n = T/t_{1/2}) \therefore Amount left in 2 halves = 1/22 = $\frac{1}{4}$ g-atom \therefore Amount of X decayed in 2 halves = $\left(1 - \frac{1}{4}\right) = \frac{3}{4}$ g-atom Or amount of He formed = $\frac{3}{4}$ g-atom (since 1 g-atom of X gives 1 g-atoms of He) \therefore Volume of He formed = $\frac{3}{4} \times 22400 = 16800$ mL at STP

Exercise 2

Single Correct Choice Type

Sol 1: (D) Isotones have same number of neutron:

$$17 - 9 = B - 8$$

B = 16
Isobars have same mass number
A = B = 16
Number of neutrons 16 - 8 = 8

Sol 2: (D)
$$_{92}U^{235} +_0 n^1 \longrightarrow {}_{54}X^{139} + {}_{38}Sr^{194} + 3_0n^1$$

Sol 3: (C) $A = \lambda N$ $6.023 \times 3.7 \times 10^{10} = 3.7 \times 10^4 N$ $N = 6.023 \times 10^6 \text{ atoms}$ 1 mole of $6.023 \times 10^{23} \text{ atoms} = 100 \text{ g of } X$ $\therefore 6.023 \times 10^6 \text{ atoms}$ $\Rightarrow \frac{100}{6.023 \times 10^{23}} \times 6.023 \times 10^6 = 10^{-15} \text{ g}$

Sol 4: (D) Four half-lives (Total time = $n \times f$ -life so, n = 4), hence 0.0625

Sol 5: (D)
$$\lambda = \frac{0.693}{69.3} = 10^{-2} \text{ min}^{-1}$$

N = $\frac{-\frac{dN}{dt}}{\lambda} = \frac{100}{10^{-2}} = 10,000$

Sol 6: (B) Equal fraction decay in equal periods of time, fraction of sample remaining after 3 days

$$\Rightarrow (0.9)^3 = 0.729$$
Sol 7: (D) t = $\frac{1}{\lambda} ln\left(\frac{A_0}{A}\right) \Rightarrow t = \frac{5770}{0.693} ln8$

$$\Rightarrow 17313. 6 \text{ year}$$

Sol 8: (D) t for 20% left

$$\Rightarrow t_1 = \frac{2.303}{\lambda} \log \frac{1}{1 - 0.8} = \frac{\ln 5}{\lambda}$$

t for 50% left

$$\Rightarrow t_2 = \frac{1}{\lambda} \ln 2$$
$$\frac{t_2}{t_1} = \frac{\frac{1}{\lambda} \ln 2}{\frac{1}{\lambda} \ln 5} = 0.43$$
$$t_2 = 0.43 t_1$$

Sol 9: (B) Total time = nt_{1/2};

n = 5; $\frac{\text{Initialactivity}}{2^{n}}$ Initial activity = 0.01 × 2⁵ = 0.32 µC₁

Sol 10: (B)
$$\lambda t = \ln \left(\frac{A_0}{A}\right) = \frac{0.693}{t_{1/2}} \times 200 = \ln \left(\frac{2140}{535}\right)$$

= $t_{1/2} = 100$ min.

Sol 11: (C)

t = 48.19

$$\lambda = \frac{1}{10} \ln \left(\frac{100}{100 - 25} \right)$$
$$t = \frac{1}{\lambda} \ln \left(\frac{N_0}{N} \right)$$
$$t = \frac{10}{\ln \left(\frac{4}{3} \right)} \times \ln \left(\frac{4 \times 10^{20}}{10^{20}} \right)$$

Sol 12: (B) $t_{1/2} = \frac{t}{4}$; $t_{1/2} = T \ln 2$ so $\frac{t}{4} = T \ln 2$; $t = 4t \ln 2$ Sol 13: (D) W_0 = initial wt ; $W \Rightarrow$ wt. after 20 days $\lambda_A = \frac{2.303}{t} \log \left(\frac{W_0}{W_A} \right)$; $\lambda_B = \frac{2.303}{t} \log \left(\frac{W_0}{W_B} \right)$ $\lambda_A - \lambda_B = \frac{2.303}{t} \log \left(\frac{W_B}{W_A} \right)$ So $\lambda_B = 0.6237$ $\therefore (t_{1/2})_B = \frac{0.693}{0.6237} \log \left(\frac{W_B}{W_A} \right) = 1.11 \text{ day}$ Sol 14: (C) Given $(n_0)B = 8 \times (n_0)_{A'}$; $(n)_A = 2 \times (n)_B$ $\lambda_A - \lambda_B = \frac{2.303}{t} \log \left[\frac{(N_A)_0}{(N_A)} \times \frac{(N_B)}{(N_B)_0} \right]$

$$T = \frac{\ln\left(\frac{1}{16}\right)}{\frac{0.693}{50} - \frac{0.693}{10}} = 50 \text{ min}$$

Sol 15: (B) As per given $\frac{dN}{dt} = \alpha \propto \lambda N$ for max. Number of nuclei

$$\frac{dN}{dt}$$
 =0; α = λ . N, N = $\frac{\alpha}{\lambda}$

Sol 16: (C)
$$\frac{\text{Atoms of Sr}}{\text{Atoms of Rb}} = 0.05$$

or
$$\frac{\text{Atomsof}(\text{Sr}+\text{Rb})}{\text{Atomsof}(\text{Rb})} = 1.05$$

so,
$$\frac{\text{Initial number of atoms of Rb}}{\text{Pr esent number of atoms Rb}} = 1.05$$

$$t = \frac{2.303}{\lambda} \log(n_0 / n) = \frac{2.303}{0.693} \times 4.7 \times 10^{10} \log(1.05)$$

 $= 3.28 \times 10^{9}$ year

Sol 17: (A) $\lambda_A N_A = \lambda_B N_B$

(:: rate of disintegration are same)

$$\frac{N_A}{N_B} = \frac{\lambda_B}{\lambda_A} = \frac{2}{1}$$

Sol 18: (B) N = N₀.e<sup>-
$$\lambda$$
t</sup>
When N = parent remaining (p) and
N₀ = Initial parent
= Parent remaining (p) + daughter formed
P = (p + d).e^{- λ t} or In $\frac{(p+d)}{p} = \lambda$.t
t = $\frac{1}{\lambda} ln \left(1 + \frac{d}{p} \right)$
Sol 19: (B) $\lambda = \lambda + \lambda + \lambda = \frac{0.693}{2}$ and $\frac{\lambda_1}{2} = \frac{1}{2}$

Sol 19: (B) $\lambda = \lambda_1 + \lambda_2$; $\lambda = \frac{0.693}{22}$ and $\frac{\lambda_1}{\lambda_2} = \frac{2}{98}$ $\lambda_1 = 0.00063 \text{ year}^{-1}$; $\lambda_2 = 0.03087 \text{ year}^{-1}$

