Solved Examples

JEE Main/Boards

Example 1: The half-life period of a first-order reaction is 30 min. Calulate the specific reaction rate of the reaction. What fraction of the reactant remains after 70 min?

Sol: $k_1 = \dfrac{0.6932}{t_{\frac{1}{2}}} = \dfrac{0.6932}{30} = 0.0231$ min^{-1}.

Let the reaction be $\quad$ A $\rightarrow \quad$ Product

Initial concentration $\quad$ a

Concentration after $\quad$ (a – x) $\quad$ x

70 min

$\therefore$ Fraction of the reaction remained unreacted

$= \dfrac{(a-x)}{a}$ Now, $k_1 = \dfrac{2.303}{t} \log \dfrac{a}{a-x}$ or 0.0231

$= \dfrac{2.303}{70} \log \dfrac{a}{a-x}$

$\log \dfrac{a}{a-x} = \dfrac{0.0231 \times 70}{2.303} = 0.7021$

Taking antilog, we get $\dfrac{a}{a-x} = 5.036$

$\therefore \dfrac{a-x}{a} = \dfrac{1}{5.036} \approx 0.2$

Example 2: For the reaction 2NO + $Cl_2 \rightarrow$ 2NOCl, when the concentration of both reactants is doubled the rate increased by a factor of 8, but when only the concentration of Cl_2 concentration is doubled, the rate doubles. What is the order of the reaction with respect to NO and Cl_2?

Sol: Rate = k [NO]^m [Cl_2]^n

Let the concentrations of NO and Cl_2 be x and y, respectively.

R_1 = kx^m y^n and, R_2 = k (2x)^m (2y)^n

$\therefore \dfrac{R_2}{R_1} = 2^{m+n} = 8 = 2^3$. (given)

$\therefore$ m + n = 3 Again, R_3 = k(x)^m (2y)^n

= k x^{m}y^n. 2^n. $\therefore \dfrac{R_3}{R_1} = 2^n = 2 \quad$ (given)

$\therefore$ n = 1; m = 3 – 1 = 2.

Example 3: In a reaction $2N_2O_5 \rightarrow 4NO_2 + O_2$, the rate can be expressed as

(i) $-\dfrac{d[N_2O_5]}{dt} = k_1[N_2O_5]$

(ii) $\dfrac{d[NO_2]}{dt} = k_2[N_2O_5]$

(iii) $\dfrac{d[O_2]}{dt} = k_3[N_2O_5]$

How are k_1, k_2 and k_3 related?

Sol: The rate law reaction is rate =

$-\dfrac{1}{2}\dfrac{d[N_2O_5]}{dt} = \dfrac{1}{4}\dfrac{d[NO_2]}{dt} = \dfrac{d[O_2]}{dt} = k\left[N_2O_5\right]$

$\therefore -\dfrac{d[N_2O_5]}{dt} = 2k[N_2O_5] = k_1[N_2O_5]$

$\dfrac{d[NO_2]}{dt} = 4k[N_2O_5] = k_2[N_2O_5]$

$\dfrac{d[O_2]}{dt} = k [N_2O_5] = k_3[N_2O_5]$

$\therefore \begin{cases} k_1 = 2k \\ k_2 = 4k \\ k_3 = k \end{cases}$ or $k = \dfrac{k_1}{2} = \dfrac{k_2}{4} = k$

or $2k_1 = k_2 = 4k_3$.

Example 4: The reaction $2N_2O_5 \rightarrow 4NO_2 + O_2$ forms NO_2 at the rate of 0.0072 mol L^{-1}s^{-1} after a certain time.

(a) What is the rate of change of [O_2] at this time?

(b) What is the rate of change of [N_2O_5] at this time?

(c) What is the rate of reaction at this time ?

Sol: The rate of the reaction is expressed as

rate $= -\dfrac{1}{2}\dfrac{d[N_2O_5]}{dt} = +\dfrac{1}{4}\dfrac{d[NO_2]}{dt} = +\dfrac{d[O_2]}{dt}$

and given that

$\dfrac{d[NO_2]}{dt} = 0.0072$ moIL^{-1}s^{-1}.

(a) Rate of appearance of

$O_2 = \dfrac{1}{4}$ × rate of appearance of NO_2

$$\frac{d[O_2]}{dt} = \frac{1}{4} \times \frac{d[NO_2]}{dt} = \frac{1}{4} \times 0.0072 = 0.0018 \text{ mole/L/s.}$$

(b) Rate of disappearance of N_2O_5 = $\frac{1}{2} \times$ rate of appearance of NO_2

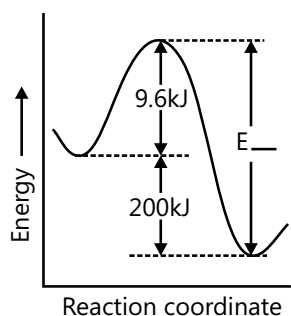$$-\frac{d[N_2O_5]}{dt} = \frac{1}{2} \times \frac{d[NO_2]}{dt} = \frac{1}{2} \times 0.0072$$

$$= -0.0036 \text{ mole /L/s.}$$

(c) Rate of reaction = $\frac{1}{4} \times \frac{d[NO_2]}{dt}$

$$= \frac{1}{4} \times 0.0072 = 0.0018 \text{ (mole/L)s}^{-1}.$$

Example 5: The activation energy for the reaction O_3 (g) + NO (g) $\rightarrow$ NO_2 (g) + O_2 (g) is 9.6 kJ/mol. Prepare an activation energy plot it $\Delta H°$ for this reaction is -200 kJ/mole. What is the energy of activation for the reverse reaction?

**Sol:** Energy of activation for reverse reaction
= 9.6 + 200 kJ = 209.6 kJ.

Example 6: 1 mL of methyl acetate was added to 20 mL of 0.5 N HCl and 2mL of the mixture was withdrawn from time t_c during the progress of hydrolysis of the ester and titrated with a solution of alkali. The amount of alkali needed for titration at various intervals is given below:

Time:	0	20	119	∞	(min)
Alkali used:	19.24	20.73	26.6	42.03	(mL)

Establish that the reaction is of first order.

Sol:

$$CH_3COOCH_3 + H_2O \xrightarrow[\text{[H]}]{HCl} CH_3COOH + CH_3OH$$
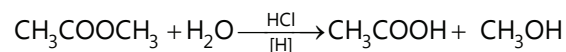
Ini.Conc. a

Conc. after t   (a-x)   x

HCl acts as a catalyst. The alkali used against HCl is subtracted from the total alkali used (given in the data) to get the volume of alkali used only against CH_3COOH.

At zero time, no CH_3COOH is formed. Hence, alkali used at zero time is only for HCl. Thus we have

Time(min) :	0	20	119	∞
Vol. of alkali (mL)used against CH_3COOH :	19.24	20.73	26.6	42.03

$$\begin{array}{cccc} -19.24 & -19.24 & -19.24 & -19.24 \\ =0 & =1.49 & =7.36 & =22.79 \\ & (x) & (x) & (a) \end{array}$$
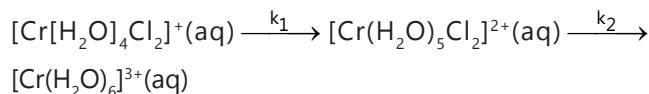
For t – 20;

$$k_1 = \frac{2.303}{20}\log\frac{22.79}{22.79 - 1.49} = 0.0033 \text{ min}^{-1}$$

For t = 119 ;

$$k_1 = \frac{2.303}{119}\log\frac{22.79}{22.79 - 7.36} = 0.0032 \text{ min}^{-1}$$

The constancy of k_1 shows that the reaction is of first order.

Example 7: For the reaction

$$[Cr[H_2O]_4Cl_2]^+(aq) \xrightarrow{k_1} [Cr(H_2O)_5Cl_2]^{2+}(aq) \xrightarrow{k_2}$$
$$[Cr(H_2O)_6]^{3+}(aq)$$

$k_1 = 1.76 \times 10^{-3}$ s^{-1} and $k_2 = 5.8 \times 10^{-5}$ s^{-1} for the initial concentration of $[Cr(H_2O)_5Cl_2]^+$ is 0.0174 mol/L at 0°C. Calculate the value of t at which the concentration of $[Cr(H_2O)_5Cl_2]^{2+}$ is maximum.

Sol: We have, t = $\dfrac{2.303(\log k_1 - \log k_2)}{k_1 - k_2}$

$$= \frac{2.303(\log 1.76 \times 10^{-3} - \log 5.8 \times 10^{-5})}{1.76 \times 10^{-3} - 5.8 \times 10^{-5}} = 2005 \text{ seconds.}$$

Example. 8: The complexation of Fe^{2+} with the chelating agent dipyridyl has been studied kinetically in both forward and reverse directions.

$$Fe^{2+} + 3 \text{ dipy} \rightarrow Fe(dipy)_3^{2+}$$
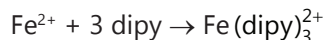
Rate (forward) = (1.45×10^{13}) $[Fe^{2+}][dipy]^3$ and rate (reverse) = $(1.22 \times 10^{-4}$ $[Fe(dipy)_3^{2+}]$.

Find the stability constant for the complex.

Sol: At dynamic equilibrium, Rate of formation of complex = Rate of its decomposition

$$(1.45 \times 10^{13}) [Fe^{2+}][dipy]^3 = (1.22 \times 10^{-4} [Fe(dipy)_3^{2+}]$$

$$k_a = \frac{[Fe(dipy)_3^{2+}]}{[Fe^{2+}][dipy]^3} = \frac{1.45 \times 10^{13}}{1.22 \times 10^{-4}} = 1.19 \times 10^{17}.$$

Example 9: Bicyclohexane was found to undergo two parallel first order rearrangements. At 730 K, the first order rate constant for the formation of cyclohexene was measured as 1.26×10^{-4} sec^{-1}, and for the formation of methyl cyclopentane the rate constant was 3.8×10^{-5} sec^{-1}. What is the percentage distribution of the rearrangement products?

Sol:
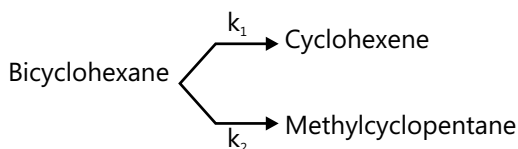
Percentage of cyclohexene $= \dfrac{k_1}{k_1 + k_2} \times 100$

$= \dfrac{1.26 \times 10^{-4}}{1.26 \times 10^{-4} + 3.8 \times 10^{-5}} \times 100 = 77\%$

$\therefore$ Percentage of methyl cyclopentane = 23%.

Example 10: A first-order reaction has a specific reaction rate of 10^{-2} sec^{-1}. How much time will it take for 10 g of its reactant to be reduced to 2.5 g?

Sol: Rate constant, $k = 10^{-2}$ sec^{-1}

Initial reactant conc. $[A]_0 = 10$ g

Final reactant conc. $[A]_t = 2.5$ g

Time required, t = ?

For a first-order reaction.

$t = 2.303 \times 10^2 \log 4 s = 230.3 \times 0.6020 s = 138.6 s$.

JEE Advanced/Boards

Example 1: The rate constant of a reaction is given by: ln K(sec^{-1}) = $14.34 - (1.25 \times 10^4)/T$. Calculate (a) the energy of activation and (b) the rate constant at 500 K. (c) At what temperature will its half-life period be 256 min?

Sol: Given:

ln K = $14.34 - [(1.25 \times 10^4)/T]$ ....(i)

Arrhenius equation, ln K = ln A $- (E_a/RT)$..(ii)

(a) Comparing equations (i) and (ii),

$(E_a/R) = 1.25 \times 10^4$ $\therefore$ $E_a = 1.25 \times 10^4 R$

$= 1.25 \times 10^4 \times 1.987 \times 10^{-3}$ kcal mol^{-1} = 24.84 kcal mol^{-1}

(b) ln K = $14.34 - [(1.25 \times 10^4)/500]$

($\because$ T = 500 K)

$\therefore$ K = 2.35×10^{-5} sec^{-1}

(c) K = $\dfrac{0.693}{256 \times 60}$ (for first order)

$\therefore$ log $\dfrac{0.693}{256 \times 60} = 14.34 - \dfrac{1.25 \times 10^4}{T}$

$\therefore$ T = 513 K

Example 2: The specific reaction rate of a first-order reaction is 0.02 sec^{-1}. The initial concentration of the reactant is 2 molL^{-1}. Calculate (a) initial rate, and (b) rate after 60 sec.

Sol: For a first-order reaction:

Rate of a reaction = k × molar concentration of the reactant.

(a) $\therefore$ Initial rate = k × initial concentration

= 0.02 × 2 = 0.04 mol/L^{-1} sec^{-1}.

(b) Concentration of the reactant after 60 sec k = $\dfrac{2.303}{60}$ log $\dfrac{2}{\text{concentration after 60 s}} = 0.02.$

$\therefore$ Concentration of the reactant after 60 sec = 0.60 M.

$\therefore$ Rate after 60 sec = k × concentration of the reactant after 60 sec.

= 0.02 × 0.60 = 0.012 molL^{-1} sec^{-1}

Example 3: The rate constant is numerically the same for first, second and third order reaction, the unit of concentration being in moles per litre. Which reaction should be the fastest and is this true for all ranges of concentrations ?

Sol: Suppose R_1, R_2 and R_3 are the rates of reactions of first, second and third order, respectively, and k is the rate constant, which is the same for the three reactions,

$\therefore$ $R_1 = k[A]^1$; $R_2 = k[A]^2$; $R_3 = k[A]^3$

[A] being the concentration of the reactant A in moles per litre.

Now if, [A] = 1, $R_1 = R_2 = R_3$;

[A] < 1, $R_1 > R_2 > R_3$; and

[A] > 1, $R_1 < R_2 < R_3$.

Example 4: For a reaction at 800°C

2NO + 2H$_2$ → N$_2$ + 2H$_2$O, the following data were obtained:

[NO]×10^{-4} mole/L	[H$_2$]×10^{-3} mole/L	d[NO]/dt×10^{-4} mole/L min
(i) 1.5	7.0	4.4
(ii) 1.5	3.5	2.2
(iii) 1.5	2.0	0.24

What is the order of this reaction with respect to NO and H$_2$?

Sol: From the data (i) and (ii), we see that when the concentration of H$_2$ is halved, the rate is also halved at constant concentration of NO. Hence the reaction is of first order with respect to H$_2$ Let us now consider the data (ii) and (iii) to determine the order with respect to NO as [H$_2$] is constant.

The rate law of the above reaction is

$$\text{rate} = -\frac{1}{2} \times \frac{d[NO]}{dt} = k[NO]^m[H_2]^1$$

where, m is the order with respect to NO

$$\text{Or} - \frac{d[NO]}{dt} = 2k[NO]^m[H_2]$$

Substituting data (ii) and (iii), we get

$2.2 \times 10^{-4} = 2k(1.5 \times 10^{-4})m. (2 \times 10^{-3})$ ...(i)

$0.24 \times 10^{-4} = 2k(0.5 \times 10^{-4})m. (2 \times 10^{-3})$ ...(ii)

Dividing (i) by (ii),

$$\frac{2.2}{0.24} = \frac{(1.5 \times 10^{-4})^m}{(0.5 \times 10^{-4})^m} = 3^m \text{ or } \frac{220}{24} = 3^m$$

Taking log, log 220 – log 24 = m log 3

$2.4324 - 1.3802 = m \times 0.4771$
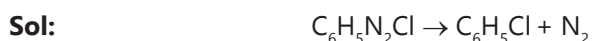
Or $0.9622 = 0.4771 m$ or $m = \frac{0.9622}{0.4771} = 2$.

Hence the reaction is of second and first order with respect to NO and H, respectively.

Example 5: From the following data for the de-composition of diazobenzene chloride, show that the reaction is of first order

Time	20	50	70	∞	(min)
Vol. of N$_2$	10	25	33	162	(mL)

Sol: C$_6$H$_5$N$_2$Cl → C$_6$H$_5$Cl + N$_2$

Initial concentration   a

After time t   (a – x)   x

At ∞ time, i.e. when the reaction is complete, the whole of C$_6$H$_5$N$_2$Cl converts into N$_2$. Hence volume of N$_2$ at ∞ time corresponds to the initial concentration 'a' while volumes of N$_2$ at different time intervals correspond to x as shown above. substituting the given data in equation of first-order reaction, we get the following results.

For t = 20 min

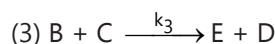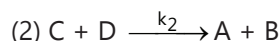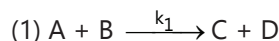$$k_1 = \frac{2.303}{20}\log\frac{162}{162-10} = 0.0032 \text{ min}^{-1}$$

For t = 50 min,

$$k_1 = \frac{2.303}{50}\log\frac{162}{162-25} = 0.0033 \text{ min}^{-1}$$

For t = 70 min,

$$k_1 = \frac{2.303}{70}\log\frac{162}{162-33} = 0.0032 \text{ min}^{-1}$$

The consistency of k$_1$ shows that the decomposition of C$_6$H$_5$N$_2$Cl is a first-order reaction.

Example 6: From the following reaction scheme, write the rate law for the disappearance of A, B and C.

(1) A + B $\xrightarrow{k_1}$ C + D

(2) C + D $\xrightarrow{k_2}$ A + B

(3) B + C $\xrightarrow{k_3}$ E + D

Sol.: The reaction A is removed in step 1 and produced in step 2

$$\therefore -\frac{d[A]}{dt} = k_1[A][B] - k_2[C][D] \text{ Similarly}$$

$$-\frac{d[B]}{dt} = k_1[A][B] + k_3[B][C] - k_2[C][D] \text{ and}$$

$$-\frac{d[C]}{dt} = k_2[C][D] + k_3[B][C] - k_1[A][B].$$

Example 7: At a certain temperature, the half change period for the catalytic decomposition of ammonia were found as follows:

Pressure (Pascals): 6667 13333 26666

Half life period in hours: 3.52 1.92 1.0

Calculate the order of reaction.

Sol: $\frac{(t_{1/2})_1}{(t_{1/2})_2} = \left(\frac{a_2}{a_1}\right)^{n-1}$

where, n is order of reaction

From the given data, $\frac{3.52}{1.92} = \left(\frac{13333}{6667}\right)^{n-1}$

(a ∝ initial pressure) = $(2)^{n-1}$

$\log \dfrac{3.52}{1.92} = (n-1)\log 2 = 0.3010 \times (n-1)$

$0.2632 = 0.3010 \times (n-1)$; $n = 1.87 \approx 2$

Similar calculations are made between first and third observations, n comes equal to 1.908 (≈ 2).
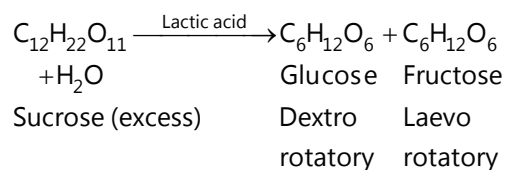
Thus, the reaction is of second order.

Example 8: The optical rotation of can sugar in 0.5 N acid at 25°C at various time intervals are given below:

Time (min):   0   1435   11360 ∞

Rotation(°):   34.50°   31.10°   13.98° $-$ 10.77°

Show that the reaction is of first order.

Sol:

$C_{12}H_{22}O_{11} \xrightarrow{\text{Lactic acid}} C_6H_{12}O_6 + C_6H_{12}O_6$
$\quad + H_2O \qquad\qquad\quad$ Glucose   Fructose
$\quad$ Sucrose (excess) $\qquad$ Dextro   Laevo
$\qquad\qquad\qquad\qquad\qquad$ rotatory   rotatory

Since in this reaction dextro form clianges to laevo form, the optical rotation decreases with the progress of the reaction. Thus change in rotation is proportional to the amount of sugar remaind after different time intervals. We now have,

| Time (min)	0	1435	11360	∞
Change in rotation(°)	34.50 $-$ ($-$10.77) = 45.27 (a)	31.10 $-$ ($-$10.77) = 4 1 . 8 7 (a $-$ x)	13.98 $-$ (-10.77) =24.75 (a $-$ x)	$-$ 10.77$-$ ($-$10.77) = 0

Substituting the data in equation,

for t = 1435 min

$k_1 = \dfrac{2.303}{1435}\log\dfrac{45.27}{41.87} = 5.442 \times 10^{-5}$

and for t = 1136 min

$k_1 = \dfrac{2.303}{1435}\log\dfrac{45.27}{41.87} = 5.311 \times 10^{-5}$

The values of k are fairly constant and so the reaction is of first order .

Example 9: The catalytic decomposition of formic acid may take place in two ways:

(i) $HCOOH \rightarrow H_2O + CO$

(ii) $HCOOH \rightarrow H_2 + CO_2$
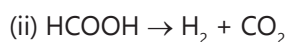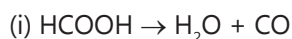
The rate constant and activation energy for reaction (i) are 2.79×10^{-3} min^{-1} at 237°C and 12.0 kcal mol^{-1} respectively. These values for reaction (ii) are 1.52×10^{-4} min^{-1} at 237°C and 24.5 kcal mol^{-1} respectively. Find out the temperature at which equimolar quantities of H_2O, CO, CO_2 and H_2 are formed (R = 2 cal).

Sol: For reaction (a) $K_1 = A_1 e^{-E_a/RT}$

or $2.79 \times 10^{-3} = A_1 e^{-\frac{12 \times 10^3}{RT}}$ ......(i)

For reaction (b): $K_2 = A_2 e^{-E_a/RT}$

$1.52 \times 10^{-4} = A_2 e^{-\frac{24.5 \times 10^3}{RT}}$ ...(ii)

By equation (i) $A_1 = \dfrac{2.79 \times 10^{-3}}{e^{-\frac{12 \times 10^3}{2 \times 510}}} = \dfrac{2.79 \times 10^{-3}}{7.8 \times 10^{-6}}$

$= 3.58 \times 10^2$

By equation (ii) $A_2 = \dfrac{1.52 \times 10^{-4}}{e^{-\frac{24.5 \times 10^3}{2 \times 510}}} = \dfrac{1.52 \times 10^{-4}}{3.7 \times 10^{-11}}$

$= 4.11 \times 10^6$

If rate constants of two reactions are same, the reactions will give equimolar mixture of products. Let these be same at temperature T, i.e.

$A_1 e^{-E_{a_1}/RT} = A_2 e^{-E_{a_2}/RT}$

$\therefore e^{\frac{E_{a_2}-E_{a_1}}{RT}} = \dfrac{A_2}{A_1}$ or $e^{\frac{[24.5-12.0]\times 10^3}{RT}} = \dfrac{A_2}{A_1}$

$= \dfrac{4.11 \times 10^6}{3.58 \times 10^2} = 1.15 \times 10^4$

Or $\dfrac{10^3}{RT} \times 12.5 = 9.35$ \T $= \dfrac{12.5 \times 10^3}{9.35 \times 2} = 668$ K

$\therefore$ T = 668 K = 395°C

Example 10: For the reversible reaction in equilibrium:
A $\underset{k_2}{\overset{k_1}{\rightleftharpoons}}$ B. The values of K_1 and K_2 are 2×10^{-3} mol L^{-1} sec^{-1} and 3×10^{-3} mol L^{-1} sec^{-1} respectively. If we add 0.5 mol of B in the equilibrium mixture, initially containing 2 mol of A. Calculate the time taken for concentration of B to become equal to 3/4 of the concentration of A at initial equilibrium. The volume of mixture is 1 L and remains constant.

Sol: A $\underset{k_2}{\overset{k_1}{\rightleftharpoons}}$ B
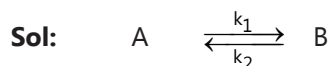
t = 0   2 mol L^{-1} 0

At eq.   (2 – X) mol L^{-1} X

K$_1$ = 2 × 10^{-3} mole L^{-1} sec^{-1} (zero order)

K$_2$ = 3 × 10^{-3} sec^{-1} (Ist order)

$\dfrac{dX}{dt} = K_1[A]^0 - K_2[B]^1$

At equilibrium $\dfrac{dX}{dt} = 0$

∴ $0 = K_1 - K_2[X]_{eq}$; \[X]$_{eq}$ = $\dfrac{K_1}{K_2} = \dfrac{2 \times 10^{-3}}{3 \times 10^{-3}}$

= 0.66 mol L^{-1} = K$_c$

$\qquad\qquad$ A $\rightleftharpoons$ B
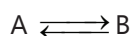
Initial eq.   1.34   0.66

Moles added   1.34   0.66+0.5= 1.16

At eq. at time t (1.34 +X)   (1.16 –X)

(The reaction will obey back ward direction on addition of B)

∵ [B] = $\dfrac{3}{4}$ [A]$_{eq}$ = $\dfrac{3}{4}$ × 1.34 = 1.005

(1.16 – X) = 1.005;   ∴ X = 0.155

Now, $\dfrac{dX}{dt}$ = K$_1$ – K$_2$[X] = 0.66K$_2$ –K$_2$X

= K$_2$[0.66 – X] ; ∴ $\dfrac{dX}{(0.66 - X)}$ = K$_2$. dt

or – 2.303 log (0.66 – X) = K$_2$. t + C

at t = 0, X = 0   ∴ C = – 2.303 log 0.66

∴ K$_2$. t = 2.303 log $\dfrac{0.66}{0.66 - X}$

∴ t = $\dfrac{2.303}{3 \times 10^{-3}}$ log $\dfrac{0.66}{0.66 - 0.155}$ = 89.24 sec

(a) Partial pressure becomes half of initial in every 100 min, therefore, order = 1.

(b) k × 100 = ln $\dfrac{800}{400}$

k × 100 = ln 2

⇒ k = 6.93 × 10^{-3} min^{-1}

(c) For 75% reaction; time required

= 2 × half-life = 200 min

(d) 2X(g) →   3Y(g)   + 2Z(g)

800 – x $\dfrac{3}{2}$ x   x

Total pressure = 800 + $\dfrac{3}{2}$x

Also 800 – x = 700 ⇒ x = 100

⇒ Total pressure = 800 + $\dfrac{3}{2}$ × 100 = 950 mm

JEE Main/Boards

Exercise 1

Q.1 A solution of A is mixed with an equal volume of a solution of B containing the same number of moles, and the reaction A + B → C occurs. At the end of 1h, A is 75% reacted. How much of A will be left unreacted at the end of 2h if the reaction is (a) first order in A and zero order in B; (b) first order in both A and B; and (c) zero order in both A and B?

Q.2 The reaction CH$_3$–CH$_2$–NO$_2$+ OH$^-$ → CH$_3$–CH–NO$_2$$^-$ +H$_2$O obeys the rate law for pseudo first order kinetic in the presence of a large excess of hydroxide ion . If 1% of nitro ethane undergoes reaction in half minute when the reaction concentration is 0.002 M, What is the pseudo first order rate constant?

Q.3 The decomposition of a compound P at temperature T according to the equation

$\qquad$ 2P$_{(g)}$ → 4Q$_{(g)}$ + R$_{(g)}$ + S$_{(l)}$
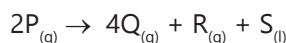
is the first order reaction. After 30 minutes from the start of decomposition in a closed vessel the total pressure developed is found to be 317 mm Hg and after a long period of time the total pressure observed to be 617 mm Hg. Calculate the total pressure of the vessel after 75 minute, if volume of liquid S is supposed to be negligible ,also calculate the tiny fraction t$_{1/8.}$

Given: Vapor pressure of S (ℓ) at temperature T = 32.5 mm Hg.

Q.4 A certain reactant B^{n+} is getting converted to B$^{(n + 4)+}$ in solution. The rate constant of this reaction is measured by titrating a volume of the solution with a

reducing reagent which only reacts with B^{n+} and $B^{(n+4)+}$. In this process, it converts B^{n+} to $B^{(n-2)+}$ and $B^{(n+4)+}$ to $B^{(n-1)+}$. At t = 0 the volume of the reagent consumed is 25 ml and at t = 10 min, the volume used up is 32 ml. Calculate the rate constant of the conversion of B^{n+} to $B^{(n+4)+}$ assuming it to be a first order reaction.

Q.5 Decomposition of H_2O_2 is a first order reaction. A solution of H_2O_2 labelled as 20 volumes was left open due to this, some H_2O_2 decomposed. To determine the new volume strength after 6 hours 10 mL of this solution was diluted to 100 mL .10mL of this diluted solution was titrated against 25mL of 0.025 M $KMnO_4$ solution under acidic conditions. Calculate the rate constant for decomposition of H_2O_2.

Q.6 A metal slowly forms an oxide film which completely protects the metal when the film thickness is 3.956 thousand times of an inch. If the film thickness is 1.281 thou. in 6 weeks, how much longer will it be before it is 2.481 thou.? The rate of film formation follows first order kinetics.

Q.7 An optically active compound A upon acid catalyzed hydrolysis yield two optically active compound B and C by pseudo first order kinetics. The observed rotation of the mixture after 20 min was 5° while after completion of the reaction it was – 20°. If optical rotation per mole of A, B & C are 60°,40° & – 80°. Calculate half-life of the reaction.

Q.8 A vessel contains dimethyl ether at a pressure of 0.4atm. Dimethyl ether decomposes as $CH_3OCH_3(g)$ → $CH_4(g)$ + $CO(g)$ + $H_2(g)$. The rate constant of decomposition is 4.78×10^{-3} min^{-1}. Calculate the ratio of initial rate of diffusion to rate of diffusion after 4.5 hours of initiation of decomposition.

Q.9 At room temperature (20°C) orange juice gets spoilt in about 64 hours. In a refrigerator at 3°C juice can be stored three times as long before it gets spoilt. Estimate (a) the activation energy of the reaction that causes the spoiling of juice (b) How long should it take for juice to get spoilt at 40°C?

**Q.10** A first order reaction, A → B, requires activation energy of 70 kJ mol^{-1}.When a 20% solution of A was kept at 25°C for 20 minutes, 25% decomposition took place. What will be the percent decomposition in the same time in a 30% solution maintained at 40°C ? Assume that activation energy remains constant in this range of temperature.

Q.11 Two reactions

(i)   A → products

(ii) B → products,

follow first order kinetics. The rate of the reaction (i) is doubled when the temperature is raised from 300 K to 310 K. The half-life for this reaction at 310 K is 30 minutes. At the same temperature B decomposes twice as fast as A. If the energy of activation for the reaction is half of that of reaction, calculate the rate constant of the reaction (ii) at 300 K

Q.12 A certain organic compound A decomposes by two parallel first order mechanism
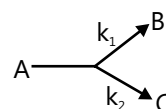
If $k_1 : k_2$ = 1: 9 and k_1 = 1.3×10^{-5}s^{-1}.

Calculate the concentration ratio of C to A, if an experiment is started with only A and allowed to run for one hour.

Q.13 The reaction cis $-$ $Cr(en)_2(OH)_2^+$ $\underset{k_2}{\overset{k_1}{\rightleftharpoons}}$ trans– $Cr(en)_2(OH)_2^+$ is first order in both directions. At 25°C the equilibrium constant is 0.16 and the rate constant k_1 is 3.3×10^{-4} s^{-1}. In an experiment starting with the pure cis form, how long would it take for half the equilibrium amount of the Trans isomer to be formed?

Q.14 For a reversible first-order reaction A $\underset{k_2}{\overset{k_1}{\rightleftharpoons}}$ B k_1 = 10^{-2} s^{-1} and $[B]_{eq}/[A]_{eq}$ = 4. If $[A]_0$ = 0.01 mole L^{-1} and $[B]_0$ = 0, what will be the concentration of B after 30 s?

Q.15 For the system $A(g) \to B(g)$, ΔH for the forward reaction is –33kJ/mol (Note. $\Delta H = \Delta E$ in this case).

Show that equilibrium constant

$K = \dfrac{[B]}{[A]}$ = 5.572×10^5 at 300 K. If the activation energies E_r and E_b are in the ratio 20: 31. Calculate E_r and E_b at this temperature .Assume that the pre-exponential factor is the same for the forward and backward reactions

**Q.16** The complex $[Co(NH_3)_5F]^{2+}$ reacts with water according to the equation

$[Co(NH_3)_5F]^{2+} + H_2O \to [Co(NH_3)5(H_2O)]^{3+} + F^-$
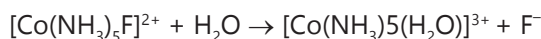
The rate of the reaction = rate const. x[complex]^a x[H$^+$]^b. The reaction is acid catalysed i.e. [H$^+$] does not change during the reaction.

Thus rate = k[Complex]^a where k' = k[H$^+$]^b calculate 'a' and 'b' given the following data at 25°C.

[Complex]M	[H$^+$]M	$T_{1/2}$hr	$T_{3/4}$hr
0.1	0.01	1	2
0.2	0.02	0.5	1

Q.17 For the two parallel reactions A$\xrightarrow{k_1}$B and A$\xrightarrow{k_2}$C, show that the activation energy E' for the disappearance of A is given in terms of activation energies E$_1$ and E$_2$ for the two paths by E' = $\dfrac{k_1E_1 + k_2E_2}{k_1 + k_2}$
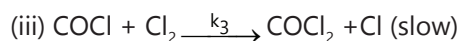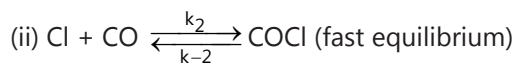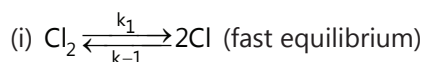
Q.18 For the mechanism

A + B $\underset{k_2}{\overset{k_1}{\rightleftharpoons}}$ C ; C $\xrightarrow{k_3}$ D
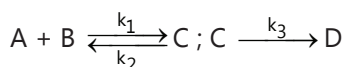
(a) Derive the rate law using the steady-state approximation to eliminate the concentration of C.

(b) Assuming that k$_3$ << k$_2$, express the pre-exponential factor A and E$_a$ for the apparent second order rate constant in terms of A$_1$, A$_2$ and A$_3$ and E$_{a_1}$, E$_{a_2}$ and E$_{a_3}$ for the three steps.

Q.19 The reaction of formation of phosgene from CO and Cl$_2$ is CO + Cl$_2$ → COCl$_2$

The proposed mechanism is

(i) Cl$_2$ $\underset{k-1}{\overset{k_1}{\rightleftharpoons}}$ 2Cl (fast equilibrium)

(ii) Cl + CO $\underset{k-2}{\overset{k_2}{\rightleftharpoons}}$ COCl (fast equilibrium)

(iii) COCl + Cl$_2$ $\xrightarrow{k_3}$ COCl$_2$ +Cl (slow)

Show that the above mechanism leads to the following rate law $\dfrac{d[COCl_2]}{dt}$ = K[CO][Cl$_2$]$^{3/2}$.

Where K = $k_3 \cdot \dfrac{k_2}{k-2}\left(\dfrac{k_1}{k-1}\right)^{1/2}$.

Q.20 For the following first order gaseous reaction
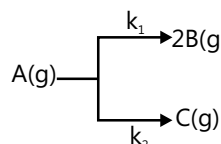
The initial pressure in a container of capacity V litres is 1 atm. Pressure at time t = 10 sec is 1.4 atm and after infinite time it becomes 1.5 atmosphere. Find the rate constant k$_1$ and k$_2$ for the appropriate reaction.

Q.21 A first order reaction takes 69.3 minutes for 50% completion. How much time will be needed for 80% completion?

Q.22 The specific rate constant for a reaction increases by a factor 4 of the temperature is changed from 27°C to 47°C. Find the activation energy for the reaction

Q.23 The reaction 2A+ B + C → D + 2 E is of first order with respect to A and of second order with respect to B and is of zero order with respect to C

(i) Write down the rate law for the reaction

(ii) What will be the effect of doubling concentration of A, B and C.

Q.24 A first order reaction is 50% completed in 30 min at 27°C and in 10 minutes at 47°C. Calculate the rate constant at 27°C and the energy- of activation of the reaction in kJ per mole

Q.25 The optical rotation of sucrose in 0.5 M HCl at 35° C at different time intervals are given below. Show that the reaction follows first order kinetics

Time (min)	0	10	20	30	40	∞
Rotation (degrees)	+32.4	+28.8	+25.5	+22.4	+19.6	−11.1

Q.26 $t_{1/2}$ of a reaction is halved as the initial concentration of the reaction is doubled, find out the order of the reaction.

Q.27 The rate constant of a reaction is 1.5 × 10^{-7} sec^{-1} at 50°C and 4.5 × 10^{-7} sec^{-1} at 100°C. Evaluate the Arrhenius parameters A and Ea.

Q.28 A substance reacts according to the law of first order reaction the velocity constant of the reaction is 1.0 × 10^{-2} sec^{-1}. If initial conc. of the substance is 1.0 M

(a) Find out the initial rate

(b) Find out the rate after 1 min.

Q.29 What will be initial rate of a reaction if its rate constant is 10^{-3} min^{-1} and concentration of reactant is 0.2 mol dm^{-3}. How much of reactant will be converted into products in 200 minutes.

Q.30 A first order reaction is 20% complete in 10 minutes. Calculate

(a) Specific rate constant of the reaction and

(b) Time taken for the reaction to go to 75 % completion

Exercise 2

Single Correct Choice Type

Q.1 For the reaction A + B → C; starting with different initial concentration of A and B, initial rate of reaction were determined graphically in four experiments.

S. No.	$[A]_0$/M (Initial conc.)	$[B]_0$/M (Initial conc.)	rate/ (M sec^{-1})
1	1.6×10^{-3}	5×10^{-2}	10^{-3}
2	3.2×10^{-3}	5×10^{-2}	4×10^{-3}
3	1.6×10^{-3}	10^{-1}	2×10^{-3}
4	3.2×10^{-3}	10^{-1}	8×10^{-3}

Rate law for reaction from above data is

(A) $r = k[A]^2W^2$ (B) $r = k[A]^2[B]$

(C) $r = k[A][B]^2$ (D) $r = k[A][B]$

Q.2 The rate law for a reaction between the substances A and B is given by rate = $k [A]^n [B]^m$ On doubling the concentration of A and halving the concentration of B, the ratio of the new rate to the earlier rate of the reaction will be as

(A) $2^{(n-m)}$ (B) $1/2^{m+n}$ (C) $(m + n)$ (D) $(n - m)$

Q.3 In a first order reaction, the concentration of the reactant, decreases from 0.8 to 0.4 M in 15 minutes. The time taken for the concentration to change from 0.1 M to 0.025 M is

(A) 30 minutes   (B) 15 minutes

(C) 7.5 minutes   (D) 60 minutes

Q.4 The rate equation for the reaction

2A + B → C is found to be: rate=k [A] [B] The correct statement in relation to this reaction is

(A) Unit of k must be s^{-1}

(B) $t_{1/2}$ is a constant

(C) Rate of formation of C is twice the rate of disappearance of A

(D) Value of k is independent of the initial concentration of A and B

Q.5 $t_{1/4}$ can be taken as the time taken for the concentration of a reactant to drop to 3/4 of its value. If the rate constant for a first order reaction is k, the $t_{3/4}$ can be written as

(A) 0.69/k   (B) 0.75/k   (C) 0.10/k   (D) 0.29/k

Q.6 A reaction was found to be second order with respect to the concentration of carbon monoxide. If the concentration of carbon monoxide is doubled, with everything else kept the same, the rate of reaction will

(A) Double   (B) Remain unchanged

(C) Triple   (D) Increase by a factor of 4

Q.7 For a hypothetical reaction,

A + 3B → P ΔH = −2x kJ/mole of A

and M → 2Q + R ΔH = −x kJ/mole of M
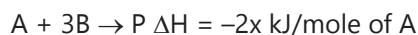
If these reactions are carried simultaneously in a reactor such that temperature is not changing. If rate of disappearance of B is y M sec^{-1} then rate of formation (in M sec^{-1}) of Q is:

(A) $\dfrac{2}{3}y$ (B) $\dfrac{3}{2}y$ (C) $\dfrac{4}{3}y$ (D) $\dfrac{3}{4}y$

Q.8 Gaseous reaction A → B + C follows first order kinetics. Concentration of A changes from 1M to 0.25 M in 138.6 minutes. Find the rate of reaction when concentration of A is 0.1 M.

(A) 2×10^{-3}M min^{-1} (B) 10^{-3}M min^{-1}

(C) 10^{-4}M min^{-1} (D) 5×10^{-4}M min^{-1}

Q.9 The initial rate of zero-order reaction of the gaseous reaction A(g) → 2B(g) is 10^{-2} M min^{-1}. If the initial concentration of A is 0.1M. What would be the concentration of B after 60 sec?

(A) 0.09 M   (B) 0.01 M

(C) 0.02 M   (D) 0.002 M

Q.10 Consider the following first order competing reactions:

$X \xrightarrow{k_1} A + B$ and $Y \xrightarrow{k_2} C + D$ if 50% of the reaction of X was completed when 96% of the reaction of Y was completed the ratio of their rate constants (k_2/k_1) is

(A) 4.06   (B) 0.215   (3) 1.1   (D) 4.65

Q.11 At certain temperature, the half-life period for the thermal decomposition of a gaseous substance depends on the initial partial pressure of the substance as follows

P(mm Hg) 500 250

$t_{1/2}$(in min) 235 950

Find the order of reaction

[Given log(23.5) = 1.37; log (95)= 1.97; log 2 = 0.30]
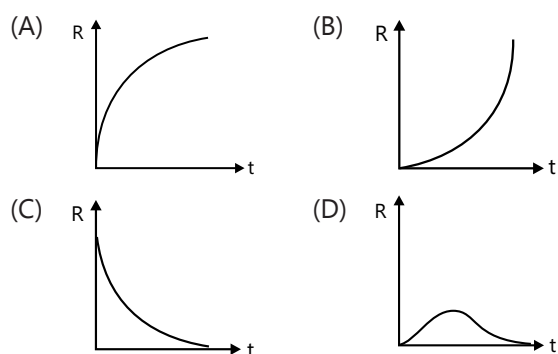
(A) 1   (B) 2   (C) 2.5   (D) 3

Q.12 Consider the reaction: A → B + C

Initial concentration of A is 1M. 20 minutes time is required for completion of 20% reaction.

If $\dfrac{d[B]}{dt}$ =k[A], then half life $(t_{1/2})$ is

(A) 55.44 min   (B) 50 min

(C) 62.13 min   (D) None of these

Q.13 If decomposition reaction A(g) → B (g) follows first order kinetics then the graph of rate of formation (R) of B against time t will be

(A)

(B)

(C)

(D)

Q.14 The rate constant for the forward reaction A(g) → 2B(g) is 1.5 × 10⁻³ s⁻¹ at 100 K. If 10⁻⁵ moles of A and 100 moles of B are present in a 10 litre vessel at equilibrium then rate constant for the backward reaction at this temperature is

(A) 1.50 × 10⁴L mol⁻¹ s⁻¹   (B) 1.5 × 10¹¹L mol⁻¹ s⁻¹

(C) 1.5 × 10¹⁰L mol⁻¹ s⁻¹   (D) 1.5 × 10⁻¹¹L mol⁻¹ s⁻¹

Q.15 Reaction A + B → C + D follows following rate law: rate = k[A]$^{1/2}$[B]$^{1/2}$. Starting with initial conc. of 1 M of A and B each, what is the time taken for concentration of A to become 0.25 M.

Given: k = 2.303 × 10⁻³ sec⁻¹

(A) 300sec.   (B) 600 sec.   (C) 900 sec.   (D) 1200 sec.

Q.16 The reaction A (g) → B(g) + 2C (g) is a first order reaction with rate constant 3.465 × 10⁻⁶s⁻¹.Starting with 0.1 mole of A in 2 litre vessel, find the concentration of A after 200 sec, when the reaction is allowed to take place at constant pressure and temperature

(A) 0.05 M   (B) 0.025 M

(C) 0.0125 M   (D) None of these

Q.17 In respect of the equation k = A exp (– E_a / RT), which one of the following statements is correct?

(A) R is Rydberg's constant

(B) k is equilibrium constant

(C) A is adsorption factor

(D) E_a is the energy of activation

Q.18 Rate of a reaction can be expressed by Arrhenius equation as k = Ae$^{-E/RT}$ In this equation, E represents

(A) The fraction of molecules with energy greater than the activation energy of the reaction

(B) The energy above which all the colliding molecules will react

(C) The energy below which colliding molecules will not react

(D) The total energy of the reacting molecules at a temperature T.

Q.19 The rate constant, the activation energy and the Arrhenius parameter (A) of a chemical reaction at 25°C are 3.0 × 10⁻⁴ s⁻¹, 104.4 kJmol⁻¹ and 6.0 × 10⁴ S⁻¹ respectively. The value of the rare constant at T → ∞

(A) 2.0 × 10⁻¹⁸s⁻¹   (B) 6.0 × 10¹⁴s⁻¹

(C) Infinity   (D) 3.6 × 10³⁰s⁻¹

Q.20 A first order reaction is 50% completed in 20 minutes at 27°C and in 5 min at 47°C. The energy of activation of the reaction is

(A) 43.85kJ/mol   (B) 55.14kJ/mol

(C) 11.97kJ/mol   (D) 6.65kJ/mol

Q.21 For the first order reaction A → B + C, carried out at 27°C if 3.8 × 10⁻¹⁶ % of the reaction molecules exists in the activated state, the E_a(activation energy) of the reaction is [log 3.8 = 0.58]

(A) 12 kJ/mole   (B) 831.4kJ/mole

(C) 100 kJ/mole   (D) 88.57kJ/mole

Q.22 In a reaction carried out at 400 K , 0.0001% of the total number of collisions are effective. The energy of activation of the reaction is

(A) Zero

(B) 7.37k cal/mol

(C) 9.212 k cal/mol

(D) 11.05k cal/mol

Previous Years' Questions

Q.1 For a reaction $\frac{1}{2}A \rightarrow 2B$, rate of disappearance of 'A' is related to the rate of appearance of B' by the expression **(2008)**

(A) $-\frac{d[A]}{dt} = \frac{1}{4}\frac{d[B]}{dt}$

(B) $-\frac{d[A]}{dt} = \frac{d[B]}{dt}$

(C) $-\frac{d[A]}{dt} = 4\frac{d[B]}{dt}$

(D) $-\frac{d[A]}{dt} = \frac{1}{2}\frac{d[B]}{dt}$

Q.2 The rate of a chemical reaction doubles for every 10° C rise of temperature. If the temperature is raised by 50° C, the rate of the reaction increases by about **(2011)**

(A) 10 times

(B) 24 times

(C) 32 times

(D) 64 times

Q.3 In a first order reaction the concentration of reactant decreases from 800 mol/dm³ to 50 mol/dm³ in 2×10^2 sec. The rate constant of reaction in sec⁻¹ is **(2003)**

(A) 2×10^4

(B) 3.45×10^{-5}

(C) 1.386×10^{-2}

(D) 2×10^{-4}

Q.4 Consider the reaction, 2 A + B → Products When concentration of B alone was doubled, the half-life did not change. When the concentration of A alone was doubled, the rate increased by two times. The unit of rate constant for this reaction is **(2007)**

(A) L mol⁻¹ s⁻¹

(B) No unit

(C) mol L⁻¹ s⁻¹

(D) s⁻¹

Q.5 The rate constant for the reaction,

$2N_2O_5 \rightarrow 4NO_2 + O_2$ is 3×10^{-5} sec⁻¹. If the rate is 2.40×10^{-5} mol litre⁻¹ sec⁻¹.

Then the concentration of N_2O_5 (in mol litre⁻¹) is **(2001)**

(A) 1.4

(B) 1.2

(C) 0.04

(D) 0

Q.6 The half-life period of a first order chemical reaction is 6.93 minutes. The time required for the completion of 99% of the chemical reaction will be (log 2 = 0.301)

(2009)

(A) 230.3 minutes

(B) 23.03 minutes

(C) 46.06 minutes

(D) 460.6 minutes

Q.7 A reaction involving two different reactants **(2005)**

(A) Can never be a second order reaction

(B) Can never be a unimolecular reaction

(C) Can never be a bimolecular reaction

(D) Can never be a first order reaction

Q.8 A reaction was found to be second order with respect to the concentration of carbon monoxide. If the concentration of carbon monoxide is doubled with everything else kept the same, the rate of reaction will

(2006)

(A) Remain unchanged
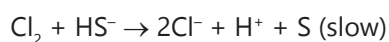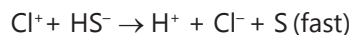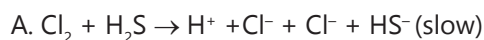
(B) Triple

(C) Increase by a factor of 4

(D) Double

Q.9 For the reaction A + 2B → C, rate is given by R = [A][B]² then the order of the reaction is **(2002)**

(A) 3

(B) 6

(C) 5

(D) 7

Q.10 The following mechanism has been proposed for the reaction of NO with Br_2 to from NOBr: NO(g) + Br_2 (g) $\rightleftharpoons$ $NOBr_2$ (g) $NOBr_2$(g) + NO(g) → 2NOBr (g) If the second step is the rate determining step, the order of the reaction with respect to NO(g) is **(2006)**

(A) 1

(B) 0

(C) 3

(D) 2

Q.11 Consider the reaction $Cl_{2(aq)} + H_2S_{(aq)} \rightarrow S_{(s)} + 2H^+_{(aq)} + 2Cl^-_{(aq)}$ The rate equation for this reaction is rate = $k[Cl_2][H_2S]$ Which of these mechanisms is/are consistent with this rate equation

A. $Cl_2 + H_2S \rightarrow H^+ + Cl^- + Cl^- + HS^-$ (slow)

$Cl^+ + HS^- \rightarrow H^+ + Cl^- + S$ (fast)

B. $H_2S \rightleftharpoons H^+ + HS^-$ (fast equilibrium)

$Cl_2 + HS^- \rightarrow 2Cl^- + H^+ + S$ (slow) **(2010)**

(A) A only

(B) B only

(C) Both A and B

(D) Neither A nor B

Q.12 The time for half life period of a certain reaction A → Products is 1 hour. When the initial concentration of the reactant 'A' is 2.0 mol L^{-1}, how much time does it take for its concentration to come for 0.50 to 0.25 mol L^{-1} if it is a zero order reaction   **(2010)**

(A) 1 h   (B) 4h   (C) 0.5h   (D) 0.25 h

Q.13 The energies of activation for forward and reverse reactions for $A_2 + B_2 \longrightarrow 2AB$ are 180kJ mol^{-1} and 200kJ mol^{-1} respectively. The presence of catalyst lowers the activation energy of both (forward and reverse) reactions by 100 kJ mol^{-1}. The enthalpy change of the reaction ($A_2 + B_2 \rightarrow 2AB$) in the presence of catalyst will be (in kJ mol^{-1})   **(2007)**

(A) 300   (B) -120   (C) 280   (D)- 20

Q.14 Consider an endothermic reaction X → Y with the activation energies E_b and E_f for the backward and forward reactions, respectively, in general   **(2005)**

(A) $E_b < E_f$

(B) $E_b > E_f$

(C) $E_b = E_f$

(D) There is no definite relation between E_b and E_f

Q.15 If 'I' is the intensity of absorbed light and C is the concentration of AB for the photochemical process AB + hυ → AB*, the rate of formation of AB* is directly proportional to   **(2001)**

(A) C   (B) I   (C) I^2 (D) C.I

Q.16 For a reaction $\dfrac{1}{2}A \longrightarrow 2B$, rate of disappearance of 'A' is related to the rate of appearance of 'B' by the expression   **(2008)**

(A) $-\dfrac{d[A]}{dt} = \dfrac{1}{2}\dfrac{d[B]}{dt}$ (B) $-\dfrac{d[A]}{dt} = \dfrac{1}{4}\dfrac{d[B]}{dt}$

(C) $-\dfrac{d[A]}{dt} = \dfrac{d[B]}{dt}$ (D) $-\dfrac{d[A]}{dt} = 4\dfrac{d[B]}{dt}$

Q.17 The half-life period of a first order chemical reaction is 6.93 minutes. The time required for the completion of 99% of the chemical reaction will be (log 2 = 0.301)   **(2009)**
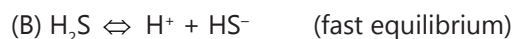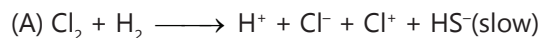
(A) 230.3 minutes   (B) 23.03 minutes

(C) 46.06 minutes   (D) 460.6 minutes

Q.18 The time for half-life period of a certain reaction A $\longrightarrow$ products is 1 hour. When the initial Concentration of the reactant 'A', is 2.0 mol/L, how much time does it take for its concentration to come from 0.50 to 0.25 mol/L if it is a zero order reaction?   **(2010)**

(A) 4 h   (B) 0.5 h   (C) 0.25 h   (D) 1 h

Q.19 Consider the reaction: $Cl_2(aq) + H_2S(aq) \longrightarrow$ S(s) + 2H$^+$(aq) + 2Cl$^-$ (aq) The rate equation for this reaction is rate = k [Cl$_2$] [H$_2$S]

Which of these mechanisms is/are consistent with this rate equation?   **(2010)**

(A) $Cl_2 + H_2 \longrightarrow$ H$^+$ + Cl$^-$ + Cl$^+$ + HS$^-$(slow)

Cl$^+$ + HS$^- \longrightarrow$ H$^+$ + Cl$^-$ + S   (fast)

(B) $H_2S \Leftrightarrow$ H$^+$ + HS$^-$ (fast equilibrium)

Cl_2 + HS$^- \longrightarrow$ 2Cl$^-$ + H$^+$ + S (slow)

(A) B only   (B) Both A and B

(C) Neither A nor B   (D) A only

Q.20 The rate of a chemical reaction doubles for every 10ºC rise of temperature. If the temperature is raised by 50ºC, the rate of the reaction increases by about: **(2011)**

(A) 24 times   (B) 32 times

(C) 64 times   (D) 10 times

Q.21 For a first order reaction, (A) $\longrightarrow$ products, the concentration of A changes from 0.1 M to 0.025 M in 40 minutes. The rate of reaction when the concentration of A is 0.01 M is: **(2012)**

(A) 1.73 x 10^{-5} M/ min   (B) 3.47 x 10^{-4} M/min

(C) 3.47 x 10^{-5} M/min   (D) 1.73 x 10^{-4} M/min

Q.22 The rate of a reaction doubles when its temperature changes from 300 K to 310 K. Activation energy of such a reaction will be : (R = 8.314 JK^{-1} mol^{-1} and log 2 = 0.301)   **(2013)**

(A) 53.6 kJ mol^{-1} (B) 48.6 kJ mol^{-1}

(C) 58.5 kJ mol^{-1} (D) 60.5 kJ mol^{-1}

Q.23 . For the non-stoichiometry reaction 2A + B → C + D, the following kinetic data were obtained in three separate experiments, all at 298 K.   **(2014)**

Initial Concentration (A)	Initial Concentration (A)	Initial rate of formation (C) (mol L⁻¹s⁻¹)
0.1 M	0.1 M	1.2×10^{-3}
0.1 M	0.2 M	1.2×10^{-3}
0.2 M	0.1 M	2.4×10^{-3}

The rate law for the formation of C is

(A) $\dfrac{dC}{dt} = k[A][B]$　　　(B) $\dfrac{dC}{dt} = k[A]^2[B]$

(C) $\dfrac{dC}{dt} = k[A][B]^2$　　　(D) $\dfrac{dC}{dt} = k[A]$

Q.24 Decomposition of H_2O_2 follows a first order reaction. In fifty minutes the concentration of H_2O_2 decreases from 0.5 to 0.125 M in one such decomposition. When the concentration of H_2O_2 reaches 0.05 M, the rate of formation of O_2 will be: **(2016)**

(A) 6.93×10^{-4} mol min⁻¹　　(B) 2.66 L min⁻¹at STP

(C) 1.34×10^{-2} mol min⁻¹　　(D) 6.93×10^{-2} mol min⁻¹

JEE Advanced/Boards

Exercise 1

Q.1 Ammonia and oxygen reacts at higher temperatures as $4NH_3(g) + 5O_2(g) \rightarrow 4NO(g) + 6H_2O(g)$

In an experiment, the concentration of NO increases by 1.08×10^{-2} mol litre⁻¹ in 3 seconds. Calculate

(i) Rate of reaction (ii) Rate of disappearance of ammonia (iii) Rate of formation of water

Q.2 In the following reaction $2H_2O_2 \rightarrow 2H_2O + O$ rate of formation of O_2 is 3.6 M min⁻¹

(i) What is rate of formation of H_2O?