Sol 20: (B) $_{84}Pb^{218} \rightarrow {}_{82}Pb^{219} + {}_{2}He^{4} \rightarrow {}_{83}Bi^{214} + {}_{-1}e^{0}$

Pb²¹⁴ to reach maximum number of nuclei

$$t_{max.} = \frac{1}{\lambda_1 - \lambda_2} ln \frac{\lambda_1}{\lambda_2} = 247.5 \text{ sec}$$

Where, $\lambda_1 = \frac{0.693}{183}; \lambda_2 = \frac{0.693}{161}$

Previous Years' Questions

Sol 1: (C) $_{90}$ Th²³⁴ $\xrightarrow{-\beta} _{91}X^{234} \xrightarrow{-\beta} _{92}Y^{234} \xrightarrow{-\alpha} _{90}Z^{230}$ **Sol 2: (C)** $^{24}_{12}$ Mg+ $\gamma \longrightarrow ^{23}_{11}$ Na+ $^{1}_{1}$ H

Sol 3: (D) Equate mass number and atomic number

Sol 4: (B)

$${}_{92}M^{238} \longrightarrow {}_{y}N^{x} + 2 {}_{2}He^{4}$$

$${}_{y}N^{x} \longrightarrow {}_{B}L^{A} + 2b^{+}$$

$${}_{y}N^{x} = {}_{(92-2\times2)}N^{(238-4\times2)} = {}_{88}N^{230}$$

$${}_{88}N^{230} \xrightarrow{2\beta^{+}} {}_{(88-2)}L^{(230)} = {}_{86}L^{230}$$
Total number of neutrons in ${}_{86}L^{230}$

$$230 - 86 = 144$$

Sol 5: (C) β -particle is emitted in radioactivity by Conversion of neutron to proton

Sol 6: (B) N =
$$\frac{N_0}{64} = \frac{N_0}{2^6}$$
 \therefore n = 6

Thus total time = $2 \times 6 = 12$ hr.

Sol 7: (D) N =
$$\frac{N_0}{2^n}$$
 and n = $\frac{560}{140}$ = 4; N = $\frac{1}{2^4}$ = $\frac{1}{16}g$

Sol 8: (C)
$$k = \frac{0.095}{t_{1/2}}$$

$$\Rightarrow t_{1/2} = \frac{0.693}{k} = \frac{0.693}{0.58} = 1.2 \text{ hr}$$

(D)

$$r = \frac{0.693}{t_{1/2}} \times N_0 = \frac{0.693}{1600 \times 365 \times 24 \times 60 \times 60} \times \frac{6.023 \times 10^{23}}{226}$$

= 3.7 × 10¹⁰ dps
Sol 10: (A) $\frac{N}{N_0} = \left(\frac{1}{2}\right)^{\frac{1}{t_{1/2}}}$; $\frac{N}{200} = \left(\frac{1}{2}\right)^{\frac{24}{4}}$; $\frac{N}{200} = \left(\frac{1}{2}\right)^6$
 $N = \frac{200}{64} = 3.125 \text{ g}$

Sol 11: (A) ${}^{238}_{92}U \xrightarrow{\lambda \alpha Particle}_{\text{emission}} {}^{234}_{90}Th \xrightarrow{2\beta particles}_{\text{emission}} {}^{234}_{92}U$

Sol 12: (C) A basis of for the C-14 dating technique.

Sol 13: (A)
$${}^{A}_{Z}X \longrightarrow {}^{A-1}_{Z}X + {}^{1}_{0}n$$

n =
$$\frac{18}{8}$$
 = 6 half lives
∴ N = $\frac{N_0}{2^n} = \frac{256}{2^6} = 4.0 \text{ g}$

JEE Advanced/Boards

Exercise 1

Sol 1: Energy supplied to α -particle $q \times \upsilon$

$$= 2 \times 1.602 \times 10^{-19} \times 3 \times 10^{5} \text{ J}$$

$$= \frac{2 \times 1.602 \times 10^{-13} \times 3 \times 10^{5}}{1.602 \times 10^{-19}} \,\mathrm{eV} = 6 \times 10^{5} \,\mathrm{eV}$$

The energy given is used up to overpower the penetration of nucleus and imparting energy to C and H atoms, i.e., $1 \times 10^5 \text{ eV} + 5 \times 10^5 \text{ eV} = 6 \times 10^5 \text{ eV}$.

Thus, extra energy given to α -particles is used in imparting velocity to C and H and to overpower the

forces of repulsion. The mass decayed during the course of reaction is responsible for emission γ -rays.

Total mass before reaction

= 4.0026 + 10.0129 = 14. 0155 amu

Total mass after reaction

- = 13.0036 + 1.008 = 14.0116 amu
- ... Mass decay during reaction
 - = 14. 0155 14. 0116 = 0.0039 amu
- ... Total energy given out
- = 0.0039 x 931 MeV = 3.6309 MeV= 3.6309 x 10⁶ eV = 3.6309 × 10⁶ × 1.602 × 10⁻¹⁹ J = 5.816 x 10⁻¹³ J also, E = hv
- 5.816 x 10⁻¹³ = 6.625 × 10⁻³⁴ × υ υ = 8.77 × 10²⁰ Hz and υ = c/ λ ∴ 8.77 x 10²⁰ = (3.0 × 10⁸)/ λ
- $\therefore \lambda = 3.4 \times 10^{-13} \text{ m}$
- Sol 2: ${}^{266}_{88}$ Ra $\longrightarrow {}^{222}_{86}$ Rn + ${}^{4}_{2}$ He $N_0 = 1$ g-atom; $t_{1/2}$ Ra = 1600 year, t = 800 year Now, t = $\frac{2.303}{K} \log \frac{N_0}{N}$ $800 = \frac{2.303 \times 1600}{0.693} \log \frac{1}{N}$ (∵ N = 0.707 g-atom) \therefore Amount of Ra decayed = 1 – 0.707 = 0.293 ... Moles of Rn formed = 0.293 and moles of He formed = 0.293 \therefore PV = nRT : Total pressure of He and Rn is $P = \frac{2 \times 0.293}{5} \times 0.0821 \times 300 = 2.887 \text{ atm}$ \therefore P_{He} = P × mole fraction of He $= 2.887 \times \frac{1}{2} = 1.443$ atm **Sol 3:** $n = \lambda . N_{1}$, $r_{2} = \lambda . N_{2}$ $\therefore \frac{r_1}{r_2} = \frac{N_1}{N_2} = \frac{3.02 \times 10^6}{1.20 \times 10^6} = 2.52$

Also 10 =
$$\frac{2.303}{\lambda} \log \frac{N_0}{N_1}$$
 ... (i)

$$20 = \frac{2.303}{\lambda} \log \frac{N_0}{N_2}$$
... (ii)