(ii) What is rate of disappearance of H_2O_2?

Q.3 In a catalytic experiment involving the Haber process $N_2 + 3H_2 \rightarrow 2NH_3$, the rate of reaction was measured as

Rate = $\dfrac{\Delta[NH_3]}{\Delta t}$ = 2 × 10⁻⁴ mol L⁻¹ s⁻¹.

If there were no side reactions, what was the rate of reaction expressed in terms of (a) N_2, (b) H_2?

Q.4 The reaction $2A + B + C \rightarrow D + E$ is found to be first order in A second order in B and zero order in C. (1)

Give the rate law for the reaction in the form of differential equation.

(ii) What is the effect in rate of increasing concentrations of A, B, and C two times?

Q.5 At 27°C it was observed during a reaction of hydrogenation that the pressure of hydrogen gas decreases from 2 atmosphere to 1.1 atmosphere in 75 minutes. Calculate the rate of reaction (in M sec⁻¹) and rate of reaction in term of pressure.

Q.6 For the elementary reaction $2A + B_2 \rightarrow 2AB$. Calculate how much the rate of reaction will change if the volume of the vessel is reduced to one third of its original volume?

Q.7 For the reaction $3BrO^- \rightarrow BrO_3^- + 2Br^-$ in an alkaline aqueous solution the value of the second order (in BrO⁻) rate constant at 80°C in the rate law for

$-\dfrac{\Delta[BrO^-]}{\Delta t}$ was found to be 0.056L mol⁻¹ s⁻¹. What is the rate constant when the rate law is written for

(a) $\dfrac{\Delta[BrO_3^-]}{\Delta t}$ (b) $\dfrac{\Delta[Br^-]}{\Delta t}$?

Q.8 Dinitropentoxide decomposes as follows:

$N_2O_5(g) \rightarrow 2NO_2(g) + \dfrac{1}{2}O_2(g)$
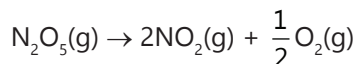
Given that $- d\,[N_2O_5]/dt = k_1[N_2O_5]$

$d[NO_2]/dt = k_2[N_2O_5]$; $d[O_2]/dt = k_3[N_2O_5]$

What is the relation between k_1, k_2 and k_3?

Q.9 Suppose that the Sun consist entirely of hydrogen atom and releases the energy by the nuclear reaction.

$4^1_1H \longrightarrow ^4_2He$ with 26 MeV of energy released. If the total output power of the Sun is assumed to remain constant at 3.9×10^{26} W find the time it will take to burn all the hydrogen. Take the mass of the Sun as 1.7×10^{30} kg.

Q.10 The reaction A(g) + 2B(g) → C(g) + D(g) is an elementary process. In an experiment, the initial partial pressure of A & B are $P_A = 0.6$ and $P_B = 0.8$ atm. Calculate the ratio of rate of reaction relative to initial rate when P_C becomes 0.2 atm.

Q.11 In the given reaction, A → B rate constant is 1.2×10^{-2} M s^{-1}. What is concentration of B after 10 and 20 min, if we start with 10 M of A.

Q.12 For the following data for the zero order reaction A → products. Calculate the value of k.

Time(min)	[A]
0.0	0.10 M
1.0	0.09 M
2.0	0.08 M

Q.13 The rate constant for a zero order reaction is 2×10^{-2} mol/L sec^{-1}, if the concentration of the reactant after 25 sec is 0.25 M, calculate the initial concentration.

Q.14 A drop of solution (volume 0.10 ml) contains 6×10^{-6} mole of H^+, if the rate constant of disappearance of H^+ is 1×10^7 mole liter^{-1} sec^{-1}. How long would it take for H^+ in drop to disappear?

Q.15 A certain substance A is mixed with an equimolar quantity of substance B. At the end of an hour A is 75% reacted Calculate the time when A is 10% unreacted. (Given: order of reaction is zero)

Q.16 A first order reaction is 75% completed in 72 min. How much time will it take for (i) 50% completion (ii) 87.5% completion.

Q.17 A first order reaction is 20% complete in 10 min. Calculate (i) the specific rate constant. (ii) the time taken for the reactions to go to 75% completion.

Q.18 Show that in case of unimolecular reaction, the time required for 99.9% of the reaction to take place in ten times that required for half of the reaction.

Q.19 A first order reaction has a rate constant is 1.5×10^{-3} sec^{-1}. How long will 5.0 g of this reactant take to reduce to 1.25 g?

Q.20 A drug is known to be ineffective after it has decomposed 30%. The original concentration of a sample was 500 units/ml. When analyzed 20 months later, the concentration was found to be 420units/ml. Assuming that decomposition is of first order, what will be the expiry time of the drug?

Q.21 A viral preparation was inactivated in a chemical bath. The inactivation process was found to be first order in virus concentration. At the beginning of the experiment 2.0% of the virus was found to be inactivated per minute. Evaluate k for inactivation process.

Q.22 If a reaction A → Products, the concentrations of reactant A are C_0, aC_0, a^2C_0, a^3C_0 ....after time interval 0, t, 2t, 3t,........... where a is a constant. Given 0 < a < 1. Show that the reaction is of first order. Also calculate the relation between k,a and t.

Q.23 The reaction $SO_2Cl_2(g)$ → $SO_2(g)$ + $Cl_2(g)$ is a first order gas reaction with k = 2.2×10^{-5} sec^{-1} at 320°C. What % of SO_2Cl_2 is decomposed on heating this gas for 90 min?

Q.24 Two substances A($t_{1/2}$ = 5 mins) and B($t_{1/2}$ = 15 mins) follow first order kinetics are taken in such a way that initially [A]= 4 [B]. Calculate the time after which the concentration of both the substance will be equal.

Q.25 At 800° C the rate of reaction

$2NO + H_2 → N_2 + H_2O$
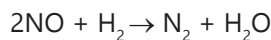
Changes with the concentration of NO and H_2 are

	[NO] in M	[H_2] in M	$-\dfrac{1}{2}\dfrac{d[NO]}{dt}$ in M sec^{-1}
(i)	1.5×10^{-4}	4×10^{-3}	4.4×10^{-4}
(ii)	1.5×10^{-4}	2×10^{-3}	2.2×10^{-4}
(iii)	3.0×10^{-4}	2×10^{-3}	8.8×10^{-4}

(a) What is the order of this reaction?

(b) What is the rate equation for the reaction?

(c) What is the rate when

[H_2] = 1.5×1^{-3} M and [NO] = 1.1×1^{-3}M?

Q.26 The data below are for the reaction if NO and Cl_2 to form NOCl at 295 K

Concentration of Cl_2 [M]	Concentration of NO	Initial Rate $(M\ s^{-1})$
0.05	0.05	1×10^{-3}
0.15	0.05	3×10^{-3}
0.05	0.15	9×10^{-3}

(a) What is the order w. r.t. NO and Cl_2 in the reaction.

(b) Write the rate expression

(c) Calculate the rate constant

(d) Determine the reaction rate when concentration of Cl_2 and NO are 0.2 M & 0.4 M respectively.

Q.27 The catalytic decomposition of N_2O by gold at 900 °C and at an initial pressure of 200 mm is 50% complete in 53 minutes and 73% complete in 100 minutes

(i) What is the order of the reaction?

(ii) Calculate the velocity constant

(iii) How much of H_2O will decompose in 100 min. at the same temperature but at initial pressure of 600 mm?

Q.28 The pressure of a gas decomposing at the surface of a solid catalyst has been measured at different times and the results are given below

t (sec)	0	100	200	300
Pa(Pascal)	4×10^3	3.5×10^3	3×10^3	2.5×10^3

Determine the order of reaction, its rate constant.

Q.29 The half -life period of decomposition of a compound is 50 minutes. If the initial concentration is halved, the half life period is reduced to 25 minutes. What is the order of reaction?

Q.30 In this case we have A → B + C

Time	t	∞
Total pressure of A + B +C	P_2	P_3

Find k.

Q.31 A → B + C

Time	t	∞
Total pressure of (B +C)	P_2	P_3

Find k.

Q.32 A → B + C

Time	0	t
Volume of reagent	V_1	V_2

The reagent reacts with A, B and C. Find k.

[Assuming n-factor of A B & C are same]

Q.33 A → 2B + 3C

Time	t	∞
Volume of reagent	V_2	V_3

The reagent reacts with A, B and C.

Find k. [Assuming n-factor of A B & C are same]

Q.34 S → G + F

Time	t	∞
Rotation of Glucose & Fructose	r_1	r_∞

Find k.

Q.35 The reaction $AsH_3(g) \rightarrow As(s) + \dfrac{3}{2}H_2(g)$ was followed at constant volume at 310°C by measuring the gas pressure at intervals. Show from the following figures that reaction is of first order.

Time (in hrs)	0	5	7.5	10
Total pressure (in min)	758	827	856	882

Q.36 The thermal decomposition of dimethyl ether as measured by finding the increase in pressure of the reaction.

$(CH_3)_2O(g) \rightarrow CH_4(g) + H_2(g) + CO(g)$ at 500°C is as follow:

Time (sec.)	390	1195	3155	∞
Pressure increase (mm Hg)	96	250	467	619

The initial pressure of ether was 312 mm Hg. Write the rate equation for this reaction and determine the rate constant.

Q.37 From the following data show that decomposition of H_2O_2 in aqueous media is first order.

Time in (minutes)	0	10	20
Volume (in c.c. of $KMnO_4$)	22.8	13.3	8.25

Q.38 The following data were obtained in experiment on inversion of cane sugar

Time (minute)	0	60	120	1805	360	∞
Angle of rotation (degree)	+13.1	+11.6	+10.2	+9.0	+5.87	−3.8

Show that the reaction is of first order. After what time would you expect a zero reading in polarimeter?

Q.39 At 100°C the gaseous reaction A → 2B + C was observed to be of first order. On starting with pure A it is found that at the end of 10 minutes the total pressure of system is 176 mm Hg and after a long time 270 mm Hg. From these data find (a) initial pressure of A (b) the pressure of A at the end of 10 minutes (c) the specific rate of reaction(d) the half-life period of the reaction?

Q.40 The decomposition of N_2O_5 according to the equation $2N_2O_5$ (g) → 4 NO_2(g) + O_2(g) is a first order reaction. After 30 min, from start of decomposition in a closed vessel the total pressure developed is found to be 284.5 mm Hg. On complete decomposition, the total pressure is 584.5 mm Hg. Calculate the rate constant of the reaction.

Q.41 A definite volume of H_2O_2 undergoing spontaneous decomposition required 22.8 c.c. of standard permanganate solution for titration. After 10 and 20 minutes respectively the volumes of permanganate required were 13.8 and 8.25 c.c.

(a) Find order of reaction. How may the result be explained?

(b) Calculate the time required for the decomposition to be half completed.

(c) Calculate the fraction of H_2O_2 decomposed after 25 minutes.

Q.42 Hydrogen peroxide solution was stored in a mild steel vessel. It was found, however, that the hydrogen peroxide decomposed on the wall of the vessel (a first order reaction) .An experiment with 100 ml of a solution gave 10.31 ml oxygen (corrected to 1 atm & 273 K) after 5.1 days. Find how long the peroxide can be stored before the loss of 20.00 ml oxygen occurs (per 100 ml solution) under similar storage conditions if complete decomposition of the H_2O_2 sample gave 46.34 mL oxygen.

Q.43 The reaction A(aq) → B (aq) + C (aq) is monitored by measuring optical rotation of reaction mixture as different time interval .The species A, B and C are optically active with specific rotations 20°, 30° and − 40° respectively. Starting with pure A if the value of optical rotation was found to be 2.5° after 6.93 minutes and optical rotation was −5° after infinite time. Find the rate constant for first order conversion of A into B and C.

Q.44 For a reaction

$$x \overset{k_1}{\underset{k_2}{\nearrow\searrow}} \begin{matrix} y \\ z_t \end{matrix}$$
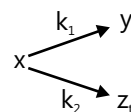
Calculate value of ratio, $\dfrac{[x]_t}{[y]+[z]}$ at any given instant.

Q.45

$$A \overset{k_1}{\underset{k_2}{\nearrow\searrow}} \begin{matrix} B \\ C \end{matrix}$$
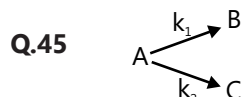
k_1 = x hr^{-1}; $k_{1:}$ k_2 = 1: 10. Calculate $\dfrac{[C]}{[A]}$ after one hour from the start of the reaction. Assuming only A was present in the beginning.

Q.46 How much time would be required for B to reach maximum concentration for the reaction A $\overset{k_1}{\longrightarrow}$ B $\overset{k_2}{\longrightarrow}$ C.

Given $k_1 = \dfrac{\ln 2}{4}$ $k_2 = \dfrac{\ln 2}{2}$

Q.47 For first order parallel reaction k_1 and k_2 are 8 and 2 min^{-1} respectively at 300 K. If the activation energies for the formation of B and C are respectively 20 and 28.314 kJ/ mol respectively find the temperature at which B and C will be obtained in molar ratio of 2:1.

$$A \overset{k_1}{\underset{k_2}{\nearrow\searrow}} \begin{matrix} B \\ C \end{matrix}$$
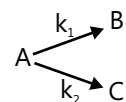
[Given: ln4 = 1.4]

Q.48 In gaseous reactions important for understanding the upper atmosphere, H_2O and O react bimolecularly to form two OH radicals. ΔH for This reaction is 72 kJ at 500 K and E_a = 77 kJ mol^{-1}, then calculate E_a for the bimolecular recombination of 2OH radicals to form H_2O and O at 500 K.

Q.49 The energy of activation of a first order reaction is 104.5 kJ mole^{-1} and pre - exponential factor (A) is 5×10^{11} sec^{-1}. At what temperature, will the reaction have a half-life of 1 minute?

Q.50 The specific rate constant for a reaction increases by a factor of 4. If the temperature is changed from 27°C to 47°C. Find the activation energy for the reaction.

Q.51 The energy of activation and specific rate constant for a first order reaction at 25°C are 100 kJ/mole and 3.46×10^{-3} sec^{-1} respectively. Determine the temperature at which half life of the reaction is 2 hours.

Q.52 A catalyst lowers the activation energy for a certain reaction from 75 kJ to 25 kJ mol^{-1}. What will be the effect on the rate of reaction at 25°C after things being equal?

Q.53 Given that the temperature coefficient for the saponification of ethyl acetate by NaOH is 1.75. Calculate activation energy for the saponification of ethyl acetate.

Q.54 At 380°C the half-life period for the first order decomposition of H_2O_2 is 360 min. The energy of activation of the reaction is 200 kJ mol^{-1}. Calculate the time required for 75% decomposition at 450°C.

Q.55 The reaction $2NO + Br_2 \rightarrow 2NOBr$, is supposed to follow the following mechanism

(i) $NO + Br_2 \xrightleftharpoons{\text{fast}} NOBr_2$

(ii) $NOBr_2 + NO \xrightarrow{\text{slow}} 2NOBr$
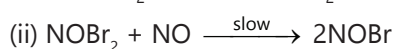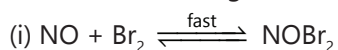
Suggest the rate law expression.

Q.56 For the reaction $2H_2 + 2NO \rightarrow N_2 + 2H_2O$, the following mechanism has been suggested $2NO \rightarrow N_2O_2$ equilibrium constant K_1 (fast)
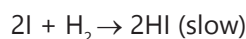
$N_2O_2 + H_2 \xrightarrow{k_2} N_2O + H_2O$ (slow)

$N_2O + H_2 \xrightarrow{k_3} H_2 + H_2O$ (fast)
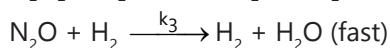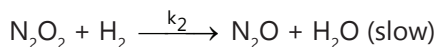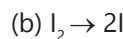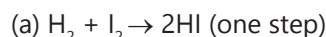
Establish the rate law for given reaction.

Q.57 Reaction between NO and O_2 to form NO_2 is $2NO + O_2 \rightarrow 2NO_2$ follows the following mechanism

$NO + NO \xrightleftharpoons[k_{-1}]{K_1} N_2O_2$ (in rapid equilibrium)

$N_2O_2 + O_2 \xrightarrow{k_2} 2NO_2$ (slow)
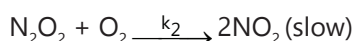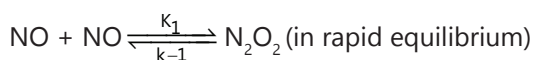
Show that the rate of reaction is given by $\frac{1}{2}\left(\frac{d[NO_2]}{dt}\right)$ = K $[NO]^2[O_2]$

Q.58 Deduce rate law expressions for the conversion of H_2 and I_2 to HI at 400°C corresponding to each of the following mechanisms:

(a) $H_2 + I_2 \rightarrow 2HI$ (one step)

(b) $I_2 \rightarrow 2I$

$2I + H_2 \rightarrow 2HI$ (slow)

(c) $I_2 \rightarrow 2I$

$I + H_2 \rightarrow IH_2$

$IH_2 + I \rightarrow 2HI$ (slow)
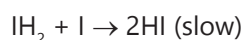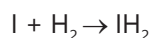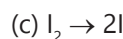
(d) Can the observed rate law expression

rate = $k[H_2][I_2]$ distinguish among these mechanisms?

(e) If it is known that ultraviolet light causes the reaction of H_2 and I_2 to proceed at 200°C with the same rate law expression, which of these mechanisms becomes most improbable?
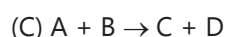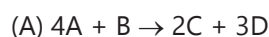
Exercise 2

Single Correct Choice Type

Q.1 The rate of a reaction is expressed in different ways as follows:

$$+\frac{1}{2}\left(\frac{d[C]}{dt}\right)=-\frac{1}{3}\left(\frac{d[D]}{dt}\right)=+\frac{1}{4}\left(\frac{d[A]}{dt}\right)=-\left(\frac{d[B]}{dt}\right)$$

The reaction is:

(A) $4A + B \rightarrow 2C + 3D$

(B) $B + 3D \rightarrow 4A + 2C$

(C) $A + B \rightarrow C + D$

(D) $B + D \rightarrow A + C$

Q.2 For the reaction system

$2NO$ (g) + O_2 (g) $\rightarrow$ $2NO_2$(g) volume is suddenly reduced to half of its value by increasing the pressure on it. If the reaction is first order with respect to O_2 and second order with respect to NO the reaction rate will

(A) Increase to four times of its initial value

(B) Diminish to one-fourth of its initial value

(C) Diminish to one-eight of its initial value

(D) Increase to eight times of its initial value

Q.3 The energies of activation for forward and reverse reactions for $A_2 + B_2 \rightleftharpoons 2AB$ are 180 kJ mol^{-1} and 200 kJmol^{-1} respectively. The presence of catalyst lower the activation energy of both (forward and reverse)
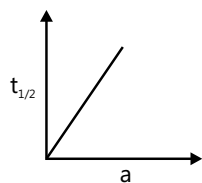
reactions by 100 kJ mol^{-1}. The magnitude of enthalpy change of the reaction (A$_2$ + B$_2$ → 2AB) in the presence of catalyst will be (in kJ mol^{-1}).

(A) 300   (B) 120   (C) 20   (D) –20
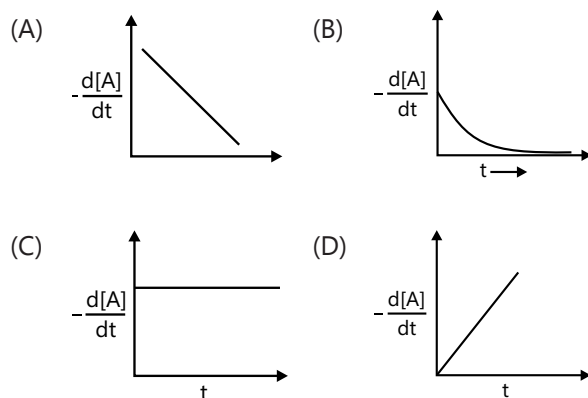
Q.4 Which graph represents zero order reaction

[A(g) → B(g)]

(A)

(B)

(C)

(D)
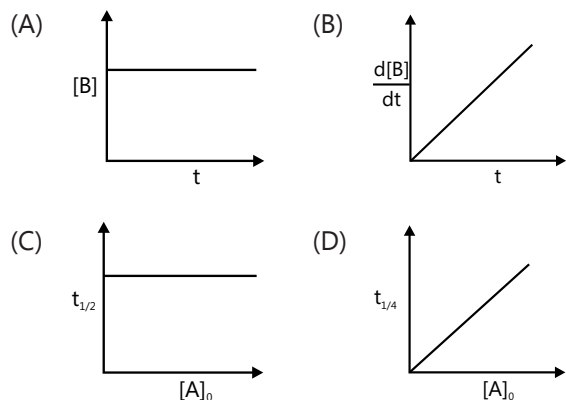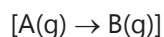
Q.5 Consider the reaction A → B, graph between half-life (t$_{1/2}$) and initial concentration (a) of the reaction is


Hence graph between – $\dfrac{d[A]}{dt}$ and time will be

(A)

(B)

(C)

(D)

Q.6 The reactions of higher order are rare because

(A) Many body collisions involve very high activation energy

(B) Many body collisions have a very low probability

(C) Many body collisions are not energetically favoured

(D) Many body collisions can take place only in the gaseous phase.

Q.7 For the first order decomposition of SO$_2$Cl$_2$(g).

SO$_2$Cl$_2$(g) → SO$_2$(g) + Cl$_2$(g) a graph of log (a$_0$ – x) vs t is shown in figure. What is the rate constant (sec^{-1})?
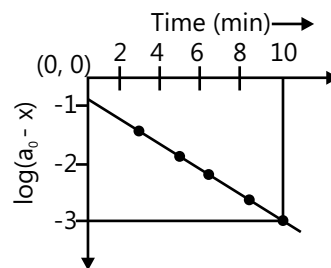
(A) 0.2   (B) 4.6 × 10^{-1}

(C) 7.7 × 10^{-3} (D) 1.15 × 10^{-2}

Q.8 Decomposition of H$_2$O$_2$ is a first order reaction. A solution of H$_2$O$_2$ labelled as "16.8 V" was left open due to this, some H$_2$O$_2$ decomposed. To determine the new volume strength after 2.303 hours. 20 mL of this solution was diluted to 100 mL. 25 mL of this diluted solution was titrated against 37.5 mL of 0.02 M KMnO$_4$ solution under acidic conditions [Given: STP is 1 atm and 273 K].

The rate constant (in hr^{-1}) for decomposition of H$_2$O$_2$ is:

(A) 0.15   (B) 0.30   (C) 0.60   (D) 1.3

Q.9 The variation of concentration of A with time in two experiments starting with two different initial concentration of A is given in the following graph. The reaction is represented as A (aq) → B(aq).

What is the rate of reaction (M/min) when concentration of A in aqueous solution was 1.8 M?
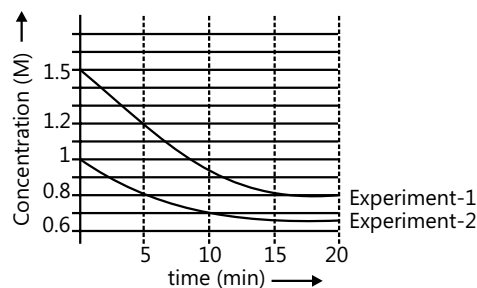
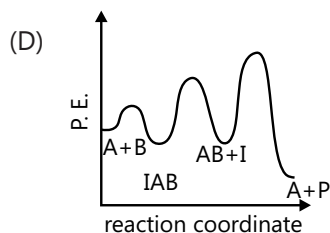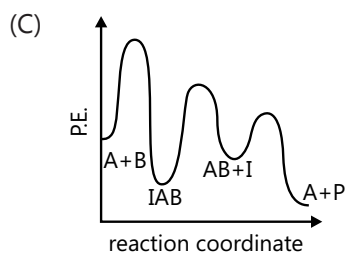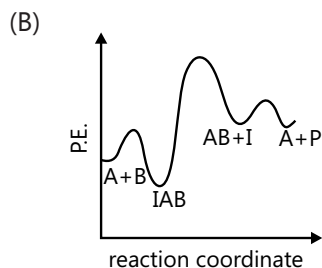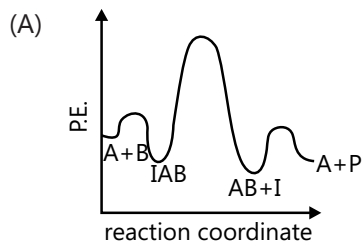(A) 0.08 M min^{-1} (B) 0.036 M min^{-1}

(C) 0.13 M min^{-1} (D) 1 M min^{-1}

Q.10 The following mechanism has been proposed for the exothermic catalyzed complex reaction.

A+B $\xrightleftharpoons{fast}$ IAB $\xrightarrow{k_1}$ AB+I $\xrightarrow{k_2}$ P+A
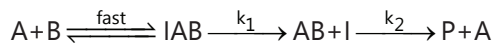
If k$_1$ is much smaller than k$_2$. The most suitable qualitative plot of potential energy (PE.) versus reaction coordinate for the above reaction.
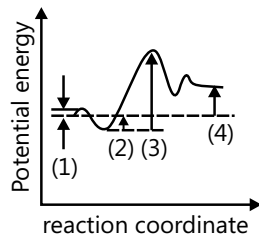
(A)

(B)

(C)

(D)

Q.11 The following mechanism has been proposed for the reaction of NO with Br_2 to form NOBr
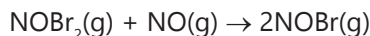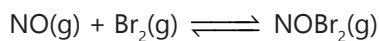
$NO(g) + Br_2(g) \rightleftharpoons NOBr_2(g)$

$NOBr_2(g) + NO(g) \rightarrow 2NOBr(g)$

If the second step is the rate determining step, the order of the reaction with respect to NO(g) is

(A) 2   (B) 1   (C) 0   (D) 3

Q.12 Choose the correct set of indentifications.

	(1)	(2)	(3)	(4)
(A)	ΔE for E+S→ES	E_a for ES→EP	$\Delta E_{overall}$ for S®P	E_a for EP→E+P
(B)	E_a for E+S→ES	ΔE for E+S→ES	E_a for ES→EP	$\Delta E_{overall}$ for S®P
(C)	E_a for ES→EP	E_a for EP→E+P	$\Delta E_{overall}$ for S®P	ΔE for EP→E+P
(D)	E_a for E+S→ES	E_a for ES→EP	E_a for EP→E+P	$\Delta E_{overall}$ for S®P
(E)	ΔE for E+S→ES	$\Delta E_{overall}$ for S®P	ΔE for EP→E+P	E_a for EP→E+P

Multiple Correct Choice Type

Q.13 SO_3 gas is entering the environment at a constant rate of 6.93×10^{-5} gm/L/day due to the emission of polluting gases from thermal power plant but at the same time it is decomposing & following first order kinetics with half-life of 100 days.

Based on above information select the true statement (s).

(A) Concentration of SO_3 in Kota is 1.25×10^{-5} M (Assume SO_3 present in air reaches steady state)

(B) If 10^3 L of air is passed through 1L pure water (assuming all SO_3 to be dissolved in it) & resulting solution is titrated against 1 N NaOH solution, 15 ml is required to reach end point

(C) An industry is manufacturing H_2SO_4 at the rate of 980 kg per day with the use of SO_3 in air it should use 8×10^5 litre air/day

(D) If SO_3 emission is stopped then after 1000 days its concentrations will reduce to $\approx 1.2 \times 10^{-3}$ M.

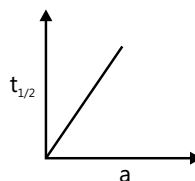**Q.14** For the reaction A → B. The rate law expression is $-\dfrac{d[A]}{dt} = k[A]^{1/2}$. If initial concentration of [A] is $[A]_0$, then

(A) The integrated rate expression is $k = \dfrac{2}{t}(A_0^{1/2} - A^{1/2})$
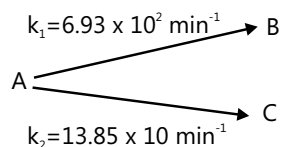
(B) The graph of $\sqrt{A}$ vs t will be

(C) The half-life period $t_{1/2} = \dfrac{K}{2[A]_0^{1/2}}$

(D) The time taken for 75% completion of reaction $t_{3/4} = \dfrac{\sqrt{[A]_0}}{k}$

Q.15 Consider the reaction,

$$A \xrightarrow{k_1 = 6.93 \times 10^2 \text{ min}^{-1}} B$$
$$A \xrightarrow{k_2 = 13.85 \times 10 \text{ min}^{-1}} C$$

A, B and C all are optically active compound. If optical rotation per unit concentration of A, B and C are 60°, –72°, 42° and initial concentration of A is 2 M then select write statements(s).