By eqs. (ii) – (i)

$$20 - 10 = \frac{2.303}{\lambda} \left[\log \frac{N_0}{N_2} - \log \frac{N_0}{N_1} \right]$$

$$10 = \frac{2.303}{\lambda} \left[\log \frac{N_1}{N_2} \right] = \frac{2.303}{\lambda} \log 2.52$$

$$\therefore \lambda = 0.092 \text{ min}^{-1}$$

$$t_{1/2} = \frac{0.693}{\lambda} = \frac{0.693}{0.092} = 7.50 \text{ min}$$
$$T_{av.} = \frac{1}{\lambda} = \frac{1}{0.092} = 10.87 \text{ min}$$

Sol 4: Let activity of ${}_{x}A_{1}$ and ${}_{x}A_{2}$ be m and n curie respectively at t = 0

Also, \therefore Rate \propto Number of atoms

$$\therefore \text{ For }_{x}A_{1} \text{ decay}$$
$$t = \frac{2.303}{\lambda} \log \frac{N_{0}}{N} = \frac{2.303}{\lambda} \log \frac{r_{0}}{r}$$

$$20 = \frac{2.303 \times 14}{0.693} \log \frac{m}{r_1} \quad \therefore \quad r_1 = 0.3716$$

Similarly, for $_{x}A_{2}$ decay

$$t = \frac{2.303}{\lambda} \log \frac{r_0}{r};$$

$$20 = \frac{2.303 \times 25}{0.693} \log \frac{n}{r_2} \quad \therefore \quad r_2 = 0.5744 \text{ n}$$

Given that activity after 20 day remains $\frac{1}{2}$ of original activity
 $\therefore 0.2716 \text{ m} \pm 0.5744 \text{ n} = \frac{1}{2}$ (ii)

 $\therefore 0.3716 \text{ m} + 0.5744 \text{ n} = -\frac{1}{2} \dots (ii)$

Solving eqs. (i) and (ii) m = 0.3669 curie;

n = 0.6331 curie For ratio of atoms, i.e., $(N_0^{A_1} / N_0^{A_2})$, we can write

$$\frac{r_0^{A_1}}{r_0^{A_2}} = \frac{\lambda^{A_1}}{\lambda^{A_2}} \times \frac{N_0^{A_1}}{N_0^{A_2}} \quad (\because \ r = \lambda.N_0)$$

or
$$\frac{0.3669}{0.6331} = \frac{0.693 \times 25}{14 \times 0.693} \frac{N_0^{A_1}}{N_0^{A_2}}$$
 or $\frac{N_0^{A_1}}{N_0^{A_2}} = 0.3255$

Sol 5: We know, A $\xrightarrow{\lambda_1}$ B $\xrightarrow{\lambda_2}$ C Given, [A]₀ = 1.8 M, λ_1 = 1.8 × 10⁻⁵ s⁻¹ and λ_2 = 1.1 × 10⁻² s⁻¹

Since, $\lambda_1 << \lambda_2$, thus, B will be converted to C at higher rate than A is converted to B. Thus, sequential reaction may therefore, be written as :

$$A \xrightarrow{\lambda_{1}} C$$

$$\therefore [A]_{0} = [A]_{t} + [C]_{t} \qquad \dots (i)$$

For 1 order reaction, rate expression in integrated form gives

$$[A]_t = [A]_0 e^{-\lambda_1 t}$$
 ... (ii)

Thus, by eqs. (i) and (ii).

$$\begin{aligned} [A]_0 &= [A]_0 e^{-\lambda_1 t} + [C]_t \quad \text{or} \quad [C]_t = [A]_0 [1 - e^{-\lambda_1 t}] \\ &= 1.8 \ [1 - e^{-1.8} \times 10^{-5} \times 24 \times 3600] \\ [C]_t &= 1.42 \text{ M} \end{aligned}$$

Sol 6: ${}_{Z}^{m}A \xrightarrow{-\alpha} {}_{Z-2}^{m-4}B \xrightarrow{-\beta} {}_{Z-1}^{m-4}C$ ($t_{1/2})_{A} = 10$ month ($t_{1/2})_{B} = 6$ month

The radioactive equilibrium is attached then, at equilibrium the ratio of atoms of A and B left is :

$$\frac{N_A}{N_B} \!=\! \frac{t_{1/2}A}{t_{1/2}B} \!=\! \frac{10}{6} \!=\! 1.66$$

If half-life of A = 6 month and B is 10 month, then since $t_{1/2}A < t_{1/2}B$ or $\lambda_A > \lambda_B$ and thus no equilibrium will be set.

Note: Radioactive process are first order in nature and any radioactive species completely decays only at infinite time.

Sol 7: Uranium present

 $= \frac{50}{100}g = \frac{0.50}{2.38}g - \text{atom} = 2.10 \times \times 10^{-3} \text{ g-atom}$

Pb formed from uranium decay

$$= \frac{2.425 \times 93}{100 \times 206 \times 100} = 0.109 \times 10^{-3} \text{ g-atom}$$

Thus, N =
$$2.10 \times 10^{-3}$$
 g-atom

$$N_0 = (2.10 + 0.109) \times 10^{-3} \text{ g-atom}$$

Now,
$$t = \frac{2.303}{\lambda} \log_{10} \frac{N_0}{N} = \frac{2.303}{1.52 \times 10^{-10}} \log_{10} \frac{2.209 \times 10^{-3}}{2.10 \times 10^{-3}}$$

 $R = 3.3 \times 10^8$ year

Sol 8: We know,
$$x \xrightarrow{\lambda_x} y \xrightarrow{\lambda_y} z$$

 $t = 0$, $[r_x]_0$, $[r_y]_0$
 $t = 4$, $[r_x]_t$, $[r_y]_t$
 $[r_x]_0 = [r_y]_0$ (Given)
 $\therefore 1_x[N_x]_0 = 1_y[N_y]_0$ or $\frac{[N_x]_0}{[N_y]_0} = \frac{\lambda_y}{\lambda_x}$