(A) Solution will be optically active and dextro after very long time

(B) Solution will be optically active and laevo after very long time

(C) Half life of reaction is 15 min

(D) After 75% conversion of A in to B and C angle of rotation of solution will be 36°

Q.16 Which of the following statement is incorrect?

(A) The order of reaction is the sum of powers of all the concentration terms in the rate equation.

(B) The order of reaction with respect to one reactant is the ratio of the change of logarithm of the rate of the reaction to the change in the logarithm of the concentration of the particular reactant, keeping the concentrations of all other reactants constant.

(C) Orders of reactions cannot be fractional.

(D) The order of a reaction can only be determined from the stoichiometric equation for the reaction.

Q.17 Select incorrect statement(s)

(A) Unit of pre-exponential factor (A) for second order reaction is mol L^{-1} s^{-1}

(B) A zero-order reaction must be a complex reaction

(C) Molecularity is defined only for RDS in a complex reaction

(D) Decay constant (λ) of radioactive substance is affected by temperature

Q.18 In a consecutive reaction system A $\xrightarrow{E_1}$ B $\xrightarrow{E_2}$ C when E_1 is much greater than E_2, the yield of B increase with

(A) Increase in temperature

(B) Decreases in temperature

(C) Increase in initial concentration of A

(D) Decrease in initial concentration of A

Q.19 Which of the following is/are correct statement?

(A) Stoichiometry of a reaction tells about the order of the elementary reaction.

(B) For a zero-order reaction, rate and the rate constant are identical

(C) A zero-order reaction is controlled by factors other than concentration of reactants.

(D) A zero-order reaction is always elementary reaction

Assertion Reasoning Type

(A) Statement-I is true, statement-II is true and statement-II is correct explanation for statement-I

(B) Statement-I is true, statement-II is true and statement-II is NOT the correct explanation for statement-I

(C) Statement-I is true, statement-II is false.

(D) Statement-I is false, statement-II is true.

Q.20 Statement-I: A fractional order reaction must be a complex reaction.

Statement-II: Fractional order of RDS equals to overall order of a complex reaction.

Q.21 Statement-I: Temperature coefficient of a one step reaction may be negative

Statement-II: The rate of reaction having negative order with respect to a reactant decreases with the increase in concentration of the reactant.

Q.22 Statement-I: The overall rate of a reversible reaction may decrease with the increase in temperature.

Statement-II: When the activation energy of forward reaction is less than that of backward reaction, then the increase in the rate of backward reaction is more than that of forward reaction on increasing the temperature

Q.23 Statement-I: In a reversible endothermic reaction E_a of forward reaction is higher than that of backward reaction.

Statement-II: The threshold energy of forward reaction is more than that of backward reaction.

Q.24 Statement-I: The time of completion of reaction of type A → product

(order < 1) may be determined.

Statement-II: Reactions with order $\geq$ 1 are either too slow or too fast and hence the time of completion cannot be determined

Q.25 Statement-I: A catalyst provides an alternative path to the reaction in which conversion of reaction into products takes place quickly

Statement-II: The catalyst forms an activated complex of lower potential energy with the reactants by which more number of molecules are able to cross the barrier per unit of time.

Comprehension Type

Paragraph 1

For a hypothetical elementary reaction $A \overset{k_1}{\underset{k_2}{\longrightarrow}} \overset{B}{\underset{C}{}}$

where $\dfrac{k_1}{k_2} = \dfrac{1}{2}$. Initially only 2 moles of A is present.

Q.26 The total number of moles of A, B & C at the end of 50% reaction are

(A) 2　　　(B) 3　　　(C) 4　　　(D) 5

Q.27 Number of moles of B are

(A) 2　　　(B) 1　　　(C) 0.666　　　(D) 0.33

Paragraph 2

The gaseous reaction: $n_1 A(g) \rightarrow n_2 B (g)$ is first order with respect to A. The true rate constant of reaction is k. The reaction is studied at a constant pressure and temperature. Initially, the moles of A were 'a' and no B were present.

Q.28 How many moles of A are present at time, t?

(A) $a \cdot e^{-kt}$　　　　　(B) $a \cdot e^{-n_1 kt}$

(C) $a \cdot e^{-n_2 kt}$　　　　　(D) $a(1 - e^{-n_2 kt})$

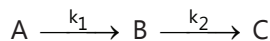**Q.29** If the initial volume of system were v_0, then the volume of system after time t will be

(A) $\dfrac{n_1 v_0}{n_2}$

(B) $\dfrac{n_2 v_0}{n_1}$

(C) $v_0 \left[\dfrac{n_2}{n_1} + \left(1 - \dfrac{n_2}{n_1} \right) \cdot e^{-n_1 kt} \right]$

(D) $v_0 \left[\dfrac{n_2}{n_1} + \left(\dfrac{n_2}{n_1} - 1 \right) \cdot e^{-n_2 kt} \right]$

Q.30 What will be the concentration of A at time t, if $n_1 = 1$ and $n_2 = 2$?

(A) $[A_0] \cdot e^{-kt}$

(B) $[A_0] \left(\dfrac{e^{-kt}}{2 - e^{-kt}} \right)$

(C) $[A_0] \left(\dfrac{e^{-kt}}{1 - e^{-kt}} \right)$

(D) $[A_0](1 - 2 \cdot e^{-kt})$

Paragraph 3

For the reaction sequential reaction

$A \xrightarrow{k_1} B \xrightarrow{k_2} C$

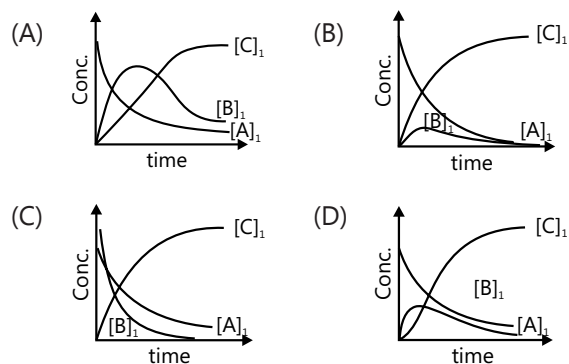the concentration of A, B & C at anytime 't' is given by

$[A]_t = [A]_0 e^{-kt}$; $[B]_t = \dfrac{k_1 [A]_0}{(k_2 - k_1)} [e^{-k_1 t} - e^{-k_2 t}]$

$[C]_t = [A]_0 - ([A]_t + [B]_t)$

Q.31 The time at which concentration of B is maximum is

(A) $\dfrac{k_1}{k_2 - k_1}$

(B) $\dfrac{1}{k_2 - k_1} \ln \dfrac{k_1}{k_2}$

(C) $\dfrac{1}{k_1 - k_2} \ln \dfrac{k_1}{k_2}$

(D) $\dfrac{k_2}{k_2 - k_1}$

Q.32 Select the correct option if $k_1 = 1000 s^{-1}$ and $k_2 = 20 s^{-1}$.
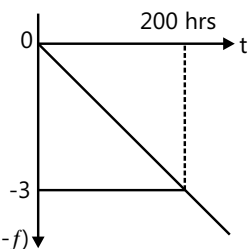

Paragraph 4

Oxidation of metals is generally a slow electrochemical reaction involving many steps. These steps involve electron transfer reactions. A particular type of oxidation involve overall first order kinetics with respect to fraction of unoxidised metal $(1 - f)$ surface thickness relative to maximum thickness (T) of oxidised surface, when metal surface is exposed to air for considerable period of time

Rate law: $= k(1 - f)$, where $f = x/T$,

x = thickness of oxide film at time 't' and

T = thickness of oxide film at t = ∞

A graph of ln(1 − f) vs t is shown inthe adjacent figure.

Q.33 The time taken for thickness to grow 50% of T is
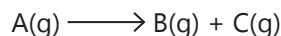
(A) 23.1 hrs   (B) 46.2hrs

(C) 100 hrs   (D) 92.4 hrs

Q.34 The exponential variation of 'f' with t(hrs) is given by

(A) $[1 − e^{-3t/200}]$ (B) $e^{-3t/200−1}$

(C) $e^{-3t/200}$ (D) $e^{3t/200}$

Paragraph 5

A reaction is said to be first order if it's rate is proportional to the concentration of reactant. Let us consider a reaction

$$A(g) \longrightarrow B(g) + C(g)$$

At t = 0   a   0   0

At time t   a - x   x   x

The rate of reaction is govern by the expression $\frac{dx}{dt}$ = k(a − x) and integrated rate equation for a given reaction is represented as

$k = \frac{1}{t} \ln\left(\frac{a}{a−x}\right)$ where a = initial concentration and

(a − x) = concentration of A after time t.

Q.35 Thermal decomposition of compound X is a first order reaction .If 75% of X is decomposed in 100 min. How long will it take for 90% of the compound to decompose? Given: log 2 = 0.30

(A) 190 min   (B) 176.66 min

(C) 166.66 min   (D) 156.66 min

Q.36 Consider a reaction A(g) $\longrightarrow$ 3B(g) + 2C(g) with rate constant 1.386×10^{-2} min^{-1}. Starting with 2 moles of A in 12.5 litre vessel initially, if reaction is allowed to takes place at constant pressure & at 298 K then find the concentration of B after 100 min.

(A) 0.04 M   (B) 0.36 M
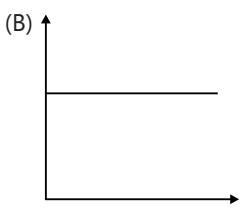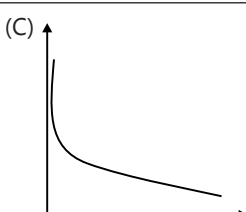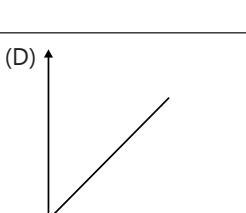
(C) 0.09 M   (D) None of these

Match the Columns

Q.37 For the reaction of type A(g) → 2B(g)

Column I contains four entries and column II contains four entries. Entry of column I are to be matched with only one entry of column II

Column I	Column II
(A) $\frac{d[B]}{dt}$ vs $\frac{−d[A]}{dt}$ for first order	(p)
(B) [A] vs t for first order	(q)
(C) [B] vs t for first order	(r)
(D) [A] vs t for zero order	(s)

Q.38 Column-I and column-II. Entry of column-I are to be matched with one or more than one entries of column-II and vice versa.

Column-I (Graphs reaction A → Products)	Column-II (Co-ordinates)
(A)	(p) ln [A] (y-axis), t(x-axis) (order = 1)

(B)	(q) $t_{1/2}$(y-axis), $[A_0]$ (x-axis) (order = 1)
(C)	(r) r(y-axis), t(x-axis)(order > 0)
(D)	(s) r(y-axis), t(x-axis)(order = 0)
	(t) $t_{1/2}$(y-axis), $[A_0]$ (x-axis) (order > 1)
	(u) $\dfrac{1}{[A]}$ (y-axis), t(x-axis) (order = 2)
	(v) r(y-axis), [A](x-axis)(order = 1)

Previous Years' Questions

Q.1 The rate constant of a reaction depends on *(1981)*

(A) Temperature

(B) Initial concentration of the reactants

(C) Time of reaction

(D) Extent of reaction

Q.2 A catalyst is a substance which *(1983)*

(A) Increases the equilibrium concentration of the product

(B) Changes the equilibrium constant of the reaction

(C) Shortens the time to reach equilibrium

(D) Supplies energy to the reaction

**Q.3** If I is the intensity of absorbed light and C is the concentration of AB for the photochemical process.

AB + hv → AB*, the rate of formation of AB* is directly proportional to *(2001)*

(A) C   (B) I   (C) I^2 (D) C.I

**Q.4** Which one of the following statements is incorrect about order of reaction? *(2005)*

(A) Order of reaction is determined experimentally

(B) Order of reaction is equal to sum of the power of concentration terms in differential rate law

(C) It is not affected with stoichiometric coefficient of the reactants

(D) Order cannot be fractional

Q.5 Plots showing the variation of the rate constant (k) with temperature (T) are given below. The plot that follows Arrhenius equation is *(2010)*

(A)   (B)

(C)   (D)
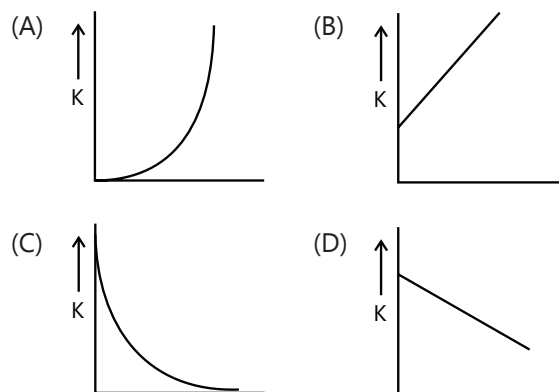
Comprehension (Q.6), (Q. 7), (Q.8)

Carbon-14 is used to determine the age of organic material. The procedure is based on the formation of ^{14}C by neutron capture in the upper atmosphere.

$$^{14}_{7}N +\, ^{1}_{0}n \longrightarrow\, ^{14}_{6}C +\, ^{1}_{1}p$$
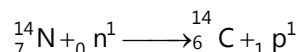
^{14}C is absorbed by living organisms during photosynthesis. The ^{14}C content is constant in living organism once the plant or animal dies, the uptake of carbon dioxide by it ceases and the level of ^{14}C in the dead being, falls due to the decay which C–14 undergoes $^{14}_{6}C \longrightarrow\, ^{14}_{7}N + \beta^{-}$

The half-life period of ^{14}C is 5770 yr.

The decay constant (λ) can be calculated by using the following formula

$$\lambda = \frac{0.693}{t_{1/2}}$$

The comparison of the β^{-} activity of the dead matter with that of the carbon still in circulation enables measurement of the period of the isolation of the material from the living cycle. The method however, ceases to be accurate over periods longer than 30,000 yr. The proportion of ^{14}C to ^{12}C in living matter is

$1 : 10^{12}$. *(2006)*

Q.6 Which of the following option is correct?

(A) In living organisms, circulation of ^{14}C from atmosphere is high so the carbon content is constant in organism

(B) Carbon dating can be used to find out the age of earth crust and rocks

(C) Radioactive absorption due to cosmic radiation is equal to the rate of radioactive decay, hence the carbon content remains constant in living organisms

(D) Carbon dating cannot be used to determine concentration of ^{14}C in dead beings.

Q.7 What should be the age of fossil for meaningful determination of its age?

(A) 6 yr

(B) 6000 yr

(C) 60,000 yr

(D) It can be used to calculate any age

Q.8 A nuclear explosion has taken place leading to increase in concentration of C^{14} in nearby areas. C^{14} concentration is C_1 in nearby areas and C_2 in areas far away. If the age of the fossil is determined to be T_1 and T_2 at the places respectively then

(A) The age of fossil will increase at the place where explosion has taken place and $T_1 - T_2 = \frac{1}{\lambda} \ln \frac{C_1}{C_2}$

(B) The age of fossil will decrease at the place where explosion has taken place and $T_1 - T_2 = \frac{1}{\lambda} \ln \frac{C_1}{C_2}$

(C) The age of fossil will be determined to be the same

(D) $\frac{T_1}{T_2} = \frac{C_1}{C_2}$

Q.9 The concentration of R in the reaction

R → P was measured as a function of time and the following data obtained:

[R] (molar)	1.0	0.75	0.40	0.10
t (min)	0.0	0.05	0.12	0.18

The order of the reaction is **(2010)**

Q.10 Radioactive decay is a first order process. Radioactive carbon in wood sample decays with a half-life of 5770 yr. What is the rate constant (in yr^{-1}) for the decay? What fraction would remain after 11540 yr? **(1984)**

Q.11 A first order gas reaction has $A' = 1.5 \times 10^{-6}$ per second at 200° C. If the reaction is allowed to run for 10 h, what percentage of the initial concentration would have change in the product? What is the half-life of this reaction? **(1987)**

Q.12 An experiment requires minimum beta activity produced at the rate of 346 beta particles per minute. The half-life period of $_{42}Mo^{99}$ which is a beta emitter is 66.6 h. Find the minimum amount of $_{42}Mo^{99}$ required to carry out the experiment in 6.909 h. **(1989)**

Q.13 The gas phase decomposition of dimethyl ether follows first order kinetics

$$CH_3-O-CH_3(g) \rightarrow CH_4(g) + H_2(g) + CO(g)$$

The reaction is carried out in a constant volume container at 500°C and has a half-life of 14.5 min. Initially only dimethyl ether is present at a pressure of 0.40 atm. What is the total pressure of the system after 12 min? Assume ideal gas behaviour. **(1993)**

Q.14 (a) The rate constant of a reaction is $1.5 \times 10^7 s^{-1}$ at 50° C and $4.5 \times 10^7 s^{-1}$ at 100°C. Evaluate the Arrhenius parameters A and E_a. **(1998)**

(b) For the reaction, N_2O_5 (g) → $2NO_2$ (g) + $\frac{1}{2}O_2$ (g)

calculate the mole fraction $N_2O_5(g)$ decomposed at a constant volume and temperature, if the initial pressure is 600 mm Hg and the pressure at any time is 960 mm Hg. Assume ideal gas behaviour.

Q.15 $2X(g) \rightarrow 3Y(g) + 2Z(g)$

Time (in min)	0	100	200
Partial pressure of X (in mm of Hg)	800	400	200

Assuming ideal gas condition. Calculate **(2005)**

(A) Order of reaction

(B) Rate constant

(C) Time taken for 75% completion of reaction.

(D) Total pressure when $p_x = 700$ mm

Q.16 Consider a reaction aG + bH ⟶ Products. When concentration of both the reactants G and H is doubled, the rate increases by eight times. However, when concentration of G is doubled keeping the concentration of H fixed, the rate is doubled. The overall order of the reaction is **(2007)**

(A) 0   (B) 1   (C) 2   (D) 3

Q.17 Under the same reaction conditions, initial concentration of 1.386 mol dm⁻³ of a substance becomes half in 40 seconds and 20 seconds through first order and zero order kinetics, respectively. Ratio 1 $\left(\dfrac{k_1}{k_0}\right)$ of the rate constants for first order (k_1) and zero order (k_0) of the reactions is *(2008)*

(A) 0.5 mol⁻¹ dm³   (B) 1.0 mol dm⁻³

(C) 1.5 mol dm⁻³   (D) 2.0 mol⁻¹ dm³

Q.18 An organic compound undergoes first-order decomposition. The time taken for its decomposition to 1/8 and 1/10 of its initial concentration are $t_{1/8}$ and $t_{1/10}$ respectively. What is the value of $\dfrac{[t_{1/8}]}{[t_{1/10}]}\times 10$? (take $\log_{10}2=0.3$) *(2013)*

Q.19 In the reaction, $P+Q\longrightarrow R+S$ the time taken for 75% reaction of P is twice the time taken for 50% reaction of P. The concentration of Q varies with reaction time as shown in the figure. The overall order of the reaction is *(2013)*
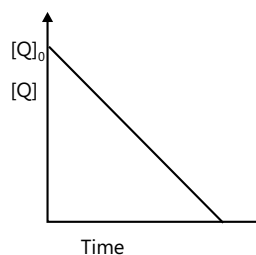
(A) 2   (B) 3   (C) 0   (D) 1

Q.20 For the elementary reaction M $\longrightarrow$ N, the rate of disappearance of M increases by a factor of 8 upon doubling the concentration of M. The order of the reaction with respect to M is *(2014)*

(A) 4   (B) 3   (C) 2   (D) 1

Q.21 According to the Arrhenius equation, *(2015)*

(A) A high activation energy usually implies a fast reaction

(B) Rate constant increases with increase in temperature. This is due to a greater number of collisions whose energy exceeds the activation energy

(C) Higher the magnitude of activation energy, stronger is the temperature dependence of the rate constant

(D) The pre-exponential factor is a measure of the rate at which collisions occur, irrespective of their energy.

MASTERJEE Essential Questions

JEE Main/Boards

Exercise 1

Q.1	Q.4	Q.7	Q.9
Q.12	Q.19	Q.24	

Exercise 2

Q.2	Q.10	Q.16

Previous Years' Questions

Q.9	Q.14	Q.15

JEE Advanced/Boards

Exercise 1

Q.7	Q.9	Q.20	Q.36
Q.43	Q.58(e)		

Exercise 2

Q.8	Q.12	Q.28	Q.29
Q.33	Q.34	Q.37	

Previous Years' Questions

Q.12	Q.15

Answer Key

JEE Main/Boards

Exercise 1

Q.1 (a) 6.25 ; (b) 14.3; (c) 0 %

Q.2 2×10^{-2} min^{-1}

Q.3 $P_1 = 379.55$ mmHg, $t^{7/n} = 399.96$ min

Q.4 0.0207 min^{-1}

Q.5 k = 0.022 hr^{-1}

Q.6 15.13 week

Q.7 20 min

Q.8 0.26: 1

Q.9 (a) 43.46 kJ mol^{-1} (b) 20.47 hour

Q.10 % decomposition = 67.21 %

Q.11 k = 0 0327 min^{-1}

Q.12 0.537

Q.13 4.83 mins

Q.14 0.0025 m

Q.15 $E_r = 6 \times 10^4$ J; $E_b = 9.3 \times 10^4$ J

Q.16 a = b= 1

Q.17 $E = \dfrac{E_1 k_1 + E_2 k_2}{k_1 + k_2}$

Q.18 (a) $\dfrac{d(D)}{dt} = \dfrac{k_1 k_3 (A)(B)}{k_2 + k_3}$

(b) $E_a = E_{a1} + E_{a3} - E_{a2}$ A $= \dfrac{A_1 A_3}{A_2}$

Q.20 0.0805

Q.21 161 minutes

Q.22 55.33 kJ mole^{-1}

Q.23 Rate = K(A)[13]^2 rate will became 8 times

Q.24 $K_{27} = 3.85 \times 10^{-4}$ sec^{-1}

$K_{47} = 11.55 \times 10^{-4}$ sec^{-1}.

E = 43.78 kJ/mol

Q.25 It is first order kinetics with

k = 8.64×10^{-1}

Q.26 2

Q.27 Ea = 2.2×10^4

A = 5.42×10^{10}

Q.28 (a) = 1×10^{-2} mol l^{-1} s^{-1}

(b) = 5.495×10^{-3} mol^{-1} l^{-1} s^{-1}

Q.29 Rate = 2×10^{-4} mol dm^{-3} min^{-1} x = 18.12%

Q.30 k = 0.02231 min^{-1} t = 62.07 min

Exercise 2

Single Correct Choice Type

Q.1 B	**Q.2** A	**Q.3** A	**Q.4** D	**Q.5** D	**Q.6** D
Q.7 C	**Q.8** B	**Q.9** C	**Q.10** D	**Q.11** D	**Q.12** C
Q.13 C	**Q.14** D	**Q.15** B	**Q.16** A	**Q.17** D	**Q.18** C
Q.19 B	**Q.20** B	**Q.21** C	**Q.22** D		

Previous Years' Questions

Q.1 A	**Q.2** C	**Q.3** C	**Q.4** A	**Q.5** D	**Q.6** C
Q.7 B	**Q.8** C	**Q.9** A	**Q.10** D	**Q.11** A	**Q.12** D
Q.13 D	**Q.14** A	**Q.15** B	**Q.16** B	**Q.17** C	**Q.18** C
Q.19 D	**Q.20** B	**Q.21** B	**Q.22** A	**Q.23** D	**Q.24** A

JEE Advanced/Boards

Exercise 1

Q.1 (i) $r = \dfrac{1}{4}\dfrac{d[NO]}{dt} = 9 \times 10^{-4}$ mol litre^{-1} sec^{-1}

(ii) 36×10^{-4} mol litre^{-1} sec^{-1}

(iii) 54×10^{-4} mol litre^{-1} sec^{-1}

Q.2 (i) 7.2 mol litre^{-1} min^{-1},

(ii) 7.2 mol litre^{-1} min^{-1}

Q.3 (a) 1×10^{-4} mol L^{-1} s^{-1},

(b) 3×10^{-4} mol L^{-1} s^{-1}

Q.4 (i) $\dfrac{dx}{dt} = k\,[A][B]^2$

(ii) Rate increases by 8 times

Q.5 7.23×10^{-6} Ms^{-1}, 0.012 atm min^{-1}

Q.6 Rate increases by 27 times

Q.7 (a) 0.019 mol L^{-1} s^{-1},

(b) 0.037 mol L^{-1} s^{-1}

Q.8 $2k_1 = k_2 = 4k_3$

Q.9 2.72×10^{18} sec

Q.10 1/6

Q.11 (i) 7.2 M, (ii) 10 M

Q.12 K = 0.01 M min^{-1}

Q.13 0.75 M

Q.14 6×10^{-9} sec

Q.15 1.2 hr

Q.16 (i) 36 min (ii) 108 min

Q.17 (i) 0.0223 min^{-1}, (ii) 62.17 min

Q.19 924.362 sec

Q.20 Expiry time = 41 months

Q.21 3.3×10^{-4} s^{-1}

Q.22 $k = \dfrac{2.303}{t}\log\dfrac{1}{a}$

Q.23 11.2%

Q.24 15 min

Q.25 (a) Third order, (b) r = k[NO]^2[H$_2$],

(c) 8.85×10^{-3} M sec^{-1}

Q.26 (a) Order w.r.t. NO = 2 and w.r.t. Cl$_2$ = 1,

(b) r = K[NO]^2[Cl$_2$],

(c) K = 8 L^2 mol^{-2}s^{-1},

(d) Rate = 0.256 mole L^{-1} s^{-1}

Q.27 (i) First order

(ii) k = 1.308×10^{-2} min^{-1}

(iii) 73%

Q.28 (i) Zero order, (ii) K = 5 Pa/s

Q.29 Zero order

Q.30 $k = \dfrac{1}{t}\ln\dfrac{P_3}{2(P_3 - P_2)}$

Q.31 $k = \dfrac{1}{t}\ln\dfrac{P_3}{(P_3 - P_2)}$

Q.32 $k = \dfrac{1}{t}\ln\dfrac{V_1}{(2V_1 - V_2)}$

Q.33 $k = \dfrac{1}{t}\ln\dfrac{4V_3}{5(V_3 - V_2)}$

Q.34 $k = \dfrac{1}{t}\ln\dfrac{r_\infty}{(r_\infty - r_1)}$

Q.35 First order

Q.36 (i) r = K[(CH$_3$)$_2$O]$_2$ 0.000428 sec^{-1}

Q.37 First order

Q.38 966 min

Q.39 (a) 90 mm,

(b) 47 mm,

(c) 6.49×10^{-2} per minutes,

(d) 10.677 min.

Q.40 $k_1 = 2.605 \times 10^{-3}$ min^{-1}

Q.41 (a) first order,

(b) 13.75 minutes,

(c) 0.716 0.180 atm, 47.69 sec

Q.42 11.45 days

Q.43 0.1 min^{-1}

Q.44 $\dfrac{1}{e^{(K_1+K_2)t}-1}$

Q.45 $\dfrac{[C]}{[A]}=\dfrac{10}{11}(e^{11x}-1)$

Q.46 t = 4 min

Q.47 0379.75 K

Q.48 5 kJ mol⁻¹

Q.49 349.1 K

Q.50 55.33 kJ mole⁻¹

Q.51 306 K

Q.52 Rate of reaction increases 5.81×10^8 times

Q.53 10.757 k cal mol⁻¹

Q.54 t=20.4 minutes 56. 2000 K

Q.55 r = K′ [NO]² [Br₂]

Q.56 $k = k_2^{'}$

Q.57 r = K[NO]² [H₂], where K=k₂ × K₁/k⁻¹

Q.58 (d) No, (e) mechanism (a) is incorrect

Exercise 2

Single Correct Choice Type

Q.1 B	**Q.2** D	**Q.3** C	**Q.4** D	**Q.5** C	**Q.6** B
Q.7 C	**Q.8** C	**Q.9** A	**Q.10** A	**Q.11** A	**Q.12** B

Multiple Correct Choice Type

Q.13 A, D	**Q.14** A,B,D	**Q.15** A, D	**Q.16** C, D	**Q.17** A, C, D	**Q.18** A, C
Q.19 A, B, C					

Comprehension Type

Q.20 C	**Q.21** D	**Q.22** A	**Q.23** C	**Q.24** C	**Q.25** A
Q.26 B	**Q.27** C	**Q.28** B	**Q.29** D	**Q.30** B	**Q.31 C**
Q.32 C	**Q.33** B	**Q.34** A	**Q.35** C	**Q.36** B	

Match the Columns

Q.37 A → s; B → r; C → p; D → q   **Q.38** A → p; B → q, s; C → r, t; D → v

Previous Years' Questions

Q.1 A	**Q.2** C	**Q.3** D	**Q.4** D	**Q.5** A	**Q.6** A
Q.7 B	**Q.8** A	**Q.9** 0	**Q.10** 0.25	**Q.11** 128.33h	

Q.12 3.56×10^{-16} **Q.13** 0.75 atm   **Q.14** 4.15×10^3 s⁻¹, 0.375

Q.15 (a) 1 (b) 693x10-3 min⁻¹ (c) 200 min (d) 950 mm   **Q.16** D

Q.17 A	**Q.18** 9	**Q.19** D	**Q.20** C	**Q.21** B, C, D

Solutions

JEE Main/Boards

Exercise 1

Sol 1: (a) $A + B \rightarrow C$

We have, first order in A and 0 order in B.

Rate = $\dfrac{-d[A]}{dt}$ = $k[A]^1[B]^0 = \dfrac{-d[A]}{dt} = -k[A]$

For first order reaction, we know

$[A] = [A_0]\, e^{-kt}$

We have, at t = 1 hour

75% of A reacted

$[A] = A_0 - 0.75;\ A = \dfrac{1}{4}A_0$

$\dfrac{1}{4}[A_0] = [A_0]\, e^{-kt} \Rightarrow k = \ln 4$

Now t = 2 hour,

$\dfrac{[A]}{[A_0]} = e^{-2\times\ln 4} = \dfrac{1}{16}$

$[A] = 6.25\ \%$ of A_0

$\therefore 6.25\%$ of A will be left unreacted.

(b) Here, reaction is first order in both A and B

$\therefore \text{Rate} = \dfrac{d[A]}{dt} = k[A][B]$

Since the initial concentration of A and B is the same and they have the same coefficient, their concentration will remain same at any time.

$\dfrac{-d[A]}{dt} = k[A]^2$

$\Rightarrow \displaystyle\int_{[A_0]}^{[A]} \dfrac{d[A]}{[A]^2} = \int_0^t -k\,dt$

$\Rightarrow -\dfrac{1}{[A]} + \dfrac{1}{[A_0]} = -k(t-0) = kt$

At time t = 1 hour, $[A] = \dfrac{[A_0]}{4}$

$\therefore -\dfrac{4}{[A_0]} + \dfrac{1}{[A_0]} = -k$

$\Rightarrow k = \dfrac{3}{[A_0]}$

Now, at time t = 2 hours,

$\dfrac{-1}{[A]} + \dfrac{1}{[A_0]} = -2 \times \dfrac{3}{[A_0]} = \dfrac{-6}{[A_0]}$

$\Rightarrow \dfrac{1}{[A]} = \dfrac{7}{[A_0]} \Rightarrow \dfrac{[A]}{[A_0]} = \dfrac{1}{7}$

A left is $\dfrac{100}{7}\%$ or 14.3 %

(c) If the reaction is 0 order

Rate = $\dfrac{d[A]}{dt} = k$

$\Rightarrow \displaystyle\int_{[A_0]}^{[A]} d[A] = \int_0^t k\,dt$

$\Rightarrow [A] - [A_0] = -kt$

$\Rightarrow [A] = [A_0] - kt$
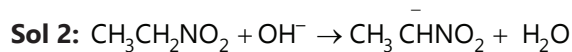
Now, at time t = 1 hour

$[A] = \dfrac{[A_0]}{4}$

$\dfrac{[A_0]}{4} - [A_0] = -k$

$\Rightarrow k = \dfrac{3}{4}[A_0]$

We see that, if t or [A] = 0

$t = \dfrac{[A_0]}{k} = \dfrac{4}{3}$ hours < 2 hours

The reactions will be finished before 2 hours and 6 % of A will be left after 2 hours.

Sol 2: $CH_3CH_2NO_2 + OH^- \rightarrow \underset{(A)}{CH_3\overset{-}{C}HNO_2} + H_2O$

Since this is a first order reaction

$[A] = [A_0]\, e^{-kt}$

Now, we have at time $t = \dfrac{1}{2}$ minute,

$[A] = 0.99[A_0]$

(1 % of nitroethane reacted)
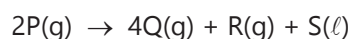
$\therefore 0.99[A_0] = [A_0]\, e^{-k.\,1/2}$

$\Rightarrow \dfrac{-k}{2} = \log_e(0.99)$

$\Rightarrow \dfrac{-k}{2} = 0.01$ min.

$\Rightarrow k = 0.02$ min^{-1}

$k = 2 \times 10^{-2}$ min^{-1}

Sol 3: Here, since the volume of liquid is negligible and as the liquid begins to form, pressure due to liquid will always be equal to 32.5 mm Hg. Now, let initial pressure of P(g) be P_0 mm Hg, then according to stoichiometry

$$2P(g) \rightarrow 4Q(g) + R(g) + S(\ell)$$

at time

t = 0 min	P_0	0	0	0
t = 30 min	$P_0 - 2x$	4x	x	32.5
t = ∞	0	$2P_0$	$\dfrac{P_0}{2}$	32.5

Now, we are given, $P_t = 317$ mm Hg at t=30 min.

$\therefore P_0 - 2x + 4x + x + 32.5 = 317$

$\Rightarrow P_0 + 3x = 284.5$ ....(i)

At time, t = ∞ (very long time), $P_t = 617$ mm Hg

$\therefore 2P_0 + \dfrac{P_0}{2} + 32.5 = 617$

$\Rightarrow \dfrac{5P_0}{2} = 584.5$

$\Rightarrow P_0 = 233.8$ mm Hg

Putting this in (i), we get,

$3x = 284.5 - 233.8$

$\Rightarrow x = 16.9$

Now, since this is first order reaction, we have

at t = 30 min   a = 233.8   x = 16.9

$k = \dfrac{2.303}{t}\log\dfrac{P_0}{P_p} = \dfrac{2.303}{30}\log\dfrac{233.8}{233.8 - (2\times16.9)}$

$\Rightarrow k = 5.2 \times 10^{-3}$ min^{-1}

Now, at t = 75 min, we have

$k = \dfrac{2.303}{t}\log\dfrac{P_0}{P_p}$

$\Rightarrow P_t = P_0 \times 10^{-kt/2.303}$

$= 233.8 \times 10^{\frac{-5.2\times10^{-3}\times75}{2.303}}$

$P_t = 158.22$ m Hg

$\Rightarrow P_0 - 2x = 158.22$

$\Rightarrow x = \dfrac{233.8 - 158.22}{2} = 37.78$

Now, total pressure at t = 75 min

$P_t = P_0 + 3x + 32.5$
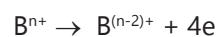
$= 233.8 + (3 \times 37.78) + 32.5$

$P_t = 379.55$ mm Hg

Time fraction, $t_{7/8}$ is time at which $\dfrac{7}{8}$ th of reaction gets completed, ie. $P_\Delta = \dfrac{P_0}{8}$

Using rate law, $\dfrac{P_0}{8} = P_0 e^{-kt} \Rightarrow t = \dfrac{2.303}{R}\log 8$
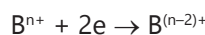
t = 399.96 min.

Sol 4: We have, the reaction as,

$$B^{n+} \rightarrow B^{(n-2)+} + 4e$$

At time t = 0 V_0 0

total time

t = 10 min $V_0 - x$ x

Now, for titration we have

$B^{n+} + 2e \rightarrow B^{(n-2)+}$

From this, we see that for volume V_0 of B^{n+}, 2V volume of titrant is used.

at time t = 0, volume of titrant used = 25 mL

$\Rightarrow 2V_0 = 25$ mL

$\Rightarrow V_0 = 12.5$ mL

For titration of $B^{(n-1)+}$, we have

$B^{(n+4)+} + 5e \rightarrow B^{(n-1)-}$

i.e. for volume V of $B^{n+} + B^{(n+4)}$, 5V volume of titrant is used.

$\therefore$ At time t = 10 min,

Volume of titrant used = 32 mL

$\Rightarrow 2(V_0 - x) + 5x = 32$

$\Rightarrow 2V_0 + 3x = 32$

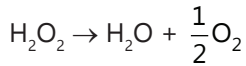$\Rightarrow 3x = 32 - 25$

$\Rightarrow x = \dfrac{7}{3}$

Now, since this is a first order reaction, rate law is

$k = \dfrac{2.303}{t}\log\dfrac{V_0}{V_{B^{n+}}} = \dfrac{2.303}{10}\log\dfrac{12.5}{12.5 - x}$

$$= \frac{2.303}{10}\log\frac{12.5}{12.5-\frac{7}{3}}; k = 0.0207 \text{ min}^{-1}$$

Sol 5: We have initially, volume strength = 20

According to reaction

$$H_2O_2 \rightarrow H_2O + \frac{1}{2}O_2$$

1 mole (34g) of H_2O_2 gives $\frac{1}{2}$ moles of O_2 i.e. 11.21 at STP

Now, volume strength is the volume of O_2 given by unit volume of H_2O_2

Let normality of H_2O_2 = N

Then, N = $\frac{\text{weight}}{\text{Eq. weight}}$

$\Rightarrow$ Weight = 17 N (equivalent weight = 17)

Now, 34 g of H_2O_2 gives 11.21 of O_2

$\therefore$ 17 N g of H_2O_2 gives $\frac{11.2\times17N}{34}$ of O_2

Volume strength = $\frac{11.2\times17N}{34}$ = 5.6 N

Now, initially volume strength = 20

$\Rightarrow N_0 = \frac{20}{5.6}$ = 3.75 N

At time, t = 6 hours, let normality be N.

Since, 10 mL of solution be diluted to 100 mL,

Now normality = $\frac{N.10}{100}$ = 0.1 N

Now, since this is first order reaction, according to rate law, as N is proportional to number of moles of H_2O_2

$$k = \frac{2.303}{t}\log\frac{N_0}{N} = \frac{2.303}{6}\log\frac{3.57}{3.125}; k = 0.022 \text{ hr}^{-1}$$

Sol 6: We have for oxide film formation.

$$k = \frac{2.303}{6}\log\frac{\tau_{max}}{\tau_{max}-\tau}$$

Where, τ_{max} = maximum thickness of oxide film (at $t \rightarrow \infty$)

τ = thickness at time t

We are given

$\tau_{max} = \frac{3.956}{1000}$ inch

$\tau = \frac{1.281}{1000}$ inch, at t = 6 weeks

$$k = \frac{2.303}{6}\log\frac{3.956}{3.956-1.281}$$

k = 0.065

Now, when, $\tau = \frac{2.481}{1000}$ inch, we have
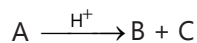
$$0.065 = \frac{2.303}{t}\log\frac{3.956}{3.956-2.481}$$

$$\Rightarrow t = \frac{2.303}{0.065}\times0.49$$

t = 15.13 weeks

t = 15.13 weeks
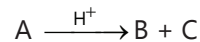
longer = 9.13 weeks

Sol 7: We have,

$$A \xrightarrow{H^+} B + C$$

Let initially x moles of A be present

$$A \xrightarrow{H^+} B + C$$

At t = 0   x   0   0

At t = ∞ 0   x   x

We know optical rotation of B and C are 40° and −80° respectively at completion,

total optical rotation

$\Rightarrow$ 40x − 80x = -10

$\Rightarrow$ x = 0.5

Now, optical rotation at t = 0

$\Rightarrow$ 60 × 0.5 = 30°

Using first order rate law,

$$k = \frac{2.303}{t}\log\frac{\theta_0 - \theta_\infty}{\theta_t - \theta_\infty}$$

θ_0 = initial optical rotation

or $t_{1/2} = \frac{0.693}{k} = \frac{0.693}{2.303} + \frac{1}{\log\frac{\theta_0 - \theta_\infty}{\theta_t - \theta_\infty}}$
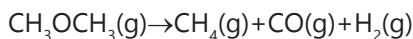
Putting values

$$t_{1/2} = \frac{0.693}{2.303} + \frac{20}{\log\frac{(30-1-20)}{(5-1-20)}}$$

since $\theta = 5°$

at t = 20 min = $\frac{0.3\times20}{\log2}$

$t_{1/2}$ = 20 min

Sol 8: Since, volume and temperature is constant, we take $P \propto n$

$$CH_3OCH_3(g) \rightarrow CH_4(g) + CO(g) + H_2(g)$$

at

t = 0   0. 4   0   0   0

t = 4.5hr.   0. 4–x   x   x   x

We are given k = 4. 78 × 10^{-3}, since unit is

min^{-1}. It is a first order reaction and

$P_A = P_0 e^{-kt}$

$= 0.4 \times e^{(-4.78 \times 10^{-3} \times 4.5 \times 60)}$

$\Rightarrow P_A = 0.11$

0. 4 − x = 0. 11

$\Rightarrow$ x = 0. 29

Now, at t = 4. 5hr, mean molecular mass, M_2

$$= \frac{(P_0 - x)M_{CH_3OCH_3} + x.M_{CH_4} + M_{CO} + x + M_0 + xM_{H_2}}{P + x + x + x + x}$$

$$= \frac{0.11 \times 46 \times 0.29 \times 16 + 0.29 \times 28 + 0.29 \times 2}{0.11 + 0.29 + 0.29 + 0.29} = 18.77$$

at t = 0, molecular mass

$M_1 = M_{CH_3OCH_3} = 46$

$P_t = 0.4 - x + 3x = 0.4 \times 2x = 0.98$

According to Graham's law

Rate of diffusion $\propto \dfrac{P}{\sqrt{M}}$

$$\frac{D_0}{D_t} = \frac{P_0}{P_t}\sqrt{\frac{M_2}{M_1}} = \sqrt{\frac{18.77}{46}} \times \frac{0.4}{0.98}$$

$\dfrac{D_0}{D_t} = 0.26$

Sol 9: (a) According to Arrhenius equation, we have

$$\log \frac{k_2}{k_1} = \frac{E_A}{2.303}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

Here, we have

$T_1 = (273 + 20)K = 293$ K

$T_2 = (273 + 3)K = 276$ K

$k_2 = \dfrac{k_1}{3}$

Putting values

$$\log \frac{1}{3} = \frac{E_A}{2.303 \times 8.314}\left(\frac{1}{293} - \frac{1}{276}\right)$$

$$\therefore E_A = \frac{+(\log 3 \times 2.303 \times 8.314 \times 293 \times 276)}{17}$$

E_A = 43. 46 kJ/mol

(b) When $T_2 = (273 + 40)$ K = 313K,

We have, $\log \dfrac{k_2}{k_1} = \dfrac{43.460}{303 \times 8.314}\left(\dfrac{1}{293} - \dfrac{1}{313}\right)$

$\Rightarrow k_2 = 3312 \, k_1$

Further, as $k \propto \dfrac{1}{t}$

$\therefore \dfrac{t_2}{t_1} = \dfrac{k_1}{k_2} \Rightarrow t_2 = \dfrac{6.4}{3.12}$

t_2 = 20. 47 hours

Sol 10: We have, according to Arrhenius equation

$$\log \frac{k_2}{k_1} = \frac{E_A}{2.303R}\left(\frac{1}{t_1} - \frac{1}{t_2}\right)$$

Here,

E_A = 70 ks mol^{-1}

$t_1 = (273 + 25)$ K = 298 K

$t_2 = (273 + 40)$ K = 313 K

Putting values

$$\log\frac{k_2}{k_1} = \frac{70000}{2.303 \times 8.314}\left(\frac{1}{298} - \frac{1}{313}\right)$$

$\Rightarrow k_2 = 3.87 \, k_1$

Now, equation

A $\rightarrow$ B

According to rate law

$[A] = [A_0] e^{-kt}$

At T = 298 K, k = k_1, ... t = 20 min,

$[A] = \dfrac{3[A_0]}{4}$

$\therefore \dfrac{3}{4} = e^{-k_1.20}$

$\Rightarrow k_1 = 0.014$ min^{-1}

$\therefore k_2 = 3.87 \, k_1 = 0.055$ min^{-1}

Now, at T = 313 K, t = 20 min,

k = 0. 055 min^{-1}

$[A] = [A_0] e^{-0.055 \times 20}$

$[A] = 0.3279 [A_0]$

$\therefore$ 67. 21 % of A got decomposed.

Sol 11: We have, according to Arrhenius equation

$$\log\frac{k_2}{k_1} = \frac{E_A}{2.303R}\left[\frac{1}{T_1} - \frac{1}{T_2}\right]$$

For, A → products

If k at 310 K is taken to be k

Then, k at 300 K is $\frac{k}{2}$

Putting this in equation, we get

$$\log 2 = \frac{E_A}{2.303 \times 8.314}\left[\frac{1}{300} - \frac{1}{310}\right]$$

$$\Rightarrow E_A = \frac{\log 2 \times 2.303 \times 8.314 \times 310 \times 300}{10}$$

E_A = 53. 67 kJ/mol

Now we are also given at T = 310 K,

$t_{1/2}$ = 30 min

$$\therefore \text{ k at 310 K } = \frac{0.693}{t_{1/2}} = 0.0231 \text{ min}^{-1}$$

At 310 K, for (ii) B → products

k = 211 for (i)

= 0. 0462 min^{-1}

Further, for (ii)

$$E_A = \frac{(E_A)}{2} = 26.802 \text{ k J/mol}$$

Therefore, using Arrhenius equation, we get

$$\log\frac{k}{0.0769} = \frac{268.02}{2.303 \times 8.314}\left(\frac{1}{310} - \frac{1}{300}\right)$$

k = 0. 0327 min^{-1}

Sol 12: We are given,

$$A \overset{k_1}{\underset{k_2}{<}} \begin{matrix} B \\ C \end{matrix}$$
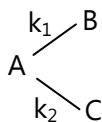
Here,

$$\frac{k_1}{k_2} = \frac{1}{9}, k = 1.3 \times 10^{-5} \text{ s}^{-1}$$

Now, both are first order reactions

$$\therefore \frac{d[A]}{dt} = -(k_1 + k_2)[A]$$

$$\Rightarrow [A] = [A_0]\ e^{-(k_1+k_2)t}$$

Now, for A → C,

We have, $\frac{d[C]}{dt} = k_2[A]$

$$\Rightarrow \frac{d[C]}{dt} = k_2[A_0]\ e^{-(k_1+k_2)t}$$

$$\Rightarrow \int_0^{[C]} d[C] = k_2[A_0]\int_0^t e^{-(k_1+k_2)t}dt$$

$$[C] = \frac{k_2[A_0]}{k_1 + k_2}(1 - e^{-(k_1+k_2)t})$$

$$\frac{[C]}{[A]} = \frac{k_2[A_0](1 - e^{-(k_1+k_2)t})}{(k_1+k_2).[A_0]e^{-(k_1+k_2)t}}$$

$$= \frac{k_2}{k_1+k_2}(e^{(k_1+k_2)t} - 1)$$

Now, we have k_1 = 1. 3 × 10^{-5} s^{-1},

$k_2 = 9k_1$ = 1. 17 × 10^{-7} s^{-1}

Time, t = 1 hour = 3600 s

Putting values,

$$\frac{[C]}{[A]} = \frac{9}{10}(e^{1.3 \times 10^{-4} \times 3600} - 1)$$

$$\frac{[C]}{[A]} = 0.537$$

Sol 13: As Cis-(en)$_2$(OH)$_2$$^+$ $\underset{k_b}{\overset{k_f}{\rightleftharpoons}}$

trans-Cr(en)$_2$(OH)$_2$$^+$

We have,

Eq. constant = $\frac{k_f}{k_b}$ = 0. 16

and $k_f = k_1$ = 3. 3 × 10^{-1} s^{-1}

$$\Rightarrow k_b = \frac{k_t}{0.16} = 2.0625 \times 10^{-4} \text{ s}^{-1}$$

Now using formula for eq. reactions.

$$\ln\left(\frac{x_{eq}}{x_{eq}.x}\right) = (k_f + k_b)\ t$$

We have to find t for which $x = \frac{x_{eq}}{q}$

$$\ln\left(\frac{x_{eq}}{x_{eq} - \frac{x_{eq}}{2}}\right) = (3.3 \times 10^{-4} + 2.0625 \times 10^{-3})t$$

$$\Rightarrow t = \frac{\ln 2}{2.3925 \times 10^{-5}} \text{ s}$$

t = 289. 71 s $\Rightarrow$ t = 4. 83 min

Sol 14: We have, $A \underset{k_2}{\overset{k_1}{\rightleftharpoons}} B$

Also, we know, $k_{eq} = \dfrac{k_1}{k_2} = \dfrac{[B]_{eq}}{[A]_{eq}}$

$\Rightarrow \dfrac{k_1}{k_2} = 4$, $k_1 = 10^{-2} \text{ s}^{-1}$

$\Rightarrow k_2 = \dfrac{10^{-2}}{4} = 2.5 \times 10^{-3} \text{ s}^{-1}$

Now at eq. , $[A] = [A_0] - x_{eq}$

$[B] = x_{eq}$

Then, $\dfrac{x_{eq}}{[A]e^{-x_{eq}}} = 4$

We are given $[A]_0 = 0.01$ mole L^{-1}

$\dfrac{x_{eq}}{0.01 x_{eq}} = 1$

$5x_{eq} = 0 + 60.07$

$x_{eq} = 0.008$ mole L^{-1}

Now, using equilibrium first order formula,

$\ln\left(\dfrac{x_{eq}}{x_{eq} - x}\right) = (k_1 + k_2)t$

At t = 30 s,

$\ln\left(\dfrac{0.008}{0.008 - x}\right) = (12.5 \times 10^{-3}) \times 30 = -0.375$

$x = 0.0025$ mole L^{-1}

Sol 15: We have,

$A(g) \rightleftharpoons B(g)$
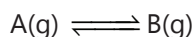
For forward reaction, we have

$\Delta H = \Delta E = -33$ kJ/mol

We know,

$\ln k = \dfrac{-\Delta H^o}{RT}$ (since $\Delta S \approx 0$)

with T = 300 K, $\Delta H = 33$ kJ/mol

we get, $k = 5.57 \times 10^5$

Now, we are given

$\dfrac{E_f}{E_b} = \dfrac{20}{31}$

Now, we have for this transformation
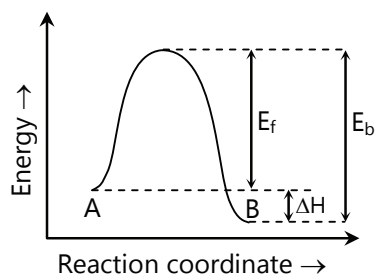
We see that

$E_b = E_f + |\Delta H|$

$\Rightarrow$ But $E_f = \dfrac{20E_b}{31}$

$\therefore E_b = \dfrac{20E_b}{31} + 33 \quad \Rightarrow \dfrac{11E_b}{31} = 33$

$\Rightarrow E_b = 63$ kJ/mol

$E_f = E_b - 33$

$E_f = 30$ kJ/mol

Sol 16: We have rate k'[complex] [a], k' = k[H⁺] [b]

Let's assume that this is Pseudo first order reaction, that is a = 1

Then, we have $t_{1/2} = \dfrac{0.693}{k'}$,

$t_{3/4} = \dfrac{1.386}{k'}$

We note that, here $t_{3/4} = 2. t_{1/2}$

which is true for given data also

Now, when, $[H^+] = 0.01$

$t_{1/2} = 1 = \dfrac{0.693}{k'} = \dfrac{0.693}{k[H^+]^b} \Rightarrow (0.01)^b = \dfrac{0.693}{k}$

When $[H^+] = 0.02$
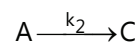
$(0.02)^b = \dfrac{0.693}{k.t_{1/2}} = \dfrac{1.386}{k}$

These both will be satisfied for b = 1.

$\therefore$ Taking a = b = 1, all the given data can be verified and there are no contradictions

$\therefore$ a = b = 1

Sol 17: $A \xrightarrow{k_1} B$

$A \xrightarrow{k_2} C$

We have, k for disappearance of A, $\dfrac{-d[A]}{dt} = (k_1 + k_2)t$

$\therefore k = k_1 + k_2$

Using Arrhenius equation,

$$Ae^{\frac{-E}{RT}} = A_1 e^{\frac{-E_1}{RT}} + A_2 e^{\frac{-E_2}{RT}}$$

A = Pre exponential constant
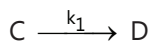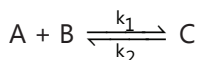
Differentiating with respect to $\dfrac{1}{T}$, we get

$$\frac{-AE}{R}e^{\frac{-E}{RT}} = \frac{-A_1 E_1}{R}e^{\frac{-E_1}{RT}} + \frac{-A_2 E_2}{R}e^{\frac{-E_2}{RT}}$$

$$\Rightarrow Ek = E_1 k_1 + E_2 k_2$$

$$\Rightarrow E = \frac{E_1 k_1 + E_2 k_2}{k}$$

$$\Rightarrow E = \frac{E_1 k_1 + E_2 k_2}{k_1 + k_2}$$

Sol 18: (a) We have,

$$A + B \underset{k_2}{\overset{k_1}{\rightleftharpoons}} C$$

$$C \xrightarrow{k_1} D$$

Since second step is RDS,

Rate = $k_3[C]$

Also, $\dfrac{d[C]}{dt} = -k_3[C] + k_2[A][B] - k_2[C]$

Now, at steady state, $\dfrac{d[C]}{dt} = 0 \Rightarrow [C] = \dfrac{k_1[A][B]}{k_3 + k_2}$

$\therefore$ Rate = $\dfrac{k_1 k_3 [A][B]}{k_3 + k_2}$

(b) If $k_2 >> k_3$, then $k_2 + k_3 \simeq k_2$

Then, Rate = $\dfrac{k_1 k_3}{k_2}$ [A] [B]

Using Arrhenius equation,

$$k = A\ e^{\frac{-E_A}{RT}}$$

$$k = \frac{A_1 e^{\frac{E_{a_1}}{RT}} A_3 e^{\frac{E_{a_3}}{RT}}}{A_2 e^{\frac{E_{a_2}}{RT}}} = \frac{A_1 A_3}{A_2}e^{\frac{-(E_{a_1} + E_{a_3} - E_{a_2})}{RT}}$$

Comparing with $k = Ae^{\frac{-E_a}{RT}}$

$$A = \frac{A_1 A_3}{A_2}$$

$$E_a = E_{a_1} + E_{a_3} - E_{a_2}$$

Sol 19 We have,

Rate, R = $k_3[COCl][Cl_2]$

($\because$ (iii) is slowest step (RDS))

Also, from equilibrium of (ii),

$$\frac{k_2}{k_{-2}} = \frac{[COCl]}{[CO][Cl]}$$

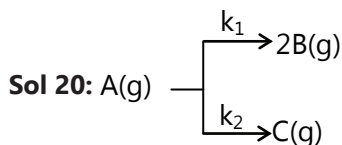And from equilibrium of (i),

$$\frac{k_1}{k_{-1}} = \frac{[Cl]^2}{[Cl_2]}$$

$$[Cl] = \left(\frac{k_1}{k_{-1}}\right)^{1/2}([Cl_2])^{1/2}$$

Putting these values back in rate formula,

we get

$$Rate = k_3 \frac{k_2}{k_{-2}}[CO]\left(\frac{k_1}{k_{-1}}\right)^{+\frac{1}{2}}([Cl_2])^{1/2}[Cl]$$

$$\frac{d[COCl_2]}{dt} = k_3 \frac{k_2}{k_{-2}}\frac{k_1}{k_{-1}}[CO][Cl_2]^{3/2} = k[CO][Cl_2]^{3/2}$$

$$k = k_3 \cdot \frac{k_2}{k_{-2}}\left(\frac{k_1}{k_2}\right)^{1/2}$$

Sol 20: A(g) $\overset{k_1}{\longrightarrow}$ 2B(g), $\overset{k_2}{\longrightarrow}$ C(g)

We have,

Rate = $\dfrac{-d[A]}{dt} = -(k_1 + k_2)[A]$

$[A] = [A]_0\ e^{-kt}$; $k = k_1 + k_2$

Further, Rate = $\dfrac{1}{2}\dfrac{d[B]}{dt} = k_1[A]$

Putting value of [A] and integrating

$$[B] = \frac{2k_1[A_1]}{k_1 + k_2}(1 - e^{-kt})$$

Similarly, $[C] = \dfrac{k_2[A]_0}{k_1 + k_2}(1 - e^{-kt})$

Now, we are given $[A]_0 = 1$ atm

At $t \to \infty$, $P_t = 1.5$ atm

Putting values and taking $t = \infty$, we get

$$\frac{2k_1}{k_1+k_2}+\frac{k_2}{k_1+k_2} = 1.5$$

$$\Rightarrow 2k_1 + k_2 = 1.5\,k_1 + 1.5k_2$$

$$\Rightarrow k_1 = k_2 = \frac{k}{2}$$

Now, taken at t = 10s, P_t = 1.4 atm

$$\therefore [A]_0 e^{-k.10} = \frac{k[A]_0}{k}(1-e^{-k.10})$$

$$\frac{k[A]_0}{2k}(1-e^{-k.10}) = 1.7$$

$[A]_0 = 1,$

$$\therefore e^{-10R} + 1 - e^{-10R} + \frac{1}{2} - \frac{e^{-10k}}{2} = 1.4$$

$$\Rightarrow e^{-10}R = 0.2$$

$$\Rightarrow k = 0.16$$

$$\Rightarrow k_1 = k_2 = \frac{k}{2} = 0.08$$

Sol 21: For 50% completion, time taken

$$t_{1/2} = \frac{0.693}{k}$$

$$\Rightarrow k = \frac{0.693}{69.3} = 0.01\ \text{min}^{-1}$$

Now, for 80%, $[A] = 0.2[A_0]$

Using $[A] = [A]_0 e^{-RT} \Rightarrow 0.2 = e^{-RT}$

$$\Rightarrow t = \frac{\ln 5}{0.01}$$

t = 161 min

Sol 22: We have, from Arrhenius equation,

$$\log\frac{k_2}{k_1} = \frac{E_a}{2.303R}\left[\frac{1}{T_1}-\frac{1}{T_2}\right]$$

Now, $\frac{k_2}{k_1} = 4$, $T_1 = 27°C = 300$ K

$T_2 = 47°C = 320$ K

Putting values, we find

$$\log 4 = \frac{E_A}{2.303\times 8.314}\left[\frac{1}{300}-\frac{1}{320}\right]$$

$$\Rightarrow E_A = \frac{2\log 2\times 320\times 300\times 2.303\times 8.314}{20}$$

$E_A = 55.33$ kJ mol^{-1}

Sol 23: $2A + B + C \rightarrow D + 2E$

(i) Since, this is first order w. r. t. A, second order w. r. t. B, and 0 order w. r. t. C.