Now maximum yield of $y(N_y)t$

at t = 4 hr. is :

$$[N_{y}]_{t} = \frac{[N_{x}]_{0} \cdot \lambda_{x}}{\lambda_{y} - \lambda_{x}} [e^{-\lambda_{x} \cdot t} - e^{-\lambda_{y} \cdot t}] + [N_{y}]_{0} e^{-\lambda_{y} \cdot t}$$
$$= \frac{\lambda_{y} [N_{y}]_{0} \cdot \lambda_{x}}{\lambda_{x} [\lambda_{y} - \lambda_{x}]} [e^{-\lambda_{x} \cdot t} - e^{-\lambda_{y} \cdot t}] + [N_{y}]_{0} e^{-\lambda_{y} \cdot t}$$
$$= \frac{\lambda_{y} [N_{y}]_{0}}{[\lambda_{y} - \lambda_{x}]} [e^{-\lambda_{x} \cdot t} - e^{-\lambda_{y} \cdot t}] + [N_{y}]_{0} e^{-\lambda_{y} \cdot t}$$
$$\therefore \quad \frac{[N_{y}]_{t}}{[N_{y}]_{0}} = \begin{bmatrix}\frac{\lambda_{y}}{\lambda_{y} - \lambda_{x}} \cdot e^{-\lambda_{x} \cdot t} \\ -\frac{\lambda_{y}}{\lambda_{y} - \lambda_{x}} e^{-\lambda_{y} \cdot t} + e^{-\lambda_{y} \cdot t}\end{bmatrix}$$

$$= \begin{bmatrix} \frac{0.693}{2 \times \left[\frac{0.693}{1} - \frac{0.693}{2}\right]} \times e^{\frac{-0.693}{2} \times 4} \\ \frac{0.693}{2 \times \left[\frac{0.693}{1} - \frac{0.693}{2}\right]} \times e^{\frac{-0.693 \times 4}{1}} + e^{\frac{-0.693 \times 4}{1}} \end{bmatrix}$$

$$= 0.25 + 0.06 + 0.06$$
$$\frac{[N_y]_t}{[N_y]_0} = 0.25$$

Sol 9:

$$^{64}_{29}Cu$$
 $\xrightarrow{-\beta^{+}}$
 $^{64}_{28}Ni$ (19%); λ_{1}
 $(19\%); \lambda_{2}$
 $+^{+0}_{-1}$
 $^{64}_{28}Ni$ (43%); λ_{3}

Given,
$$\lambda_{av} = \frac{0.693}{12.8} \text{ hr}^{-1}$$

 $\therefore \lambda_1 + \lambda_2 + \lambda_3 = \lambda_{av} = \frac{0.693}{12.8}$

- $\lambda_1 + \lambda_2 + \lambda_3 = 5.41 \times 10^{-2} \text{ hr}^{-1}$ (i) Also for parallel path decay (ii) λ_1 = Fractional yield of ${}^{64}_{30}$ Zn $\times \lambda_{av}$ λ_2 = Fraction yield of ${}^{64}_{28}$ Ni $\times \lambda_{av}$ λ_3 = Fractional yied of $^{64}_{28}$ Ni $\times \lambda_{av}$ $\frac{\lambda_1}{\lambda_2} = \frac{28}{19}$ and $\frac{\lambda_1}{\lambda_2} = \frac{38}{43}$ From eqs. (i), (v) and (vi); $\lambda_1 = 2.056 \times 10^{-2}$ $\lambda_2 = 1.028 \times 10^{-2}; \lambda_3 = 2.327 \times 10^{-2} \text{ hr}^{-1}$ \therefore t_{1/2} for β^- -emission = $\frac{0.693}{2.056 \times 10^{-2}}$ = 33.70 hr $t_{1/2}$ for β^+ -emission = $\frac{0.693}{1.028 \times 10^{-2}} = 67.41$ hr $t_{1/2}$ for electron capture = $\frac{0.693}{2.327 \times 10^{-2}}$ = 29.78 hr Sol 10: TF = T⁺ + F⁻ 1 0 0 $(1-\alpha) \quad \alpha \quad \alpha$ Given, pT = 1.7 (like pH) $[T^+] = 0.02 = Ca$
- Sol 10: TF \implies T⁺ + F⁻ 1 0 0 (1- α) α α Given, pT = 1.7 (like pH) [T⁺] = 0.02 = Ca Since $\Delta T = 0 - (-0.372) = 0.372$ for solution of TF $\Delta T_f = K_f \times (1 + \alpha) \times \text{molality} = K_f(1 + \alpha) \times C$ (: Molality = molarity for dilute solution) $\therefore \Delta T_f = K_f(C + C\alpha)$ 0.372 = 1.86(C + 0.02) $\therefore C = 0.2 - 0.02 = 0.18 \text{ M}$ Thus, $K_a = \frac{[T^+][F^-]}{[TF]} = \frac{0.02 \times 0.02}{(0.18 - 0.02)} = 2.5 \times 10^{-3}$ Also, 0.18 mole of TF contain 0.18 mole of T (including
- T^+) per litre. 0.18 \times 600

Thus, mole of TF in 600 mL = $\frac{0.18 \times 600}{1000}$ = 0.108

T has half-life = 12. 4 year; $N_0 = 0.108$

$$\therefore \text{ Amount left in 24. 8 year} = \frac{N_0}{2} = 0.054$$

or 0.05 mole of tritium undergoes β -eission. Since, one tritium atom emits one β -particle.

Number of β -emitted = [0.108 - 0.054] × 6.023 × 10²³

.... (i) \therefore Total charge emitted $= \frac{3.25 \times 10^{22} \times 1.602 \times 10^{-19}}{96500}$ Faraday = 0.054 faraday (iii) Sol 11: $\lambda_{pb} = \frac{0.693}{10.6 \times 60} = 1.0896 \times 10^{-3} \text{ min}^{-1}$ (iv) $\lambda_{bi} = \frac{0.693}{60.5} = 11.45 \times 10^{-3} \text{ min}^{-1}$ (v) $\lambda_{bi} = \frac{2.303}{\lambda_{bi} - \lambda_{pb}} - \log \frac{\lambda_{bi}}{\lambda_{pb}}$ $= \frac{2.303}{(11.45 \times 10^{-3} - 1.0896 \times 10^{-3})} \times \log \frac{11.45 \times 10^{3}}{1.0896 \times 10^{3}}$ = 227.1 minSol 12: We know, that, $t = \frac{2.303}{\lambda} \log \frac{N_{0}}{N}$ $N_{0} = 100, N = (100 - 99.9) = 0.1$ So, Time required for 99.9% decay, $t = \frac{2.303}{\lambda} \log \frac{100}{0.1} = \frac{2.303}{\lambda} \times 3$ Half life period $= \frac{0.693}{\lambda}$ So, $\frac{\text{Time required for 99.9\% decay}}{\text{Half life period}}$

$$= \frac{2.303 \times 3}{\lambda} \times \frac{\lambda}{0.693} \simeq 10$$

Sol 13: 27 MeV = $27 \times 10^{6} \times 1.6 \times 10^{-19} = 43.2 \times 10^{-13}$ J Energy radiated by the sun per day = $4 \times 10^{26} \times 3600 \times 24$ J day⁻¹ = 34.56×10^{30} J day⁻¹ 43.2×10^{-13} J of energy is obtained from = 4 amu of H = $4 \times 1.66 \times 10^{-24}$ g of H 34.56×10^{30} J of energy is obtained from

$$= \frac{4 \times 1.66 \times 10^{-24}}{43.2 \times 10^{-13}} \times 34.56 \times 10^{30} = 5.31 \times 10^{19} \text{ g}$$

Exercise 2

Single Correct Choice Type

Sol.1: (B)

$$\lambda t = \ln\left(\frac{A_0}{A}\right) = \frac{0.693}{30} \times 90 = \ln\frac{A_0}{A} = A_0 = A \times 8$$

:
$$N_0 = \frac{A_0}{\lambda} = \frac{800}{0.693} \times 30 = 3.46 \times 10^4 \text{ atoms}$$

Sol 2: (A) At time
$$\begin{array}{c} X \\ n_0 - x \end{array} \xrightarrow{} \begin{array}{c} Y \\ x \end{array}$$
;

$$\frac{n_0 - x}{x} = \frac{1}{7}$$
; $n_0 = \frac{8x}{7}$;

$$\lambda = \frac{0.693}{6.93 \times 10^9} \ \text{P} \ 10^{10} \ \text{years}^{-1}$$

$$t = \frac{2.303}{\lambda} \log \left(\frac{W_0}{W_0 - x} \right)$$
$$t = \frac{2.303}{10^{-10}} \log(8) = 2.097 \times 10^{10} \text{ years}$$

Sol 3: (C)
$$\lambda_{\text{net}}$$
 or $\lambda = \lambda_1 + 2\lambda_2 = 1.8 \times 10^{-3} + 2 \times 10^{-3}$
= 2 × 10⁻²

Average life (T_{av}) = $\frac{1}{\lambda} = \frac{1}{2 \times 10^{-2}} = 50$ sec

Sol 4: (C) $_{83}Bi^{211} \rightarrow _{81}TI^{207} + _{2}He^4$; total time = n × half-life

Moles of substance left after n halves

$$=\frac{\text{initialmoles}}{2^{n}}=\frac{2}{2^{4}}=0.125$$

Mole of He produced = 2 - 0.125 = 1.875

Pressure developed due to He

$$= \frac{1.875 \times 0.0821 \times 300}{100} = 0.4618 \text{ atm}$$

Sol 5: (D) Let initial activities of A and B are A_0 and B_0

(: after 2 half-lives of activity of A will remain
$$\frac{A_0}{4}$$
)
A₀ + B₀ = 8000 and
also $\frac{A_0}{4}$ + B₀ = 3500

(we can assume that activity of B remains constant due to larger half-life)

So
$$\frac{3A_0}{4} = 4500$$

A₀ = 6000; B₀ = 2000

$$\frac{A_0}{B_0} = \frac{6000}{2000} = \frac{3}{1}$$

Sol 6: (A) No change in activity of sample during establishment of circulatory equilibrium.

Let volume of blood is V mL, so total vol. = (V + 1) mL after injection of sample.

2 mL sample has activity of 10 dpm, so (V + 1) mL sample has activity of $\frac{10}{2} \times (V+1)$

Since rate is constant so $\frac{10}{2} \times (V+1) = 1000$; V = 199 mL

Sol 7: (C)
$$\frac{A_{0(x)}}{A_{0(Y)}} = \frac{4}{1}$$
; $\frac{A_x}{A_y} = 1$,
 $\lambda_y - \lambda_x = \frac{1}{t} \ln \left(\frac{(A_0)_y}{(A_0)_x} \times \frac{A_x}{A_y} \right)$
 $(\lambda_y - \lambda_x)t = \ln \left(\frac{1}{4} \right)$; $(t_{1/2})y = 30$ min.

Sol 8: (A) Corrected C¹⁴ count : Let initial C¹⁴ count = A₀; A₀ + A₀/10 = 15. 4; A₀ = 14 t = $\frac{1}{\lambda} \log \frac{14}{7} = 5.770 \times 10^3$ years; t = $\frac{\ln 2}{\lambda} = t_{1/2}$; t = 5770 years

Multiple Correct Choice Type

Sol 9: (C) A loss of β -particles results in the production of isobars

Sol 10: (A, C, D)

(A) In the reaction $_{_{92}}U^{_{235}} + _{_0}n^1 \longrightarrow _{_{56}}Ba^{_{140}} + 2_{_0}n^1 + x$, produced x is $_{_{36}}Kr^{_{94}}$

(C) Very large amounts of energy is produced during nuclear fission and nuclear fusion

(D) In a fission reaction, a loss in mass occurs releasing a vast amount of energy

Sol 11: (A, C, D)

(A) SI unit of radioactivity is Becquerel (Bq)

(C) $_{3}\text{Li}^{7} + _{1}\text{H}^{1} \longrightarrow _{2}\text{He}^{4}$ is (P, α) type reaction

(D) The half-life of a particular radioactive isotope is a characteristic constant of that isotope

Sol 12: (A, B, C)

(A) On bombarding $_7N^{14}$ nuclei with α -particle, the nuclei of the product formed after release of proton would be $_8O^{17}$

(B) Decay constant does not depend upon temperature

(C) Nuclide and its decay product after $\alpha\text{-emission}$ are called isodiapheres

Sol 13: (B, C) In the decay process

 $A \xrightarrow{-\alpha} B \xrightarrow{-\beta} C \xrightarrow{-B} D$

A and D are isotopes

B, C and D are isobars

Comprehension Type

Paragraph 1

Sol 14: (C)
$$\lambda = \frac{0.693}{t_{1/2}}$$

 $t = \frac{2.303}{\lambda} log \left(\frac{N_0}{N}\right) = 5 \times 10^5$ years

Sol 15: (A) $\frac{N}{N_0} = \left(\frac{1}{x}\right)^n$; where n = number of halves; $\frac{N}{N_0} = \frac{1}{10} = \left(\frac{1}{x}\right)^n = n = 4$

Total time = n ×
$$t_{1/2}$$
 = 4740 = 4 × $t_{1/2}$

 $t_{1/2} = 1185$ years

Sol 16: (B) $-\frac{dN}{dt} = \lambda \times N$ $\Rightarrow \frac{0.693}{t_{1/2}} \times n \times N_A - \frac{dN}{dt}$ $-\frac{dN}{dt} = \frac{0.693}{24,000 \times 365 \times 24 \times 60 \times 60 \times 1 \times 6.02} \times 10^{23} \text{ dps}$

Paragraph 2

Sol 17: (B) r = R₀A^{1/3}

:. Volume of nucleus =
$$(4/3)\pi r^3 = \frac{4}{3}\pi (1.5 \times 10^{-15})^3 \text{Am}^3$$

Density d =
$$\frac{m}{V} = \frac{A \times 1.66 \times 10^{-27} \text{kg}}{\frac{4}{3} \pi (1.5 \times 10^{-15})^3 \text{A}} = 1.17 \times 10^{17} \text{ kg/m}^3$$

Sol 18: (B)
$$d_c = \frac{Mass}{Volume} = \frac{12 \times 1.66 \times 10^{-27}}{\frac{4}{3} \times 3.14 \times (3 \times 10^{-15})^3}$$