Rate law = $k[A]\,[B]^2[C]^0$

Rate, R = $k[A]\,[B]^2$

(ii) Now rate, R' = $k[2A]\,[2B]^2 = 8k[A]\,[B]^2 = 8k$

$\therefore$ Rate becomes 8 times

Sol 24: We know, for first order reaction

$$k = \frac{2.303}{30}\log\frac{[A]_0}{[A]_t}$$

At T = 27°C = 300 K, at t = 30 min, 50% of reaction gets completed, i. e. $[A]_t = 0.5[A]_0$

$$k = \frac{2.303}{30}\log 2$$

k = 0.0231 min^{-1} = 3.85 × 10^{-4} s^{-1}

At T = 47°C=320 K, time taken for 50% completion is 10 min.

$$\therefore k = \frac{2.303}{10}\log 2$$

k = 0.0693 min^{-1} = 11.55 × 10^{-4} s^{-1}

Now, by Arrhenius equation

$$\ln\frac{k_2}{k_1} = \frac{E_A}{2.303}\left(\frac{1}{T_1}-\frac{1}{T_2}\right)$$

At T = 300 K, k = 0.0231 min^{-1}

T = 320 K, k = 0.0693 min^{-1}

Putting values

$$\log\frac{0.0693}{0.0231} = \frac{E_A}{2.303\times 8.314}\left(\frac{1}{300}-\frac{1}{320}\right)$$

$E_A = 43.78$ kJ/mol

Sol 25: Firstly, we assume that reaction is first order and see if the data is consistent.

For first order reaction, we have

$$k = \frac{2.303}{t}\log\frac{\theta_0 - \theta_\infty}{\theta_t - \theta_\infty}$$

At time, t = 10 min,

$$k = \frac{2.303}{t}\log\frac{32.4-(-11.1)}{28.8-(-11.1)}$$

k = 8.14 × 10^{-3} min^{-1}

At time, t = 20 min

$k = \dfrac{2.303}{t} \log \dfrac{(32.4 + 11.1)}{25.5 - (-11)}$

$k = 8.64 \times 10^{-3} \text{ min}^{-1}$

At time, t = 30 min

$k = \dfrac{2.303}{t} \log \dfrac{32.4 - (11.1)}{22.4 - (-11)} = 8.70 \times 10^{-3} \text{ min}^{-1}$

At t = 40 min,

$k = \dfrac{2.303}{40} \log \dfrac{32.4 - (11.1)}{19.6 - (-11.1)} = 8.71 \times 10^{-3} \text{ min}^{-1}$

We see that all values of k are pretty close to each other,

$\therefore$ The reaction is first order.

Sol 26: We know, for nth order reaction $t_{1/2} \propto \dfrac{1}{[A]_0^{n-1}}$

Here as $[A]_0$ is doubled, $t_{1/2}$ gets halved,

$\therefore t_{1/2} \propto \dfrac{1}{[A]_0}$

Or n – 1 = 1

$\Rightarrow$ n = 2

Hence, second order reaction.

Sol 27: We have, by Arrhenius equation

$\log \dfrac{k_2}{k_1} = \dfrac{E_a}{2.303k}\left(\dfrac{1}{T_1} - \dfrac{1}{T_2}\right)$

Now, given data,

at t = 50ºC = 323 K,

$k = 1.5 \times 10^{+7} \text{ sec}^{-1}$.

at T = 100ºC = 373 K,

$k = 4.5 \times 10^{7} \text{ sec}^{-1}$

Filling the data,

$\log 3 = \dfrac{E_a}{2.303 \times 8.314}\left(\dfrac{1}{323} - \dfrac{1}{373}\right)$

$E_a = A e^{\frac{-E_a}{RT}}$

$E_a = 2.2 \times 10^{7} \text{ J mol}^{-1}$

Now, $k = A e^{\frac{-E_a}{RT}}$

$\Rightarrow A = k e^{\frac{+E_a}{RT}}$

$= 1.5 \times 10^{7} e^{\frac{2.2 \times 10^{7}}{8.214 \times 323}}$

$A = 5.42 \times 10^{10} \text{ s}^{-1}$

Sol 28: Rate = k[A]

(i) Initial rate = $k[A]_0$

$= 1.8 \times 10^{-2} \times 0.1$

$= 1 \times 10^{-3} \text{ mol sec}^{-1} \text{ L}^{-1}$

(ii) After 60 sec (1 min),

Rate = $k[A]_1$

$= k[A]_0\, e^{-k \times 60}$

$= 5.495 \times 10^{-3} \text{ mol sec}^{-1} \text{ L}^{-1}$

Sol 29: Since, unit of rate constant is min^{-1}, it is first order reaction.

Initial rate = $k[A]_0 = 10^{-3} \times 0.2 = 2 \times 10^{-4} \text{ mol min}^{-1} \text{ dm}^{-3}$

After 200 minutes,

$[A] = [A]_0\, e^{-10^{-3} \times 200} = 0.8187[A]_0$

$\therefore$ 18.12 % of reactant converted into product.

Sol 30: (i) At time, t = 10 min, $[A] = 0.8\,[A]_0$

$\therefore 0.8[A]_0 = [A]_0\, e^{-10k}$

$\Rightarrow k = 0.022 \text{ min}^{-1}$

(ii) When 75% reaction is completed,

$[A] = \dfrac{1}{4}[A]_0,$

$\therefore \dfrac{1}{4}[A]_0 = [A]_0\, e^{-0.022t}$

$\Rightarrow t = 63.01 \text{ min.}$

Exercise 2

Sol 1: (B) From the table, we see that when (A) is doubled, rate get becomes 4 times, keeping (B) constant

$\therefore$ Rate $\propto (A)^2$

Also, when (B) is doubled, keeping (A) doubled.

Rate becomes 2 times

$\therefore$ Rate $\propto$ (B)

$\therefore$ Rate = $k(A)^2(B)$

Sol 2: (A) Rate, $r_i = k(A)^n[B]^m$

$r_f = k[2A]^n \left[\dfrac{B}{2}\right]^m = \dfrac{k\,2^n}{2^m}[A]^n[B]^m$

$\dfrac{r_f}{r_i} = 2^{(n-m)}$

Sol 3: (A) We have $t_{1/2}$ = 15 min (0. 8 M → 0. 4M)

Now, for 0. 1 M to 0. 025 M,

t = 2 × $t_{1/2}$ = 30 min

(0. 1 $\xrightarrow{t_{1/2}}$ 0. 5 $\xrightarrow{t_{1/2}}$ 0. 025)

Sol 4: (D) Only statement (D) is correct as k is constant at a given temperature.

(A) and (B) are correct for first order reaction. (C) is wrong as

$$\frac{d[C]}{dt} = -\frac{1}{2}\frac{d[A]}{dt}\left(not\ 2\frac{d[A]}{dt}\right)$$

Sol 5: (D) For a first order reaction,

$[A] = [A]_0 e^{-kt}$

When, $[A] = \frac{3}{4}[A]_0$, t = $t_{3/4}$

$\Rightarrow \frac{3}{4} = e^{-k.t_{3/4}}$

$\Rightarrow t_{3/4} = \frac{0.29}{k}$

Sol 6: (D) rate ∝ $[O]^2$

∴ When [(O)] is doubled, rate becomes 4 times.

Sol 7: (C) A + 3B → P

ΔH = -2x kJ/mole of A   ...(i)

M → 2Q + R

ΔH = -x kJ/mole of M   ...(ii)

We see that, if these reactions are carried simultaneously energy released from (i) and energy absorbed is (ii) counter each other further, ΔH = 2OH, rate of second reaction will be double of that of (i)

Now, rate of first reaction= $\frac{-1}{3}\frac{d[B]}{dt} = \frac{y}{3}$

Rate of second reaction= $\frac{2y}{3} = \frac{1}{2}\frac{d[Q]}{dt} \Rightarrow \frac{d[Q]}{dt} = \frac{4}{3}y$

Sol 8: (B) We have t = 138. 6 min for

1M → 0. 25 M

i.e., $2t_{1/2}$ = 138. 6 = $\frac{2 \times 0.693}{k}$

(1 $\xrightarrow{t_{1/2}}$ 0. 5 $\xrightarrow{t_{1/2}}$ 0. 25)

⇒ k = 0. 01

When [A] = 0. 1,

Rate = k[A]

= 0. 01 × 0. 1 M min^{-1}

= 10^{-3} M min^{-1}

Sol 9: (C) For zero order reaction, rate is always constant.

i. e. rate = 10^{-2} M min^{-1}

$$A(g) \rightarrow 2B(g)$$

t = 0   0. 1

t = 1   0. 1–x   2x

$\frac{1}{2}\frac{d[B]}{dt} = 10^{-2}$

[B] = 0. 02 t

At t = 60 sec = 1 minute
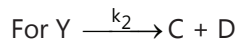
[B] = 0.02 M

Sol 10: (D) Let time be t

Then, for X $\xrightarrow{k_1}$ A + B
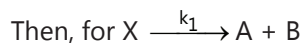
50% reaction gets completed at time t

$\Rightarrow \frac{1}{2}[X]_0 = [X]_0\ e^{-k_1 t}$

$k_1 = \frac{\ln 2}{t}$

For Y $\xrightarrow{k_2}$ C + D

96 % of reaction gets completed at time t.

∴ 0. 04$[Y]_0$ = $[Y]_0\ e^{-k_2 t}$

$k_2 = \frac{\ln 25}{t}$

$\frac{k_2}{k_1} = \frac{\ln 25}{\ln 2}$ = 4. 65

Sol 11: (D) We know, for nth order reaction

$\propto \frac{1}{P_0^{n-1}}$

$\Rightarrow \frac{(t_{1/2})_2}{(t_{1/2})_1} = \left(\frac{P_{0_1}}{P_{0_2}}\right)^{n-1}$

Putting values,

$\frac{950}{235} = \left(\frac{500}{250}\right)^{n-1}$

$\Rightarrow n - 1 = \frac{\log 4.04}{\log 2}$ = 2; ⇒ n = 3

Sol 12: (C) We have first order reaction

$$k = \frac{2.303}{t}\log\frac{[A]_0}{[A]_t}$$

at t = 20 min, $(A)_t = 0.8(A)_0$

(Since 20% reaction completed)

$$\Rightarrow k = \frac{2.303}{20}\log\frac{5}{4}$$

$k = 1.11 \times 10^{-2}$ min^{-1}

$$t_{1/2} = \frac{0.693}{k} = 62.13 \text{ minutes}$$

Sol 13: (C) Rate = $k(A) = k(A)_0 e^{-kt}$

It follows an exponential decay.

Sol 14: (D) $A(g) \rightarrow 2B(g)$

We have, $k_{eq} = \dfrac{[B]^2}{[A]} = \left[\dfrac{\left(\dfrac{100}{V}\right)^2}{\dfrac{10^{-5}}{V}}\right] = \dfrac{10^4}{10^{-5}} \cdot \dfrac{1}{10} = 10^8$

$10^8 = \dfrac{k_f}{k_b} = \dfrac{1.5 \times 10^{-3}}{k_b}$

$\Rightarrow k_b = 1.5 \times 10^{-11}$ L mol^{-1} s^{-1}

Sol 15: (B) $A + B \rightarrow C + D$

t = 0   1   1   0   0

t = 1   1-x   1–x   x   x

We have,

$$\text{Rate} = \frac{-d[A]}{dt} = k(A)^{1/2}(B)^{1/2}$$

$$\Rightarrow \frac{-d[A]}{dt} = k(1-x)^{1/2}(1-x)^{1/2}$$

$$\Rightarrow \frac{-d[A]}{dt} = k(1-x)$$

This can be written as,

$$\frac{-d[A]}{dt} = k(A)$$

$$\Rightarrow (A) = (A)_0 e^{-kt}$$

when $(A) = 0.25(A)_0$

$$t = \frac{2\ell n2}{k} = \frac{2 \times 2.303\log 2}{2.303 \times 10^{-3}}$$

t = 600 s

Sol 16: (A) We have for first order,

$(A) = (A)_0 e^{-kt}$

$(A)_0 = \dfrac{0.1}{2}$ mol L^{-1} = 0.05 mol L^{-1}

$k = 3.465 \times 10^{-6}$ s^{-1}, t = 200 s

$(A) = 0.05 \ e^{-3.465 \times 10^{-6} \times 200}$

≈ 0.05 M

Sol 17: (D) R is universal gas constant

k is rate constant

A is pre exponential factor

E_a is activation energy

Sol 18: (C) This is the correct definition.

Sol 19 (B) $k = A\,e^{-E_0/RT}$;As T → ∞,

$k = A = 6 \times 10^{14}$ s^{-1}($\because e^{-E_0/RT} \rightarrow 1$)

Sol 20: (B) We have, from Arrhenius equation

$$\log\frac{k_2}{k_1} = \frac{E_A}{2.303R}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

Here, at $T_1 = 27°C = 300$ K

$$k_1 = \frac{0.693}{20} \text{ min}^{-1}$$

At $T_2 = 47°C = 320$ K

$$k_2 = \frac{0.693}{5} \text{ min}^{-1}$$

Putting these values,

$$\log 4 = \frac{E_A}{2.303 \times 8.314}\left(\frac{1}{300} - \frac{1}{320}\right)$$

$\Rightarrow E_A = 55.14$ kJ/mol

Sol 21: (C) We have, 27°C = 300 K, 3.8×10^{-16} of reactant molecules exist in the activated region.

i.e, $N = 3.8 \times 10^{-16} N_0$

Now, $N = N_0 e^{-E_a/RT}$

$E_a = RT\log_e\dfrac{N_0}{N} = 8.314 \times 300 \log_e$

$$\dfrac{N_0}{3.8 \times 10^{-16}N_0}$$

$E_a = 100$ kJ/mol

Sol 22: (D) Since, at 400 K, 0. 0001% (10^{-4}%) of collisions are effective only 10^{-4}% of molecules have their energy above activation energy.

E_a = 2. 303 RT log $\dfrac{N_0}{N}$

= 2. 303 × 8. 314 × 400 log $\dfrac{N_0}{10^{-6}N_0}$

= 45. 944 k J/mol = 11. 05 k cal/mol

Previous Years' Questions

Sol 1: (A) $\dfrac{1}{2}A \to 2B$; $-2\dfrac{d[A]}{dt} = \dfrac{1}{2}\dfrac{d[B]}{dt}$; $-\dfrac{d[A]}{dt} = \dfrac{1}{4}\dfrac{d[B]}{dt}$

Sol 2: (C) $\dfrac{\text{Rate at 50°C}}{\text{Rate at} T_1 °C}$ = $(2)^{\frac{\Delta T}{T_1}}$ = $(2)^{\frac{50}{10}}$ = 2^5 = 32 times

Sol 3: (C) k = $\dfrac{2.303}{t}\log_{10}\dfrac{a}{a-x}$;

t = 2 × 10^2, a = 800, a − x = 50

k = $\dfrac{2.303}{2\times10^2}\log_{10}\dfrac{800}{50}$ = $\dfrac{2.303}{2\times10^2}\log_{10}16$

= $\dfrac{2.303}{2\times10^2}\log_{10}2^4$ = $\dfrac{2.303}{2\times10^2}$ × 4 × 0.301 = 1.38 × 10^{-2} s^{-1}

Sol 4: (A) 2A + B → Product

When conc. of B is doubled, the half-life did not change, hence reaction is of first order w.r.t. B. When concentration of A is doubled, reaction rate is doubled, hence reaction is of first order w.r.t. A,

Hence, over all order of reaction is 1 +1 = 2

So, unit of rate constant mol^{-1} lit s^{-1}.

Sol 5: (D) Rate= k(N_2O_5)

hence 2.4 × 10^{-5}

= 3.0 × $10^{-5}(N_2O_5)$ or (N_2O_5)

= 0.8 mol l^{-1}

Sol 6 (C) In first order reaction for x% completion

k = $\dfrac{2.303}{t}\log\left(\dfrac{100}{100-x\%}\right)$

$\dfrac{0.693}{t_{1/2}}$ = $\dfrac{2.303}{t}\log\left(\dfrac{100}{100-99}\right)$

$\dfrac{0.693}{6.93}$ = $\dfrac{2.303\times2}{t}$

So, t = 46.06 min.

Sol 7: (B) Because two molecules are taking part in elementary reaction.

Sol 8: (C) Since $-\dfrac{dx}{dt} \propto [CO]^2$ so on doubling the concentration of CO, the rate of reaction will increase by 4 times.

Sol 9: (A) R = k(A)(B)^2 order of reaction =2+1= 3

Sol 10: (D) The differential rate law for,

NO + Br_2 → $NOBr_2$ would be

$-\dfrac{dc}{dt}$ =k[$NOBr_2$][NO]

We have, $K_c = \dfrac{[NOBr_2]}{[NO][Br_2]}$

Provided the first reaction attains equilibrium rapidly.

$\therefore -\dfrac{dc}{dt}$ = k × k_c × $[NO]^2[Br_2]$ = $k[NO]^2[Br_2]$

∴The order of the reaction with respect to NO(g) is 2.

Sol 11: (A) For A

Rate = k[Cl_2][H_2S] (By slow step)

For B

Rate = k[Cl_2][HS^-]

k_{eq} = $\dfrac{[H^+][HS^-]}{[H_2S]}$

(According to equilibrium)

Rate = k[Cl_2] $\dfrac{k_{eq}[H_2S]}{[H^+]}$

Rate = k.k_{eq}[Cl_2] $\dfrac{[H_2S]}{[H^+]}$

Sol 12: (D) $t_{1/2}$ = $\dfrac{a}{2k_0}$ (for zero order reaction)

k_0 = $\dfrac{a}{2\times t_{1/2}}$ = $\dfrac{2}{2\times1}$ = 1

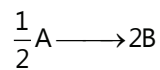$k_0 = \dfrac{A_0 - [A]_t}{t} \Rightarrow k_0 = \dfrac{0.50 - 0.25}{t} = 1$

$t = 0.25$ hr.

Sol 13: (D) So, $\Delta H_{Reaction} = E_f - E_b = 80 - 100 = -20$.

Sol 14: (A) For endothermic reaction $\Delta H = +ve$

Then from equation $\Delta H = E_{aF.R} - E_{aB.R}$; $E_{B.R} < E_{F.R}$.

Sol 15: (B) In photochemical reaction, the rate of formation of product is directly proportional to the intensity of absorbed light.

Sol 16: (B)

$\dfrac{1}{2}A \longrightarrow 2B$

$-\dfrac{d[A]}{dt} = +\dfrac{d[B]}{2dt}$

$-\dfrac{d[A]}{dt} = \dfrac{1}{4}\dfrac{d[B]}{dt}$

Sol 17: (C)

$\because \quad \lambda = \dfrac{0.6932}{t_{1/2}} = \dfrac{0.6932}{6.93} \text{min}^{-1}$

Also $\quad t = \dfrac{2.303}{\lambda}\log\dfrac{[A_\circ]}{[A]}$

$[A_\circ]$ = initial concentration (amount)

$[A]$ = final concentration (amount)

$\therefore \quad t = \dfrac{2.303 \times 6.93}{0.6932}\log\dfrac{100}{1} = 46.06$ minutes

Sol 18: (C)

For a zero order reaction $k = \dfrac{x}{t}$ .... (i)

Where x = amount decomposed

$\quad$ k = zero order rate constant

for a zero order reaction

$k = \dfrac{[A]_0}{2t_{1/2}}$ .... (ii)

Since $[A_0] = 2M$, $t_{1/2} = 1$hr; k=1

$\therefore$ from equation (i)

$t = \dfrac{0.25}{1} = 0.25$ hr

Sol 19: (D) Rate equation is to be derived w.r.t slow

Step $\therefore$ from mechanism (A)

Rate = $k[Cl_2] [H_2S]$

Sol 20: (B)

Temperature coefficient $\mu = 2$;

$\mu^{\frac{\Delta T}{10}} = \dfrac{k_2}{k_1}$;

$\mu^{\frac{50}{10}} = 2^5 = 32 = \dfrac{k_2}{k_1}$

Therefore $32k_1 = k_2$

Sol 21: (B) $k = \dfrac{2.303}{40}\log\dfrac{0.1}{0.025}$;

$k = \dfrac{0.693}{20}$

For a F.O.R., rate $= \dfrac{0.693}{20} \times 10^{-2} = 3.47 \times 10^{-4}$ M / min.

Sol 22: (A) $\log\dfrac{K_2}{K_1} = \dfrac{-E_a}{2.030R}\left(\dfrac{1}{T_2} - \dfrac{1}{T_1}\right)$

$\dfrac{K_2}{K_1} = 2$; $T_2 = 310K$ $\qquad\qquad$ $T_1 = 300K$

$\Rightarrow \log 2 = \dfrac{-E}{2.303 \times 8.134}\left(\dfrac{1}{310} - \dfrac{1}{300}\right)$

$\Rightarrow E_a = 53598.6$ J / mol $= 53.6$ KJ / mol

Sol 23: (D)

Rate of Reaction $= \dfrac{-1}{2}\dfrac{d[A]}{dt} = -\dfrac{d[B]}{dt} = \dfrac{d[C]}{dt} = \dfrac{d[D]}{dt}$

Let rate of Reaction $= k(A)^x(B)^y$

Or, $\dfrac{d[C]}{dt} = k[A]^x[B]^y$

Now from table,

$1.2 \times 10^{-3} = k [0.1]^x[0.1]^y$ .....(i)

$1.2 \times 10^{-3} = k [0.1]^x[0.2]^y$ .....(ii)

$2.4 \times 10^{-3} = k [0.2]^x[0.1]^y$ .....(iii)

Dividing equation (i) by (ii)

$\Rightarrow \quad \dfrac{1.2 \times 10^{-3}}{1.2 \times 10^{-3}} = \dfrac{k[0.1]^x[0.1]^y}{k[0.1]^x[0.2]^y}$

$\Rightarrow \quad\quad 1 = \left[\dfrac{1}{2}\right]^y$

$\Rightarrow \qquad y = 0$

Now dividing equation (i) by (iii)

$\Rightarrow \qquad \dfrac{1.2 \times 10^{-3}}{1.2 \times 10^{-3}} = \dfrac{k[0.1]^x [0.1]^y}{k[0.2]^x [0.1]^y}$

$\Rightarrow \qquad \left[\dfrac{1}{2}\right]^1 = \left[\dfrac{1}{2}\right]^y$
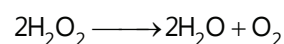
$\Rightarrow \qquad x = 1$

Hence $\dfrac{d[C]}{dt} = k[A]^1 [B]^0$

Sol 24: (A) In 50 minutes, concentration of H_2O_2 becomes $\dfrac{1}{4}$ of initial.

$\Rightarrow \qquad 2 \times t_{1/2} = 50$ minutes

$\Rightarrow \qquad t_{1/2} = 25$ minutes

$\Rightarrow \qquad K = \dfrac{0.693}{25}$ per minutes

$r_{H_2O_2} = \dfrac{0.693}{25} \times 0.05 = 1.386 \times 10^{-3}$

$2H_2O_2 \longrightarrow 2H_2O + O_2$

$r_{O_2} = \dfrac{1}{2} \times r_{H_2O_2}$

$r_{O_2} = 0.693 \times 10^{-3}$

$r_{O_2} = 6.93 \times 10^{-4}$ mol / minute $\times$ litre

JEE Advanced/Boards

Exercise 1

Sol 1: $4NH_3(g) + 5O_2(g) \rightarrow 4NO(g) + 6H_2O(g)$
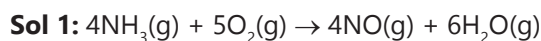
Rate of reaction $= \dfrac{-1}{4}\dfrac{d[NH_3]}{dt} = \dfrac{-1}{5}\dfrac{d[O_2]}{dt} =$

$\dfrac{1}{4}\dfrac{d[NO]}{dt} = \dfrac{1}{6}\dfrac{d[H_2O]}{dt}$

(i) Rate of reaction $= \dfrac{1}{4}\dfrac{d[NO]}{dt} = \dfrac{1}{4}\dfrac{1.08 \times 10^{-2}}{3}$

$= 9 \times 10^{-4}$ mol L^{-1}

(ii) $\dfrac{-d[NH_3]}{dt} = \left|\dfrac{+4}{4}\dfrac{d[NO]}{dt}\right|$

$= \dfrac{+1.08}{3} \times 10^{-2} = 3.6 \times 10^{-3}$ mol L^{-1}

(iii) $\dfrac{d[H_2O]}{dt} = \dfrac{6}{4}\dfrac{d[NO]}{dt}$

$= \dfrac{3}{2} \times \dfrac{1.08 \times 10^{-2}}{3} = 5.4 \times 10^{-3}$ mol L^{-1}

Sol 2: (a) $2H_2O_2 \rightarrow 2H_2O + O_2$

We know, $\dfrac{-1}{2}\dfrac{d[H_2O_2]}{dt} = \dfrac{-1}{2}\dfrac{d[H_2O]}{dt} = \dfrac{d[O_2]}{dt}$

$\dfrac{d[H_2O]}{dt} = 2\dfrac{d[O_2]}{dt} = 2 \times 3.6$ M min^{-1}

$\dfrac{d[H_2O]}{dt} = 7.2$ M min^{-1}

(b) $\dfrac{-d[H_2O_2]}{dt} = \dfrac{2}{2}\dfrac{d[H_2O]}{dt} = \dfrac{-d[H_2O_2]}{dt} = 7.2$ M min^{-1}

Sol 3: $N_2 + 3H_2 \rightarrow 2NH_3$
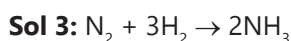
(a) $\dfrac{d[N_2]}{dt} = \dfrac{-1}{3}\dfrac{d[H_2]}{dt} = \dfrac{1}{2}\dfrac{d[NH_3]}{dt}$

$\dfrac{-d[N_2]}{dt} = \dfrac{1}{2}\dfrac{d[NH_3]}{dt}$

$= \dfrac{1}{2} \times 2 \times 10^{-4}$ mol $L^{-1}s^{-1} = 10^{-4}$ mol L^{-1} s^{-1}

(b) $\dfrac{-d[H_2]}{dt} = \dfrac{3}{2} \times \dfrac{d[NH_3]}{dt}$

$= \dfrac{3}{2} \times 2 \times 10^{-4}$ mol L^{-1} s$^{-1} = 3 \times 10^{-4}$ mol L^{-1} s^{-1}

Sol 4: (i) Reaction of first order in A, second order in B and 0 order w. r. t. C.