= 1.76 × 10¹⁷ kg/m³
 $d_{H_2O} = 1000 \text{ kg/m}^3$
 $\frac{d_c}{d_{H_2O}} = \frac{1.76 \times 10^{17}}{1,000} = 1.76 \times 10^{14}$

Match the Columns

Sol 19: $A \rightarrow s$; $B \rightarrow p$; $C \rightarrow q$; $D \rightarrow r$ (A) Isotones- ${}_{18}Ar^{39}$ and ${}_{19}K^{40}$ (B) Isobars - ${}_{91}Pa^{234}$ and ${}_{90}Th^{234}$ (C) Isotopes- ${}_{6}C^{12}$ and ${}_{6}C^{14}$ (D) Isodiapheres - ${}_{19}K^{39}$ and ${}_{9}F^{19}$

Sol 20: $A \rightarrow p, r; B \rightarrow s; C \rightarrow q; D \rightarrow r$

(A) α-emission no.- Change in mass, Atomic no.
(B) β-emission- Atomic no. increases
(C) γ-emission decreases - No change in atomic no & mass no
(D) β⁺ (Positron)- Atomic no

Previous Years' Questions

Sol 1: (B) The nuclear reaction $_{92}U^{238} \rightarrow _{2}He^{4}(\alpha) + _{90}Th^{234}$

Sol 2: (A) Isotopes have same atomic numbers (Z) but different mass number (A). Therefore, ${}_{32}Ge^{76}$ and ${}_{32}Ge^{77}$ are isotopes.

Sol 3: (D) Both α -rays and β -rays are deflected by magnetic field.

Sol 4: (B) $_{13}Al^{29}$ is neutron rich isotope, will decay by β -emission converting some of its neutron into proton as $_{0}n^{1} \rightarrow _{-1}b^{0} + _{1}H^{1}$

Sol 5: (B) The balanced nuclear reaction is

$$2_0 n^1 + {}_{92} U^{235} \rightarrow {}_{54} Xe^{139} + {}_{38} Sr^{94}$$

Sol 6: (A) In stable isotope of Na, there are 11 protons and 12 neutrons. In the given radioactive isotope of sodium (N^{24}), there are 13 neutrons, one neutron more than that required for stability. A neutron rich isotope

always decay by β -emission as $_{0}n^{1} \rightarrow _{-1}b^{0} + _{1}H^{1}$

Sol 7: (C) The required nuclear reaction is

 $_{_{11}}Na^{_{23}} \rightarrow _{_{+1}}e^0 + {}_{_{10}}Ne^{_{23}}$

Sol 8: (A, D) If sum of mass number of product nuclides in less than the same of parent nuclides, neutron emission will occur. In both (A) and (D), sum of mass numbers of product nuclides is one unit less than the same for parent nuclides, neutron emission will balance the mass numbers.

Sol 9: (A, C, D) In the following nuclear reaction, there occur decrease in atomic number (Z):

 $_{Z}X^{A} \rightarrow _{_{2}}He^{4} + _{_{Z-2}}Y^{A-4} \dots \alpha \text{-emission}$ $_{Z}X^{A} \rightarrow _{_{+1}}e^{0} + _{_{Z-1}}Y^{A} \dots \text{positron emission}$ $_{Z}X^{A} + _{_{-1}}e^{0} \rightarrow _{_{Z-1}}Y^{A} \dots \text{electrons capture}$

In beta emission, increase in atomic number is observed:

 $_{Z}X^{A} \rightarrow _{_{-1}}e^{_{0}} + _{_{Z+1}}Y^{A}$ β -emission

Sol.10: (B) Up to atomic number 20, stable nuclei possess neutron to proton ratio (n/p) = 1

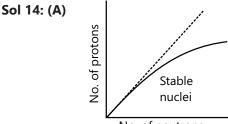
$$\frac{n}{p}(_{13}\text{Al}^{30}) = \frac{17}{13} = 1.3 > 1$$
 , unstable, b-emitters
$$\frac{n}{p}(_{20}\text{Ca}^{40}) = \frac{20}{20} = 1$$
 , stable

Also, nuclei with both neutrons and protons are usually unstable but it does not explain the assertion appropriately.

Sol 11: (3)
$${}_{92}U^{235} \rightarrow {}_{54}Xe^{142} + {}_{38}Sr^{90} + 3{}_{0}n^{1}$$

Sol 12: ${}_{92}X^{234} \rightarrow 7{}_{2}He^{4} + 6{}_{-1}e^{0} + {}_{84}Y^{206}$
Y is ${}_{84}Po^{206}$
Sol 13: ${}_{92}U^{238} \rightarrow {}_{82}Pb^{214} + 6{}_{2}He^{4} + 2{}_{-1}e$

 \Rightarrow Number of $(\alpha + \beta) = 6 + 2 = 8$



No. of neutrons

If the curve does not bend down towards the x axis then the proton-proton repulsion would overcome the attractive force of proton and neutron. Therefore, the curve bends down.

Sol 15: (B)
$$\overline{A} = \frac{\sum A_i x_i}{\sum x_i}$$

 \overline{A} = 54 × 0.05 + 56 × 0.90 + 57 × 0.05 (where \overline{A} is atomic mass of Fe)

Sol 16: (A)
$${}^{27}_{13}AI + {}_{2}\alpha^{4} \rightarrow {}^{30}_{14}Si + {}_{1}p^{1}(X)$$

 ${}^{27}_{13}AI + {}_{2}\alpha^{4} \rightarrow {}^{30}_{15}Si + {}_{0}n^{1}(Y)$
 ${}^{30}_{15}P \rightarrow {}^{30}_{14}Si + {}_{+1}\beta^{0}(Z)$

Sol 17: (8) ${}^{63}_{29}Cu + {}_{1}H^{1} \rightarrow 6_{0}n^{1} + {}^{4}_{2}He + 2_{1}H^{1} + {}^{A}_{Z}X$ Mass number: 63 + 1 = 1 × 6 + 4 + 1 × 2 + A A = 64 - 12 = 52 Atomic number: 29 + 1 = 6 × 0 + 2 + 2 × 1 + Z Z = 30-4 = 26 ${}^{A}_{Z}X = {}^{52}_{26}Fe$

Hence X is in group '8' in the periodic table.

Sol 18: (A, B) ${}_{4}^{9}Be + \gamma \longrightarrow {}_{4}^{8}Be + {}_{0}^{1}n$ ${}_{4}^{9}Be + {}_{1}^{1}P \longrightarrow {}_{4}^{8}Be + {}_{1}^{2}H$

Hence (A) and (B) are correct

Sol 19: In conversion of $^{238}_{92}$ U to $^{206}_{82}$ Pb,

 8α - particles and 6β particles are ejected.

The number of gaseous moles initially = 1 mol

The number of gaseous moles finally = 1 + 8 mol; (1 mol from air and 8 mol of $_2\text{He}^4$)

So the ratio = 9/1 = 9

Solutions

JEE Main/Boards

Exercise 1

Environmental Chemistry

Sol 1: Primary pollutants are those which after their formation remain as such, e.g., NO. Secondary pollutants are those which are formed as a result of reaction between primary pollutants, e.g., PAN (peroxyacylnitrate).

Sol 2: Ozone layer is formed in the stratosphere at an altitude of about 25-30 km from earth's surface. At this altitude, the force of gravitation is negligible.

Sol 3: The term "Environment" literally means "surrounding". It comprises of the following four major components:

(1) Atmosphere	(2) Hydrosphere
(3) Lithosphere and	(4) Biosphere

(1) **Atmosphere:** Atmosphere is a cover of gases that extends to a height of about 1600 km above the surface of the earth and protects the life on the life on the earth from the harmful radiations (cosmic rays) coming from the sun or the outer space.

(2) Hydrosphere: It forms that part of the environment which contains water in the form of sea, oceans, rivers, lakes, ponds, etc. About 75 percent of the earth's surface is covered by hydrosphere. Most of it is in the oceans and contains about 3.5% of the dissolved salt. Fresh water is present in lakes or rivers or ponds which flows into them from rain or melting of snow, etc.

(3) Lithosphere: It is the solid component of the earth consisting of soil, rocks, mountains etc. The outermost (8-40 km) thick solid part of the earth is called the crust. The uppermost part of the earth's crust contains weathered rocks as well as organic matter and is called soll. This is the most important part of lithosphere because we grow plants on this part. It is also a store-house of minerals.

(4) **Biosphere:** It is that part of the lithosphere, hydrosphere and atmosphere where living organisms interact with these parts and thus live together. For example, green plants during photosynthesis give out oxygen which is added into the atmosphere, animals inhale oxygen and give out carbon dioxide which is used by plants for photosynthesis.

Sol 4: Structure of Regions of the Atmosphere: The atmosphere may be considered to be divided mainly into four regions above the surface of the earth. These regions are defined by the temperature variation with height in addition to the decrease in density and chemical composition. The names of these regions, the altitudes at which they exist, their temperature range and their chemical composition are given in Table 14.1 below:

Region	Altitude from earth's surface	Temperature Range	Gases/Species present
(i) Troposphere	0-11 km	Decreases from 15 to -56°C	N ₂ ,O ₂ ,CO ₂ ,H ₂ O vapor
(ii) Stratosphere	11-50 km	Increases from – 56 to –2°C	$N_{2'}O_{2'}O_{3'}$ O-atoms
(iii) Mesosphere	50-85 km	Decreases from -2 to -92°C	N ₂ ,O2, O ⁺ ₂ , NO ⁺
(iv) Thermosphere	85-500 km	Increases from –92 to 1200°C	O ₂ ⁺ , O ⁺ , NO ⁺ , e ⁻

Troposphere: is the most important region of the atmosphere because it is the domain of all living organisms including animals and plants. This is the region which is greatly affected by air pollution. Further, this is the region

which contains water vapor which is essential for living organisms (Above 10 km, water is present as ice crystals). 80% of the mass of the atmosphere is in this region. The temperature of this region decreases with altitude and is minimum at about 11 km. This point is called **tropopause**. In the next region, namely **stratosphere**, the temperature begins to increase. Thus, tropopause is the point of **temperature inversion**. The ozone present in the stratosphere absorbs the harmful ultraviolet radiation coming from the sun and thus acts as an umbrella for the ultraviolet radiation for the living organisms on the earth. Due to presence of ozone layer, this region is also called **ozonosphere**. The rise in temperature is due to absorption of ultraviolet rays which is converted into heat. **Mesosphere** and **thermosphere** (collectively called lonosphere) contain gases in the ionized form. These ions reflect back the radiowaves to the earth. This forms the basis of wireless communication.

These regions may be represented diagrammatically as shown in figure.

Exosphere	
Thermosphere → <u>300 km</u>	
Mesosphere 50 km	
Stratosphere 40 km	
Troposphere <u>10 km</u>	
TB T	A PERSON AND A PER

There is one region above the thermosphere. It is called **exosphere** and is considered to the highest region of the atmosphere. It lies in the range of 500-1600 km and contains mainly atomic and ionic oxygen, hydrogen and helium. Beyond exosphere is the unbounded area called interstellar space.

Sol 5: No, temperature does not decrease continuously. From 0-11 km (called troposphere), temperature decreases. From 11-50 km (called stratosphere), temperature increases. From 50-85 km (called mesosphere), temperature again decreases and finally from 85-100 km (called thermosphere), temperature again increases.

Sol 6: Air pollution is defined as the addition of undesirable materials into the atmosphere either due to natural phenomena or due to human activity on the earth which adversely affect the quality of the air and hence affects the life on the earth.

The main sources of air pollution may be classified into two categories as follows:

- (a) Natural sources. A few examples of the natural sources of pollution are as under:
 - (i) Volcanic eruptions emitting poisonous gases like CO, H₂S, SO₂, etc.
 - (ii) Forest fires and coal-refuse fires.
 - (iii) Vegetation decay
 - (iv) Pollen grains of flowers.
- (b) Man-made sources, i.e., sources due to human activity. A few examples may be cited as follows:
 - (i) **Burning of fossil fuels** (wood, coal, etc.) which produce some poisonous gases as by-products such as CO, SO₂, oxides of nitrogen (NO_x), CH_a, etc.
 - (ii) Combustion of gasoline in the automobiles, e.g., cars, scooters, buses, trucks, etc. They emit out poisonous gases like CO, oxides of nitrogen and unburnt hydrocarbons in addition to the particles of lead.

- (iii) **Increases in population:** This is one of the major causes of pollution. More the population, more are the needs, greater are the unnatural methods adopted which disturb the balance or equilibrium of the atmosphere.
- (iv) **Deforestation:** Man has been cutting trees indiscriminately to meet his needs. This has resulted in increase in the percentage of CO_2 and decrease in the percentage of oxygen in the air (because plants take up CO_2 for photosynthesis and give out O_2)
- (v) Fast industrialization: In the last few years, the number of industries in different parts of the world and their production has increased manifold. These include paper mills, sugar mills, rubber and plastic industries, metallurgical industries using smelters, leather industries, petroleum refineries, refrigeration, mining, etc. The smoke coming out of these industries contains not only carbon particles but a number of poisonous gases like CO, CO₂, SO₂, H₂S, NO, NO₂. etc. These industries are responsible for about 20% of the total air pollution.
- (vi) Agricultural activities: The pesticides added to the soil or the sprays done over the crops are carried by the wind to different parts of the town where they give a feel smell and affect the health of animals and human beings.
- (vii) Wars: The nuclear weapons used during wars emit out radiations which adversely affect the health and prove to be fatal.