$\dfrac{dx}{dt} = k[A]^1 [B]^2 [C]^0$, $k = [D]_t$

$\Rightarrow \dfrac{dx}{dt} = k[A][B]^2$

(ii) If [A], [B], [C] are all doubled.

$r_f = k[2A][2B]^2 = 8k[A][B]^2 = 8r$

Rate becomes 8 times

Sol 5: We have, by ideal gas equation

$PV = nRT \Rightarrow P = \dfrac{n}{V}RT$

$P = CRT$

$C = \dfrac{P}{RT}$

Rate of reaction = $\dfrac{\Delta C}{\Delta t} = \dfrac{1}{RT}\dfrac{\Delta P}{\Delta T}$

We have, R = 0.0921 L atm/mol. k

T = 27°C = 300 K

ΔP = (2 – 1.1) atm = 0.9 atm

ΔT = 75 × 605 = 4500 s

Rate of reaction = $\dfrac{1}{0.0921 \times 300} \times \dfrac{0.9}{75 \times 60}\,Ms^{-1}$

= 7.23 × 10⁻⁶ Ms⁻¹

Rate of reaction in terms of pressure

= $\dfrac{\Delta P}{\Delta t} = \dfrac{0.9}{75}$ atm min⁻¹ = 0.012 atm min⁻¹

Sol 6: $2A + B_2 \rightarrow 2AB$

Since, this is an elementary reaction,

rate, $r_i = k[A]^2[B_2]$

If volume of vessel reduced to one-third, [A] and [B₂] becomes 3 times each.

$\therefore\ r_f = k[3A]^2[3B_2] = 27k\,(A)^2[B_2] = 27r_i$

Hence, rate becomes 27 times.

Sol 7: $3BrO^- \rightarrow BrO_3 + 2Br$
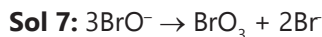
We have,

Rate = $\dfrac{-1}{3}\dfrac{\Delta[BrO]}{\Delta t} = \dfrac{\Delta[BrO_3^-]}{\Delta t}$

$= \dfrac{1}{2}\dfrac{\Delta[Br]}{\Delta t} = k[BrO^-]^{+2} = \dfrac{-\Delta[BrO^-]}{\Delta t} = 3k[BrO^-]^2$

We have, 3k = 0.056

k = 0.0186 mol⁻¹ s⁻¹

(a) $\dfrac{\Delta[BrO_3^-]}{\Delta t} = k[BrO^-]^2 = 0.0186[BrO^-]^2$

Hence rate constant = 0.0186 L mol⁻¹s⁻¹

(b) $\dfrac{\Delta[Br^-]}{\Delta t} = 2k[BrO^-]^2 = 0.037[BrO^-]^2$

Rate constant = 0.037 Lmol⁻¹s⁻¹

Sol 8: We have, $N_2O_5(g) \rightarrow 2NO_2(g) + \dfrac{1}{2}O_2(g)$
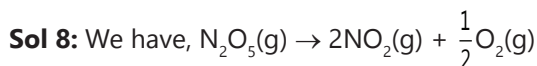
$\Rightarrow \dfrac{-d[N_2O_5]}{dt} = \dfrac{1}{2}\dfrac{d[NO_2]}{dt}$

$= \dfrac{1}{\frac{1}{2}}\dfrac{d[O_2]}{dt} = +k[N_2O_5]$

Hence, $k_1 = k,\ k_2 = 2k,\ k_3 = \dfrac{k}{2}$

$\Rightarrow k_1 = \dfrac{k_2}{2} = 2k_3 \Rightarrow 2k_1 = k_2 = 4k_3$

Sol 9: $4\,{}_1^1H \rightarrow {}_2^4He$; ΔH = 2.6 MeV
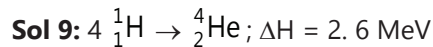
It means 4 atoms of H, eject 26 MeV energy.

Energy released by 1 mole of

$H = \dfrac{N_A}{4}$ = 26 × 10⁶ × 1.6 × 10⁻¹⁴ J = 6.26 × 10¹¹ J

Power output of sun = 3.9×10²⁶ W = 3.9 × 10²⁶ J/s

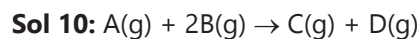i.e. it radiates 3.9 × 10²⁶ J in one second.

Number of moles of H required per second

$= \dfrac{3.9 \times 10^{26}}{6.26 \times 10^{11}}$ = 6.23 × 10¹⁴

Total moles of H on sun = $\dfrac{1.7 \times 10^{30}}{10^{-3}}$ = 1.7 × 10³³

Time taken = $\dfrac{1.7 \times 10^{33}}{6.23 \times 10^{14}}$ = 2.72 × 10¹⁸ s

Sol 10: $A(g) + 2B(g) \rightarrow C(g) + D(g)$

t = 0   0.6   0.8   0   0

t   0.6–x 0.8–2x x   x

Since this is elementary reaction

Rate, $r = k(B)^2(A)$

Now, $r_i = k(0.6)(0.8)^2 = 0.381\,k$

When $P_i = x – 0.2$ atm

$P_A = 0.6 – x = 0.4$ atm

$P_B = 0.8 – 2x = 0.8 – 0.4 = 0.4$ atm

$r_f = k(0.4)(0.4)^2 = 0.064\,k$

$\dfrac{r_f}{r_i} = \dfrac{0.064}{0.384} = \dfrac{1}{6}$

Sol 11: $A \rightarrow B$

k = 1.2 × 10⁻² Ms⁻¹

Since unit of rate constant is Ms⁻¹, it is zero order reaction

Rate law [B] = kt

At t = 10 min

[B] = 1.2 × 10⁻² × 10 × 60 M

[B] = 7.2 M

At t = 20 min

[B] = 1.2 × 10⁻² × 20 × 60 M = 14.4 M

But, $[A]_0 = 10$ M and [B] cannot be greater than $[A]_0$ $[A]_0$.

$\therefore$ [B] = 14.4 M implies that reaction has reached completion, i. e.

$[B]_{max} = 10$ M

[B] = 10 M

Sol 12: For zero order reaction,

$[A] = [A]_0 - kt$

At t = 0, $[A] = [A]_0 = 0.1$ M

At t = 1 min, [A] = 0.09 M

0.09 = 0.1 – k

$\Rightarrow$ k = 0.01 M min^{-1}

At t = 2 min, [A] = 0.1 – 0.01 × 2

= 0.08 M, which is the value given.

$\therefore$ k = 0.01 M min^{-1}

Sol 13: For zero order reaction

$[A] = [A]_0 - kt$

We are given,

k = 2 × 10^{-2} mol L^{-1}sec^{-1}

and at t = 25 sec, (A) = 0.25 M

$[A]_0 = [A] + kt$

= 0.25 + 2 × 10^{-2} × 25 = 0.75 M

Sol 14: It is a zero order reaction ($\because$ unit of rate constant is M sec^{-1})

$[H^+]_0 = \dfrac{6 \times 10^{-6}}{0.1 \times 10^{-3}}$ = 6 × 10^{-2} M

k = 10^7 mol L^{-1} sec^{-1}

Time taken to disappear = $\dfrac{[H^+]}{k}$

= $\dfrac{6 \times 10^{-2}}{10^7}$ sec = 6 × 10^{-9} sec

Sol 15: Since it is a zero order reaction

$[A] = [A]_0 - kt$

When t = 1 hour, $[A] = \dfrac{1}{4} [A]_0$

($\because$ 75% reacted)

$\therefore \dfrac{1}{4} [A]_0 = [A]_0 - k$

$\Rightarrow$ k = $\dfrac{3}{4} [A]_0$ M hr^{-1}

When A is 10% unreacted,

$[A] = \dfrac{1}{10} [A_0]$

$\therefore \dfrac{1}{10} [A]_0 = [A]_0 - kt$

$\Rightarrow \dfrac{9}{10} [A]_0 = \dfrac{3}{4} [A]_0 t$

$\Rightarrow$ t = 1.2 hr

Sol 16: (i) We know, for first order reaction

$[A] = [A]_0 e^{-kt}$

k = $\dfrac{1}{t} \ln \dfrac{[A]_0}{[A]}$

At t = 72 min, 75% reaction completed, i. e. $[A] = \dfrac{1}{4} [A]_0$

$\therefore$ k = $\dfrac{1}{72} \ln 4$ = 0.019 min^{-1}

When reaction is 50% complete,

t = $t_{1/2}$ = $\dfrac{\ln 2}{k}$ = 36 min

(ii) When reaction is 87.5% complete, [A] = 0.125$[A]_0$,

$\therefore$ t = $\dfrac{1}{k} \ln \dfrac{1}{0.125}$

t = 108 min

Sol 17: We have, for first order reaction

k = $\dfrac{1}{t} \ln \dfrac{[A]_0}{[A]_t}$

(i) At t = 10 min, reaction is 20% complete, i. e. [A] = 0.8$[A]_0$

k = $\dfrac{1}{10} \ln \dfrac{[A]_0}{0.8[A]_0}$

k = 0.0223 min^{-1}

(ii) When reaction is 75% complete,

$[A] = \dfrac{1}{4} [A]_0$

t = $\dfrac{1}{k} \ln \dfrac{[A]_0}{[A]_t}$ = $\dfrac{1}{0.0223} \ln \dfrac{[A]_0}{\dfrac{1}{4}.[A]_0}$

t = 62.17 min.

Sol 18: Order will be equal to 1.

t = $\dfrac{1}{k} \ln \dfrac{[A]_0}{[A]_t}$

When reaction is 99. 9 % complete,

$[A]_t = 10^{-3} [A]_0$

$t_1 = \dfrac{1}{k}\ln\dfrac{[A]_0}{10^{-3}[A]_0} = \dfrac{3}{k}\ln 10 = \dfrac{6.909}{k}$

When reaction is 50% completed, $[A]_t = \dfrac{[A]_0}{2}$

$\therefore t_2 = \dfrac{1}{k}\ln\dfrac{[A]_0}{0.5[A]_0} = \dfrac{\ln 2}{k} = \dfrac{0.693}{k}$

We see that $t_2 \approx 10 t_1$

Sol 19: We have, first order reaction

$N = N_0 e^{-kt}$

here, $k = 1.5 \times 10^{-3} \text{ sec}^{-1}$

$N \propto 1.25$ (wt. $\propto$ molar)

$N \propto 5$

$\therefore 1.25 = 5e^{-1.5\times 10^{-3}t}$

$\Rightarrow t = \dfrac{1}{1.5\times 10^{-3}}\ln\dfrac{5}{1.25}$

$t = 924.3625$

Sol 20: We have,

$[N]_0 = 500$

At $t = 20$ months, $[N]_t = 420$,

Using first order to rate law,

$k = \dfrac{1}{t}\ln\dfrac{[N]_0}{[N]_t}$

$k = 8.717 \times 10^{-3} \text{ month}^{-1}$

The drug will be ineffective (will expire) when it has decomposed 30%, i. e. $[N] = 0.7 [N]_0$.

$\therefore t = \dfrac{1}{t}\log\dfrac{[N]_0}{[N]_t} = \dfrac{1}{8.717\times 10^{-3}}\log\dfrac{[N]_0}{0.7[N]_0}$

$t \approx 41$ months

Sol 21: For first order reaction

$k = \dfrac{1}{t}\log\dfrac{[A]_0}{[A]_t}$

We are given, 2% of virus gets inactivated every minute at the beginning, i. e. , at $t = 1$ min, $[A]_t = 0.98[A]_0$

$k = \dfrac{1}{1}\log\dfrac{[A]_0}{0.98[A]_0}$

$k = 0.02 \text{ min}^{-1}$

$k = 3.3 \times 10^{-4} \text{ sec}^{-1}$.

Sol 22: If we assume the reaction to be of first order, then, let $[A]_t = \alpha$ and $[A]_0 = C_0$.

$a = C_0 e^{-kt}$

At time

$t = 0, \alpha = C_0$

$t = t, \alpha = C_0 e^{-k} = aC_0, a = e^{-k}$

$t = 2t, \alpha = C_0 e^{-2k} = a^2 C_0, a = e^{-k}$

$t = 3t, \alpha = C_0 e^{-3k} = a^3 C_0, a = e^{-k}$

Therefore, taking the reaction to be of first order, we found the concentration of A to be of the form given in question. Therefore, the reaction is of first order.

Sol 23: For first order reaction,

$[SO_2Cl_2] = [SO_2Cl_2]_0\, e^{-kt}$

$k = 2.2 \times 10^{-5} \text{ sec}^{-1}$,

$t = 90 \text{ min} = 5400 \text{ sec}$

$\therefore \dfrac{[SO_2Cl_2]}{[SO_2Cl_2]_0} = e^{-5400\times 2.2\times 10^{-5}} = 0.888$

11. 2 % of $[SO_2Cl_2]$ decomposed.

Sol 24: For A, $k_1 = \dfrac{\ln 2}{t_{1/2}} = \dfrac{\ln 2}{5}$

Initial concentration $= a_0$

Let $[A]_t = a$

Then, $a = e_0\, e^{-k_1 t}$

For B, $k_2 = \dfrac{\ln 2}{t_{1/2}} = \dfrac{\ln 2}{1.5}$

Initial concentration

$[B]_0 = \dfrac{[A]_0}{4} = \dfrac{a_0}{4}$

$[B]_4 = b$

Then, $b = \dfrac{a_0}{4}e^{-k_2 t}$

When $a = b$,

$a_0 e^{-k_1 t} = \dfrac{a_0}{4}e^{-k_2 t}$

$4 = e^{(k_1 - k_2)t}$

$\Rightarrow t = \dfrac{\ln 4}{k_1 - k_2}$

$$= \frac{\ln 4}{\frac{\ln 2}{5} - \frac{\ln 2}{15}} = \frac{2\ln 2}{\ln 2\left(\frac{1}{5} - \frac{1}{15}\right)} = \frac{2 \times 5 \times 15}{10}$$

t = 15 min.

Sol 25: From the data, we observe that, when $[H_2]$ is halved, keeping [NO] constant, reaction rate gets halved. So, order w. r. t H_2 is 1.

When [NO] is doubled, keeping $[H_2]$ constant, reaction rate becomes 4 times so, order w. r. t. NO is 2.

Rate = $k[NO]^2 [H_2]$

(a) Order = 2 + 1 = 3

(b) When, [NO] = 1. 5 × 10⁻⁴ M,

$[H_2]$ = 4 × 10⁻³ M,

Rate = 4. 4 × 10⁻⁴ M sec⁻¹

$$\therefore k = \frac{4.4 \times 10^{-4}}{(1.5 \times 10^{-4})^2 \times (4 \times 10^{-3})^2}$$

When [NO] = 1. 1 × 10⁻³ M,

$[H_2]$ = 1. 5 × 10⁻³ M

(c) Rate = 4. 88 × 10⁶ × (1. 1 × 10⁻³)² × (1. 5 × 10⁻³)

Rate = 8. 85 × 10⁻³ M sec⁻¹

Sol 26: From given data, we observe that, when $[Cl_2]$ is tripled, rate becomes 3 times, so, order w. r. t. Cl_2 is 1.

When [NO] is tripled, rate becomes 9 times, so, order w. r. t [NO] is 2.

(a) Order w. r. t. NO = 2

Cl = 1

(b) Rate = $k[NO]^2 [Cl_2]$

(c) When $[Cl_2]$ = 0. 05 M, [NO] = 0. 05 M,

Rate = 10⁻³

$$k = \frac{rate}{[NO]^2[Cl_2]} = \frac{10^{-3}}{(0.05)^2(0.05)} = 8 \text{ M}^{-2} \text{ sec}^{-1}$$

(d) If $[Cl_2]$ = 0. 2 M, [NO] = 0. 4 M,

Rate = $k[NO]^2 [Cl_2]$ = 8 × (0. 4)² (0. 2)

Rate = 0. 256 mol sec⁻¹ L⁻¹

Sol 27: Let us assume that this is first order reaction. i. e. $[A] = [A]_0 e^{-kt}$. Using this, we will calculate k at both times. If they are same, then our assumption is correct.

At t = 53 min, 50% reaction completed, i. e. [A] = 0. 5[A]₀

$$\therefore k = \frac{\ln 2}{t} = \frac{0.693}{53} = 0.013 \text{ min}^{-1}$$

(i) We see that both values of k are same, this is first order reaction.

(ii) $\frac{[N_2O]}{[N_2O]_0} = e^{-kt} = e^{-1.3 \times 10^{-2} \times 100} = 0.27$

Thus 73% of N_2O will decompose.

Sol 28: As in previous question, we assume order = 0 and calculate k at different time.

At t = 0 sec, P = P_0 = 4 × 10³ Pa

At t = 100 sec, P = 3. 5 × 10³ Pa

We have, $k_1 = \frac{P_0 - P}{t} = \frac{(4 - 3.5) \times 10^3}{100}$ Pa/s

k_1 = 5 Pa/s

At t = 200 sec, P = 2 × 10³ Pa

$k = k_2 = \frac{(4 - 3) \times 10^3}{200} = 5$ Pa/s

At t = 300 sec, P = 2. 5 × 10³ Pa

$k_3 = \frac{(4.2.5) \times 10^3}{300} = 5$ Pa

We see that $k_1 = k_2 = k_3 = 5$ Pa/s is same for all. Hence this is zero order reaction, rate constant = 5 Pa/s

Sol 29: We know, for nth order reaction

$$t_{1/2} \propto \frac{1}{[A]_0^{n-1}}$$
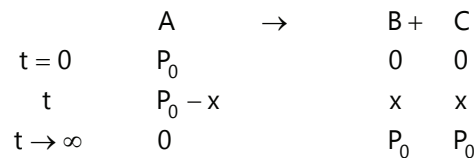
We have, at $[A]_0$, $(t_{1/2})_1 = t = 50$ min

at $\frac{[A]_0}{2}$, $(t_{1/2})_2 = 25$ min

$$\therefore \frac{50}{25} = \left[\frac{\left(\frac{[A]_0}{2}\right)}{[A]_0}\right]^{n-1} = \frac{1}{2^{n-1}}$$

$2 = \frac{1}{2^{n-1}} \Rightarrow 2^{n-1} = 2^{-1}$

n − 1 = −1

$\Rightarrow$ n = 0

Sol 30:

$$\begin{array}{llll} & A & \rightarrow & B + \quad C \\ t = 0 & P_0 & & 0 \quad\; 0 \\ t & P_0 - x & & x \quad\; x \\ t \rightarrow \infty & 0 & & P_0 \; P_0 \end{array}$$

We have, at time $t = t_1$

$P_1 = P_t = P_0 - x + x + x$

$P_2 = P_0 + x \Rightarrow x = P_2 - P_0$

At time, $t \rightarrow \infty$,

$P_t = P_3 = 2P_0$

$\Rightarrow P_0 = \dfrac{P_3}{2}$

Taking first order reaction,

$$k = \frac{1}{t}\ln\frac{(P_A)_0}{(P_A)_t} = \frac{1}{t}\ln\frac{P_0}{P_0 - x} = \frac{1}{t}\ln\frac{P_0}{P_0 - P_2 + P_0}$$

$$k = \frac{1}{t}\ln\frac{P_0}{2P_0 - P_2} = \frac{1}{3}\ln\frac{P_3}{2(P_3 - P_2)}$$

Sol 31: Here, we have, at time t

$$P_B + P_C = P_2 = 2x \Rightarrow x = \frac{P_2}{2}$$

at time $t \rightarrow \infty$, $P_B + P_0 = P_3 = 2P_0$

$$\Rightarrow P_0 = \frac{P_3}{2}$$

$$k = \frac{1}{t}\ln\frac{(P_A)_0}{(P_A)_t} = \frac{1}{t}\ln\frac{P_3}{\left(\dfrac{P_3}{2} - \dfrac{P_2}{2}\right)} = \frac{1}{t}\ln\frac{P_3}{P_3 - P_2}$$

Sol 32:

$$\begin{array}{llll} A & \rightarrow & B & + \quad C \\ \text{time} \\ t = 0 & n_0 & 0 & \quad 0 \\ t & n_0 - x & x & \quad x \\ t \rightarrow \infty & 0 & n_0 & \quad n_0 \end{array}$$
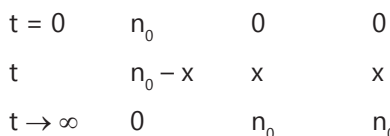
At time, $t = 0$, $V_r = V_1 = \dfrac{n_0 - a}{N}$

$$\Rightarrow n_0 = \frac{NV_1}{a}$$

(n-factor of A, B, C = a)

(using $NV_1 = n_0 a$)

Normality of reagent = N

At time, $t = t$,

$$V_n = V_2 = \frac{(n_0 - x)a + xa + xa}{N} = \frac{(n_0 + x)a}{N}$$

$$\Rightarrow n_0 + x = \frac{NV_2}{a}$$

$$x = \frac{NV_0}{a} - n_0 = \frac{N}{a}(V_2 - V_1)$$

$$k = \frac{1}{t}\ln\frac{n_0}{n_t} = \frac{1}{t}\ln\frac{n_0}{n_0 - x}$$

$$= \frac{1}{t}\ln\frac{\dfrac{NV_1}{a}}{\left(\dfrac{NV_1}{a} - \dfrac{N}{a}\right)(V_2 - V_1)}$$

$$k = \frac{1}{t}\ln\frac{V_1}{2V_1 - V_2}$$

Sol 33:

$$\begin{array}{lllll} & & A & \rightarrow \; 2B & + \; 3C \\ \text{Time, } t = 0 & & a \\ \text{Time, } t & & a - x & 2x & 3x \\ \text{Time, } t \rightarrow \infty & & 0 & 2a & 3a \end{array}$$

Let n-factor of A, B and C be n and normality of reagent = N then at time, t

$N. V_2 = (a - x)n + 2xn + 3xn$

$NV_2 = n(a + 4x)$

$$a + 4x = \frac{NV_2}{n}$$

at time, $t \rightarrow \infty$

$NV_3 = 2a. n + 3a. n$

$\Rightarrow a = NV_3 = 5an$

$$a = \frac{NV_3}{5n}$$

Then $4x = \dfrac{NV_2}{n} - \dfrac{NV_3}{5n}$

$$x = \frac{N}{4n}\left(V_2 - \frac{V_3}{5}\right)$$

$$k = \frac{1}{t}\ln\frac{a}{a - x} = \frac{1}{t}\ln\frac{NV_3}{5n\left(\dfrac{NV_3}{5n} - \dfrac{NV_2}{4n} + \dfrac{NV_3}{20n}\right)}$$

$$= \frac{1}{t}\ln\frac{V_3}{V_3 - \dfrac{5}{4}V_2 + 4V_3} = \frac{1}{t}\ln\frac{4V_3}{5(V_3 - V_2)}$$

$$k = \frac{1}{t}\ln\frac{4}{5}\frac{V_3}{\left(V_3 - V_2\right)}$$

Sol 34:   S→G+F

Time t = 0   a   0   0

Time, t   a–x   x   x

Time t → ∞   0   a   a

Let specific rotation of Glucose and Fructose be θ_1 and θ_2 respectively

Then, at time t

$x\theta_1 + x\theta_2 = r_t$

$x = \dfrac{r_t}{\theta_1 + \theta_2}$

At time, t → ∞

$a\theta_1 + a\theta_2 = r_\infty$

$a = \dfrac{r_\infty}{\theta_1 + \theta_2}$

$k = \dfrac{2.303}{t}\log\dfrac{a}{a-x} = \dfrac{1}{t}\log\dfrac{a}{a-x}$

$k = \dfrac{1}{t}\log\dfrac{r_\infty}{(\theta_1 + \theta_2)\left(\dfrac{r_\infty}{\theta_1 + \theta_2} - \dfrac{r_t}{\theta_1 + \theta_2}\right)}$

$k = \dfrac{1}{t}\log\dfrac{r_\infty}{r_\infty - r_1}$

Sol 35: As $H_3(g) \rightarrow As(s) + \dfrac{3}{2}H_2(g)$

t = 0 P_0

t = 1 $P_0 - x \dfrac{3}{2}x$

Since, as a solid, it won't contribute to pressure.

∴ At time t, $P_t = P_0 - x + \dfrac{3}{2}x = P_0 + \dfrac{x}{2}$

Let's assume reaction is first order and calculate k at different times, using $k = \dfrac{1}{4}\ln\dfrac{P_0}{P_0 - x}$

t = 0 $P_0 = 758 = P_t$

t = 5 hrs , $P_t = 827 = P_0 + \dfrac{x}{2}$

$827 = 758 + \dfrac{x}{2}$

⇒ x = 138 mm

$k = \dfrac{1}{5}\ln\dfrac{758}{758-138}$

k = 0. 04 hr⁻¹

t = 7. 5 hr, Pt = 856 = $P_0 + \dfrac{x}{2}$

$\Rightarrow \dfrac{x}{2} = 856 - 758$

x = 196 mm

$k = \dfrac{1}{7.5}\ln\dfrac{758}{758 - 196}$

k = 0. 039 hr⁻¹

t = 10 hr, $P_t = 889 = P_0 + \dfrac{x}{2}$

x = 2(883 − 758)

x = 248 mm

$k = \dfrac{1}{10}\ln\dfrac{758}{758 - 248}$

k = 0. 039 hr⁻¹

Thus, all 3 values of k are approximately the same, hence first order reaction.

Sol 36 : $(CH_3)_2O(g) \rightarrow CH_4(g) + H_2(g) + CO(g)$

Time t = 0 P_0 0   0   0

Time, t $P_0 - x$ x   x   x

t → ∞   0 P_0 P_0 P_0

Total pressure, at time t,

$P_t = P_0 - x + x + x + x = P_0 + 2x$

Increase in pressure = $(P_0 + 2x) - P_0 = 2x$

We will assume that this is a first order reaction and check the consistency of given data.

At t = 0, P_0 = 312 mm Hg

At t = 390 s, pressure increases;

ΔP = 96 mm Hg = 2x

x = 48 mm Hg

∴ $k = \dfrac{1}{t}\ln\dfrac{P_0}{P_0 - x} = \dfrac{1}{390}\ln\dfrac{312}{312 - 48}$

k = 4. 28 × 10⁻⁴ s

At t = 1195 s, ΔP = 250 = 2x

x = 125 mm Hg

$k = \dfrac{1}{1195}\ln\dfrac{312}{312 - 125}$ = 4. 28 × 10⁻⁴ s

At t = 3155 s, ΔP = 467 = 2x

x = 233. 5 mm Hg

$k = \dfrac{1}{3155}\ln\dfrac{312}{312 - 233.5}$ = 4. 30 × 10⁻⁴ sec⁻¹
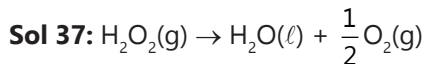
At $t \to \infty, \Delta P = 2P_0 = 624$ mm Hg

≈ 619 mm Hg

Thus, we see that all 3 values of k are approximately the same. Therefore, this is a first order reaction.