Sol 7: The five major pollutants present in the troposphere are:

- (1) Carbon monoxide (CO)
- (2) Hydrocarbons, $(C_x H_y)$
- (3) Oxides of nitrogen (NO_x)
- (4) Oxides of sulphur (SO_x)
- (5) Particulates.

Sol.8: The **non-viable** particulates are formed as a result of the disintegration of large size materials or by condensation of small size particles or droplets. The atmosphere contains four types of non-viable particulates. These are mist, smoke, fumes and dust.

Mists are produced from the particles of the spray liquids, e.g., from herbicides and insecticides and the condensation of the vapors in the air.

Smoke consists of small soot particles produced as a result of the combustion of organic matter, e.g., oil, tobacco, carbon smoke. etc.

Fumes are the vapors of certain materials present in the air, e.g., metallurgical fumes (fumes of metals) and alkali fumes.

Dust denotes fine particles produced during certain industrial processes, e.g., crushing grinding. It consists of limestone particles, sand, pulverized coal, cement, fly ash, silicon dust, etc.

Sol.9: Freon (chlorofluorocarbons) has a very long life. They stay in the atmosphere for years and ultimately reach the upper layer where they undergo photochemical reaction with ozone. Thus, ozone layer is destroyed producing an ozone hole through which ultraviolet radiation from the sun can pass through and affect life on earth.

Sol 10: Photochemical smog or Los Angeles smog: This type of smog was first observe in Los Angeles in 1950 and hence is named as "Los Angeles smog". It is formed when the air contains NO₂ and hydrocarbons and the mixture is exposed to sunlight. As the reaction takes place in the presence of sunlight to form the smog, it is called photochemical smog. Further, as strong sunlight is needed, this type of smog is formed in the months of summer during the day time when NO₂ and hydrocarbons are present in very large amounts due to heavy vehicular traffic.

Formation of photochemical smog: The mechanism of the formation of photochemical smog may be explained as follows:

In the presence of sunlight, NO₂ undergoes photolysis to form NO and atomic oxygen. Atomic oxygen then combines with the molecular oxygen in the presence of some molecule M (which acts as a source of transfer of energy) to form ozone, O₃. The ozone thus formed reacts with NO to regenerate NO₂ and O₂. Thus, NO₂ cycle is completed.

The reactions taking place may be represented as follows:

$$NO_{2} \xrightarrow{\mathbf{M}} NO + O$$

$$O + O_{2} \longrightarrow O_{3}$$

$$O_{3} + NO \longrightarrow NO_{2} + O_{2}$$

Thus, NO and O_3 produced are used up and no extra NO₂ is added into the atmosphere. But the trouble arises if hydrocarbons are also present in the atmosphere. These hydrocarbons combine with the oxygen atom produced by the photolysis of NO₂ to form highly reactive intermediates called free radicals (which are reactive species containing unpaired electrons) which may be represented by the general formula RCO*. (dot indicates an unpaired electron). These free radicals initiate a variety of reactions, some of which may be as follows:

$$RCO^{+} + O_{2} \longrightarrow RCO_{3}^{\bullet}$$

$$RCO_{3}^{\bullet} + Hydrocarbons \longrightarrow RCHO R_{2}C = O$$

$$RCO_{3}^{\bullet} + NO \longrightarrow RCO_{2} + NO_{2}$$

$$RCO_{3}^{\bullet} + O_{2} \longrightarrow O_{3} + RCO_{2}$$

$$RCO_{3}^{\bullet} + NO_{2} \longrightarrow RCO_{3}NO_{2}$$

$$Peroxyacylnitrates (PAN)$$

As a result, concentration of ozone, peroxyacylnitrates (PAN) and aldehydes (RCHO) and ketones (R₂CO) builds up in the atmosphere

As this type of smog contains O_3 and NO_2 , it is oxidizing in character.

Harmful effects of photochemical smog:

(i) All these compounds (particularly ozone and PAN) produce irritation in the eyes and also in the respiratory system.

(ii) They also damage many materials such as metals, stones, building materials, etc.

(iii) Ozone is particularly destructive to rubber (in which cracks are developed).

(iv) It is also harmful to fabrics, crops and ornamental plants.

(v) NO_2 present gives a brown colour to the photochemical smog which reduces visibility. Airplane pilots are familiar with this type of fog hanging over the cities.

The word "smog" is a misnomer here because photochemical smog contains neither smoke nor fog. It is a mixture of a number of irritation-causing compounds like NO_2 , O_3 , PAN, aldehydes, ketones, hydrocarbons and CO.

Control of Photochemical Smog: The formation of photochemical smog can be controlled or suppressed by adopting the following methods.

(i) By fitting efficient catalytic converters in the automobiles so that the emission of nitrogen oxides and hydrocarbons by these automobiles into the atmosphere can be prevented.

(ii) By spraying certain compounds into the atmosphere which generate free radicals that readily combine with the free radicals that initiate the reactions forming toxic compounds of the photochemical smog.

(iii) Certain plants such as Pinus, Juniparus, Pyrus, Vitis etc. can metabolize oxides of nitrogen. Hence, their plantation could be helpful.

Exercise 2

Sol 1: (B) Troposphere is the coldest region of the earth's atmosphere.

Sol 2: (D) PAN is a secondary pollutant.

Sol 3: (B) All are primary pollutants except H2SO4

Sol 4: (A) The most abundant hydrocarbon pollutant is Methane.

Sol 5: (C) The size of particulates of H2SO4 fog lies in the range 500-1000 nm

Sol 6: (D) The aromatic compounds present as particulates are polycyclic hydrocarbons.

Sol 7: (C) 'White lung cancer' is caused by Textile.

(A) Asbestos	(B) Silica
(C) Textile	(D) Paper

Sol 8: (B) Ozone layer is present in stratosphere

Sol 9 : (C) Depletion of ozone layer causes Skin cancer

Sol 10 (D) Freons are responsible for depletion of the ozone layer in the upper strata of the atmosphere?

Sol 11 : (C) London smog is found in winter during morning time.

Sol 12 : (B) Photochemical smog is formed in summer during day time

Sol 13: (D) Photochemical smog causes irritation in eyes

Sol 14: (C) The smog is essentially caused by the presence of Oxides of sulphur and nitrogen.

Sol 15 : (C) Conceptual fact

Previous Years' Questions

Sol 1: (D) The rain water after thunderstorm contains dissolved acid and therefore the pH is less than rain water without thunderstorm.

Sol 2: (**C**) Smog is Smoke + Fog. Smog contains mainly and.

Sol 3: (C) Ozone layer does not allow ultraviolet radiation from sun to reach earth.

Sol 4: (A) It is called MIC gas

Sol 5: (A) N₂ has triple bond and O₂ has double bond.

Sol 6: (D) DDT – non–biodegradable pollutant.