So, rate = $k[(CH_3)_2O]$, k

= 4.28×10^{-4} sec^{-1}

Sol 37: $H_2O_2(g) \to H_2O(\ell) + \frac{1}{2}O_2(g)$

Here, $V_r \propto [H_2O_2]$

Assuming this is a first order reaction

$k = \dfrac{2.303}{t}\log\dfrac{[H_2O_2]_0}{[H_2O_2]_t} = \dfrac{1}{t}\log\dfrac{V_0}{V_t}$

At time, t = 0, V_r 22.8 cc = V_0

t = 10, V_r = 13.3 cc = V_t

$k_1 = \dfrac{2.303}{10}\log\dfrac{22.8}{13.3} = 5.4 \times 10^{-2}$ min^{-1}

t = 20, V_r = 8.25 cc = V_t

$k_2 = \dfrac{2.303}{20}\log\dfrac{22.8}{8.25} = 5.1 \times 10^{-2}$ min^{-1}

k_1 and k_2 are equal within experimental error.

Therefore, first order reaction.

Sol 38: For inversion of cane sugar, assuming first order,

$k = \dfrac{1}{t}\log\dfrac{\theta_0 - \theta_\infty}{\theta_f - \theta_\infty}$

At time, t = 0, $\theta = \theta_0 = +13.1$

At time, $t \to \infty, \theta = \theta_\infty = -3.8$

At time, t = 60, $\theta_+ = 11.6°$

Sol 39: $\quad A(g) \to 2B(g) + C(g)$
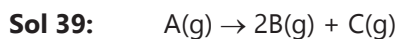
Time, t = 0 $\quad P_0 \qquad 0 \qquad 0$

Time, t $\qquad P_0 - x \quad 2x \qquad x$

Time, t→∞ $\quad 0 \qquad 2P_0 \quad P_0$

At, $t \to \infty, P_t = 3P_0 = 270$ mm Hg

$P_0 = 90$ mm Hg = (P_A)

At, t = 10 min, $P_t = P_0 - x + 2x + x = P_0 + 2x = 176$

$2x = 176 - 90$

x = 43 mm Hg

$(P_A)_+ = P_0 - x = 90 - 43 = 47$ mm Hg

Now, since, this is first order reaction.

$k = \dfrac{2.303}{t}\log\dfrac{(P_A)_0}{(P_A)_+} = \dfrac{2.303}{10}\log\dfrac{90}{47}$

$k = 6.49 \times 10^{-2}$ min^{-1}

$k_1 = \dfrac{1}{60}2.303\log\dfrac{13.1-(-3.8)}{11.6-(-3.8)}.$

$= 1.55 \times 10^{-3}$ min^{-1}

At time, t = 120 min, $\theta_t = +10.2°$

$k_2 = \dfrac{2.303}{120}\log\dfrac{(13.1)-(-3.8)}{(10.2)-(-3.8)} = 1.57 \times 10^{-3}$ min^{-1}

At time, t = 180 min, $\theta_t = +9.0°$

$k_3 = \dfrac{2.303}{180}\log\dfrac{(13.1)-(-3.8)}{(9.0)-(-3.8)} = 1.54 \times 10^{-3}$ min^{-1}

At time, t = 360 min, $\theta_t = +5.87°$

$k_4 = \dfrac{2.303}{360}\log\dfrac{(13.1)-(-3.8)}{(5.87)-(-3.8)} = 1.55 \times 10^{-3}$ min^{-1}

We see that, k_1, k_2, k_3 and k_4 are all same within experiment value.
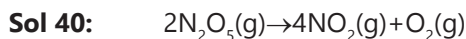
Therefore, this is a first order reaction

Half-life = $\dfrac{0.693}{k} = \dfrac{0.693}{6.49 \times 10^{-2}} = 10.677$ min

(i) $(P_A)_i = 90$ mm Hg

(ii) $(P_A)_f = 47$ mm Hg

(iii) $k = 6.49 \times 10^{-2}$ min^{-1}

(iv) $t_{1/2} = 10.67$ min

Sol 40: $\qquad 2N_2O_5(g) \to 4NO_2(g) + O_2(g)$

time, t = 0 $\quad P_0 \qquad\qquad 0 \qquad\qquad 0$

time, t = t $\quad P_0 - 2x \qquad 4x \qquad\quad x$

$t \to \infty \qquad 0 \; 2 \qquad\quad P_0 \qquad\quad \dfrac{P_0}{2}$

At $t \to \infty$, $P_t = 584.5 = 2P_0 + \dfrac{P_0}{2}$

$\Rightarrow \dfrac{5P_0}{2} = 584.5$

$\Rightarrow P_0 = 233.8$ mm Hg

At t = 30 min,

$P_t = 284.5 = P_0 - 2x + 4x + x$

$\Rightarrow P_0 + 3x = 284.5$

$3x = 284.5 - 233.8$

$x = 16.9$ mm Hg

$P_{N_2O_5} = P_0 - 2x$

$= 233.8 - 2 \times 16.9 = 200$ mm Hg

We have,

$$\frac{-1}{2}\frac{d[N_2O_5]}{dt} = k[N_2O_5]$$

$$\int_{[N_2O_5]_0}^{[N_2O_5]_t} \frac{d[N_2O_5]}{[N_2O_5]_0} = -2k\int_0^t dt$$

$$\ln\frac{[N_2O_5]_t}{[N_2O_5]_0} = -2kt$$

$$k = \frac{2.303}{2t}\log\frac{[N_2O_5]_0}{[N_2O_5]_t}$$

$$k = \frac{2.303}{2t}\log\frac{(P_{N_2O_5})_0}{(P_{N_2O_5})_t} \quad (\because P_{N_2O_5} \propto [N_2O_5])$$

$$= \frac{2.303}{2\times30}\log\frac{233.8}{200}$$

$k = 2.605 \times 10^{-3}$ min^{-1}.

Sol 41: (a) Assuming first order reaction

$$k = \frac{2.303}{t}\log\frac{V_0}{V_t}$$

We have, $V_0 = 22.8$ cc

At t = 10 min, $V_t = 13.8$ cc

$$k_1 = \frac{2.303}{10}\log\frac{22.8}{13.8} = 5.02 \times 10^{-2} \text{ min}^{-1}$$

At t = 20 min, $V_t = 8.25$ cc

$$k_2 = \frac{2.303}{20}\log\frac{22.8}{8.25} = 2 \times 10^{-2} \text{ min}^{-1}$$

Since, $k_1 \approx k_2$. This is first order reaction.

(b) $t_{1/2} = \dfrac{0.693}{k} = \dfrac{0.693}{5.05\times10^{-2}} = 13.75$ min

(c) At t = 25 min,

$$k = \frac{2.303}{25}\log\frac{V_0}{V_t}$$

Fraction decomposed

$$\frac{V_t}{V_0} = 1.10 \frac{-25\times5.05\times10^{-2}}{2.303} = 1 - 0.284$$

Fraction decomposed = 0.716

Sol 42: $H_2O_2 \rightarrow H_2O + \frac{1}{2}O_2$
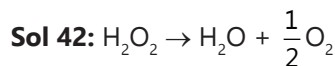
We are given complete dissociation gives 46.34 mL O_2.

Also $V_{O_2} \propto [H_2O_2]$

(V_{O_2} is volume of O_2 a given sample of H_2O_2 can give)

$\therefore [H_2O_2]_0 \propto 46.34$

Also, at t = 5.1 days, $V_{O_2} = 10.31$ mL

Then $[H_2O_2]_t \propto (46.34 - 10.31)$

So, $k = \dfrac{2.303}{t}\log\dfrac{[H_2O_2]_0}{[H_2O_2]_t}$

$$k = \frac{2.303}{5.1}\log\frac{46.34}{46.34-10.31}$$
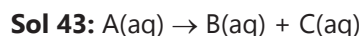
$k = 4.93 \times 10^{-2}$ days^{-1}.

When 20 mL, O_2 lost,

$[H_2O_2]_t \propto (46.34 - 20.00)$

$$t = \frac{2.303}{k}\log\frac{[H_2O_2]_0}{[H_2O_2]_0 - [H_2O_2]_t}$$

$$= \frac{2.303}{4.93\times10^{-2}}\log\frac{46.34}{46.34-20}$$

t = 11.45 days

Sol 43: $A(aq) \rightarrow B(aq) + C(aq)$

t = 0	n_0		
t = t	$n_0 - x$	x	x
t $\rightarrow \infty$	0	n_0	n_0

At $t \rightarrow \infty, \theta_\infty = -5° = n_0 \cdot \theta_B + n_0\theta_C$

We have, $\theta_A = 20°$, $\theta_B = 30°$,

$\theta_C = -40°$

$\therefore 30n_0 - 40n_0 = -5$

$n_0 = 0.5$

At time, t = 6.43 min.

$\theta_t = (n_0 - x)\theta_A + x(\theta_B + \theta_C) = 2.5$

$20n_0 + x(30.40 - 20) = 2.5$
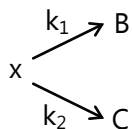
$30x = 20 \times 0.5 - 2.5$

$30x = 7.5$

$x = 0.25$

For first order conversion,

$k = \dfrac{2.303}{t}\log\dfrac{n_0}{n_0 - x}$

$= \dfrac{2.303}{6.93}\log\dfrac{0.5}{0.5 - 0.25}$

$k = 0.1 \, min^{-1}$

Sol 44:

$$x \begin{array}{c} \nearrow^{k_1} B \\ \searrow_{k_2} C \end{array}$$

$(B = y, C = z)$

We have,

$\dfrac{d[x]}{dt} = -(k_1 + k_2)[x]$

$\displaystyle\int_{[x]_0}^{[x]_t} \dfrac{d[x]}{[x]} = -(k_1 + k_2)\int_0^t dt$

$\Rightarrow [x]_t = [x]_0 e^{-kt}, \, k = k_1 + k_2$

Now, $\dfrac{d[B]}{dt} = k_1[x]_t$

$\dfrac{d[B]}{dt} = k_1[x]_0 e^{-kt}$

$\displaystyle\int_0^{[B]_t} d[B] = k_1[x]_0 \int_0^t e^{-kt}$

$[B]_t = \dfrac{-k_1[x]_0}{k} e^{-kt}\Big|_0^t$

$[B]_t = \dfrac{-k_1[x]_0}{k_1 + k_2}(1 - e^{-kt})$

Similarly $[C]_t = \dfrac{k_2[x]_0}{k_1 + k_2}(1 - e^{-kt})$

$[B]_t + [C]_t = [y] + [x]$

$= \dfrac{k_1[x]_0}{k}(1 - e^{-kt}) + \dfrac{k_2[x]_0}{k}(1 - e^{-kt})$

$= \left(\dfrac{k_1 + k_2}{k}\right)[x]_0(1 - e^{-kt}) = [x]_0 \, e^{(1 - e^{-kt})}$

$\therefore \dfrac{[x]_t}{[y] + [2]} = \dfrac{e^{-kt}}{1 - e^{-kt}} = \dfrac{1}{e^{+(k_1 + k_2)t} - 1}$

Sol 45: Using results of previous question

$[C]_t = \dfrac{k_2[A]_0}{k}(1 - e^{-kt}), \, k = k_1 + k_2$

$[A]_t = [A]_0 e^{-kt}$

$\dfrac{[C]_t}{[A]_t} = \dfrac{k_2}{k_1 + k_2}\dfrac{(1 - e^{-kt})}{e^{-kt}} = \dfrac{1}{1 + \dfrac{k_1}{k_2}}(e^{-kt} - 1)$

We have, $k_1 = x \, hr^{-1}, \, k_2 = 10 \, k_1$

$= 10 \times hr^{-1}, \, t = 1 \, hr$

$\therefore \dfrac{[C]_t}{[A]_t} = \dfrac{1}{1 + \dfrac{1}{10}}(e^{(x + 10x)} - 1)$

$\dfrac{[C]_t}{[A]_t} = \dfrac{10}{11}(e^{11x} - 1)$

Sol 46: We have,

$A \xrightarrow{k_1} B \xrightarrow{k_2} C,$
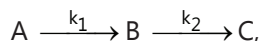
$k_1 = \dfrac{\ln 2}{\ln 1}, \, k_2 = \dfrac{\ln 2}{2}$

For [A]

$\dfrac{d[A]}{dt} = -k_1[A]$

$\Rightarrow [A] = [A]_0 e^{-k_1 t}$

$\dfrac{d[B]}{dt} = k_1[A] - k_2[B]$

$\dfrac{d[B]}{dt} = k_1[A]_0 e^{-k_1 t} - k_2[B]$

$\dfrac{d[B]}{dt} + k_2[B] - k_1[A]_0 \, e^{-k_1 t} = 0 \ldots(i)$

This is a linear differential equation.

Solving this, we get

$[B]_t = \dfrac{k_1[A]_0}{k_2 - k_1}[e^{-k_1t} - e^{-k_2t}]$

Now, at $[B]_{max}$, $\dfrac{d[B]_t}{dt} = 0$

In (i), putting $\dfrac{d[B]_t}{dt} = 0$, we get

$k_1[A]_0\, e^{-k_1t} = k_2[B]$

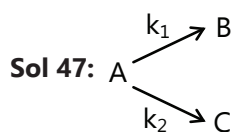$k_1[A]_0\, e^{-k_1t} = \dfrac{k_2 k_1[A]_0}{k_2 - k_1}[e^{-k_1t} - e^{-k_2t}]$

$k_2 e^{-k_1t}.k_1 e^{-k_1t} = k_2 e^{-k_1t}.k_2 e^{-k_2t}$

$\dfrac{k_1}{k_2} = e^{(k_1 - k_2)t}$

$t = \left(\dfrac{\log k_1 - \log k_2}{k_1 - k_2}\right).2.303$

$t = \dfrac{1}{k_1 - k_2}\ln\dfrac{\ln 2}{4.\ln 2} = \dfrac{-4}{\ln 2}\ln\dfrac{1}{2} = 4$

∴ t = 4 min.

Sol 47: $A \begin{array}{c} \overset{k_1}{\nearrow} B \\ \underset{k_2}{\searrow} C \end{array}$

$\dfrac{[B]}{[C]} = \dfrac{k_1}{k_2}$

We need, $\dfrac{[B]}{[C]} = 2 = \dfrac{k_1}{k_2}$

Let temperature be T.

By Arrhenius equation.

$\log\dfrac{k_2}{k_1} = \dfrac{E_a}{2.303R}\left(\dfrac{1}{T_1} - \dfrac{1}{T_2}\right)$

For $A \xrightarrow{k_1} B$, $k_2 = k_1$, $k_1 = 8$,

$E_a = 20$ kJ/mol (E_1), $T_1 = 300$, $T_2 = T$

$\log\dfrac{k_1}{8} = \dfrac{(E_a)_1}{2.303R}\left(\dfrac{1}{300} - \dfrac{1}{T}\right)$

$k_1 = 8$ antilog $\left[\dfrac{(E_a)_1}{2.303R}\left(\dfrac{1}{300} - \dfrac{1}{T}\right)\right]$

For $A \xrightarrow{k_2} C$, similarly,

$k_2 = 2$ antilog $\left[\dfrac{(E_a)_2}{2.303R}\left(\dfrac{1}{300} - \dfrac{1}{T}\right)\right]$

$\dfrac{k_1}{k_2} = 2$

4antilog$\left[\dfrac{((E_a)_1 - (E_a)_2)}{2.303R}\right]\left(\dfrac{1}{300} - \dfrac{1}{T}\right) = 2$

$\dfrac{(E_a)_1.(E_a)_2}{2.303R}\left(\dfrac{1}{300} - \dfrac{1}{T}\right) = \log\dfrac{1}{2}$
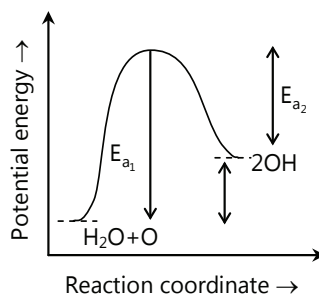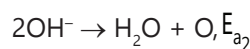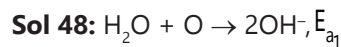
$(E_a)_1 = 20$ kJ/mol,

$(E_a)_2 = 2.8314$ kJ/mol

$\Rightarrow \dfrac{(28.314 - 20)\times 10^3}{8.314}\left(\dfrac{1}{300} - \dfrac{1}{T}\right) = 0.7$

$\dfrac{1}{300} - \dfrac{1}{T} = 7\times 10^{-4}$

$\dfrac{1}{T} = 2.63\times 10^{-3}$

T = 379.75 K

Sol 48: $H_2O + O \rightarrow 2OH^-, E_{a_1}$

$2OH^- \rightarrow H_2O + O, E_{a_2}$

$E_{a_2} = E_{a_1} - \Delta H = (77.72)$ kJ mol^{-1}

$E_{a_2} = 5$ kJ mol^{-1}

Sol 49: For $t_{1/2} = 1$ min, k = $\dfrac{0.693}{t_{1/2}}$

= 0.693 min^{-1} = 1.155 × 10^{-2}s

Now, $k = A e^{\frac{-E_a}{RT}} \Rightarrow T = \dfrac{E_a}{R}\left(\ln\dfrac{A}{k}\right)^{-1}$

A = 5 × 10^{13} sec^{-1}

$E_a = 104.5$ kJmol^{-1}

$T = \dfrac{104.5\times 10^3}{8.134}\left(\ln\dfrac{5\times 10^{13}}{1.155\times 10^{-2}}\right)^{-1}$

T = 349.1 K

Sol 50: From Arrhenius equation

$$\log \frac{k_2}{k_1} = \frac{E_a}{2.303R}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

For $T_1 = 27°C = 300$ K and

$T_2 = 47°C = 320$ K, $\frac{k_2}{k_1} = 4$

$$\therefore \log 4 = \frac{E_a}{2.303 \times 8.314}\left(\frac{1}{300} - \frac{1}{320}\right)$$

$$E_a = \frac{\log 4 \times 2.303 \times 8.314 \times 300 \times 320}{20}$$

$E_a = 55.33$ kJ/mol

Sol 51: For $t_{1/2} = 2$ hr, $k = \frac{0.693}{t_{1/2}} = \frac{0.693}{2}$ hr^{-1}

$= 9.625 \times 10^{-5}$ sec^{-1}

So, we have, $k_1 = 3.46 \times 10^{-5}$ sec^{-1}

$k_2 = 9.625 \times 10^{-5}$ sec^{-1}

$E_a = 100$ kJ mol^{-1}

$T_1 = 25°C = 298$ K

$T_2 = T$

By Arrhenius equation.

$$\log \frac{k_2}{k_1} = \frac{E_a}{2.303R}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

$$\log \frac{9.625 \times 10^{-5}}{3.46 \times 10^{-5}} = \frac{100 \times 10^3}{2.303 \times 8.314}\left(\frac{1}{298} - \frac{1}{T}\right)$$

$$\Rightarrow \frac{1}{298} - \frac{1}{T} = 8.5 \times 10^{-5}$$

$T = 306$ K

Sol 52: By Arrhenius equation

$k = A\,e^{-E_a/RT}$

$$\frac{k_2}{k_1} = e^{(E_{a_1} - E_{a_2})/RT}$$

We have,

$E_{a_1} = 75$ kJ mol^{-1}

$E_{a_2} = 25$ kJ mol^{-1}

$T = 25°C = 298$ K

$$\therefore \frac{k_2}{k_1} = 5.8 \times 10^8$$

Therefore, rate of reaction increases by 5.8×10^8 times.

Sol 53: Temperature coefficient $= \frac{k_{308k}}{k_{298k}} = 1.75$

By Arrhenius equation

$$\log \frac{k_{308k}}{k_{298k}} = \frac{E_a}{2.303k}\left(\frac{1}{298} - \frac{1}{308}\right)$$

$$E_a = \frac{\log 1.75 \times 2.303 \times 8.314 \times 298 \times 308}{10}$$

$= 42.711$ kJ mol^{-1}

$E_a = 10.757$ kJ mol^{-1}

Sol 54: At $T_1 = 380°C = 653$ K,

$k_1 = \frac{0.693}{t_{1/2}} = \frac{0.693}{360} = 1.925 \times 10^{-3}$ min^{-1}

$T_2 = 450°$ C $= 723$ K, $k_2 = k$

$E_a = 200$ k J mol^{-1}

By Arrhenius equation

$$\log \frac{k_2}{k_1} = \frac{E_a}{2.303R}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

$$\log \frac{k}{1.925 \times 10^{-3}} = \frac{200 \times 10^3}{2.303 \times 8.314}\left(\frac{1}{653} - \frac{1}{723}\right)$$
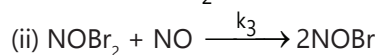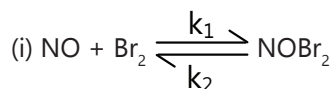
$$\log \frac{k}{1.925 \times 10^{-3}} = 1.548$$

$k = 6.81 \times 10^{-2}$ min^{-1}

Time required for 75 % reaction $= 2t_{1/2} = \frac{2 \times 0.693}{6.8 \times 10^{-2}}$

Time $= 20.4$ minutes

Sol 55: We have,

(i) $NO + Br_2 \underset{k_2}{\overset{k_1}{\rightleftharpoons}} NOBr_2$

(ii) $NOBr_2 + NO \xrightarrow{k_3} 2NOBr$

This is RDS

Here, we use equilibrium approach, as equilibrium is achieved fast

Rate $= k_3[NOBr_2]$ [NO]

For equilibrium of (i),

$$\frac{k_1}{k_2} = \frac{[NOBr_2]}{[NO][Br_2]}$$

$[NOBr_2] = \dfrac{k_1}{k_2}$ [NO] [Br]

Hence, rate $= \dfrac{k_1 k_3}{k_2}$ [NO]^2 [Br] $= k[NO]^2$ [Br$_2$]

$k = \dfrac{k_1 k_3}{k_2}$

Sol 56: (i) $2NO \rightarrow N_2O_2$

equilibrium constant $= k_1$ (fast)

(ii) $N_2O_2 + H_2 \xrightarrow{k_2} N_2O + H_2O$

RDS

(iii) $N_2O + H_2 \xrightarrow{k_3} N_2 + H_2O$
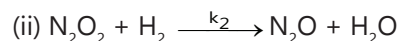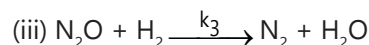
As equilibrium step is fast, we use equilibrium approach

from (i), $k_1 = \dfrac{[N_2O_2]}{[NO]^2}$

$[N_2O_2] = k_1[NO]^2$

Also, from (ii), Rate $= k_2[N_2O_2]$ [H$_2$]

$= k_1 k_2[NO]^2[H_2]$

$= k[NO]^2[H_2]$

$k = k_2 k_3$

Sol 57 (i) $NO + NO \underset{k_{-1}}{\overset{k_1}{\rightleftharpoons}} N_2O_2$ [fast]

(ii) $N_2O_2 + O_2 \xrightarrow{k_2} 2NO_2$ (RDS)
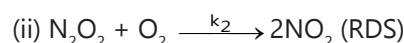
from equilibrium of (i),

$\dfrac{k_1}{k_{-1}} = \dfrac{[N_2O_2]}{[NO]^2}$

$[N_2O_2] = \dfrac{k_1}{k_{-1}}$ [NO]^2

from (ii)

Rate $= \dfrac{1}{2}\dfrac{d[NO_2]}{dt} = k_2[O_2]\,[N_2O_2] = \dfrac{k_2 k_1}{k_{-1}}$ [NO]^2[O$_2$]

Rate $= \dfrac{1}{2}\dfrac{d[NO_2]}{dt} = k[NO]^2[O_2]$,

$k = \dfrac{k_2 k_1}{k_{-1}}$

Sol 58: (a) $H_2 + I_2 \rightarrow 2HI$

since, this is one step, rate $= k[H_2]$ [I$_2$]

(b) (i) $I_2 \rightarrow 2I$

equilibrium constant $= k_1$, fast

(ii) $2I + H_2 \xrightarrow{k_2} 2HI$, RDS
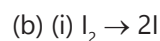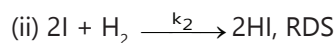
from (i) equilibrium, $k_1 = \dfrac{[I]^2}{[I_2]}$

$[I]^2 = k_1[I_2]$

from (ii) Rate $= k_2[I]^2[H_2]$

$= k_2 k_1[I_2]\,[H_2]$

$= k[H_2]\,[I_2]$, $k = k_2 k_1$

(c) (i) $I_2 \rightarrow 2I$

equilibrium constant $= k_1$, fast

(ii) $I + H_2 \rightarrow HI_2$

(iii) $IH_2 + I \xrightarrow{k_3} 2HI$, RDS
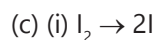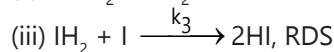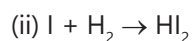
equilibrium constant $= k_2$, fast

from equilibrium (i), $k_1 = \dfrac{[I]^2}{[I_2]}$

$[I]^2 = k_1[I_2]$

from equilibrium (ii),

$k_2 = [HI]^2 \dfrac{[IH_2]}{[I][H_2]}$

$[IH_2] = k_2[I]\,[H_2]$

since (iii) is RDS,

Rate $= k_3[IH_2]\,[I]$

$= k_3 k_2[I]^2[H_2]$

$= k_1 k_2 k_3[I_2]\,[H_2]$

Rate $= k[H_2]\,[I_2]$

(d) No, it cannot distinguish between the three mechanisms as all the 3 molecules gives the same rate law.

(e) Mechanism (a) becomes most improbable as it just involves one step and it is highly unlikely that I_2 and H_2 will combine directly at 200ºC without breaking into radicals.

Exercise 2

Single Correct Choice Type

Sol 1: (B) We know,

Coefficient in rate law $= \dfrac{1}{\text{stiochiometric coefficient}}$

Given rate law

$+\dfrac{1}{2}\dfrac{d[C]}{dt} = \dfrac{-1}{3}\dfrac{d[D]}{dt} = \dfrac{+1}{3}\dfrac{d[A]}{dt} = -\dfrac{d[B]}{dt}$

Reaction is $3D + B \rightarrow 2C + 4A$

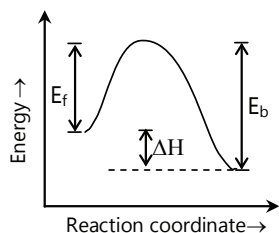**Sol 2: (D)** If volume is reduced to half, pressure will get doubled.

Now, reaction is first order w. r. t O_2 and second order w. r. t N_2

$\therefore$ Rate = $k[O_2] [N_2]^2$

$r_f = k[2O_2] [2N_2]^2$

$r_f = k[2O_2] [2N_2]^2 = 8r_i$

Sol 3: (C) We have

$\therefore |\Delta H| = E_b - E_f = (200 - 180)$ kJ mol^{-1}

$|\Delta H| = 20$ kJ/mol

Sol 4: (D) For zero order reaction

rate, $\dfrac{d[B]}{dt} = k$

$[B] = kt$

$[A] = [A]_0 - kt$

At time $t = t_{3/4}$, $[A] = \dfrac{1}{4}[A_0]$

$\Rightarrow t = \dfrac{3[A]_0}{4k}$

$\Rightarrow t_{3/4} \propto [A_0]$

Similarly, $t_{1/2} \propto [A_0]$

Sol 5: (C) Here, $t_{1/2} \propto (A)_0$, therefore, it is a zero order reaction.

So, rate of reaction $\left(\dfrac{d[A]}{dt} \right)$ will be independent of time.

Sol 6: (B) The given option is correct as there is very little probability for more than 3 atoms to collide simultaneously.

Sol 7: (C) We have $k = \dfrac{2.303}{t} \log \dfrac{a_0}{a_0 - x}$

$kt = 2.303 \log a_0 - 2.30 \log(a_0 - x)$

$\log(a_0 - x) = \dfrac{-kt}{2.303} + \log a_0$

Slope of $\log (a_0 - x)$ vs. t graph is $\dfrac{-kt}{2.303}$

Slope of given graph = $-3.3 \times 10^{-3} = \dfrac{-k}{2.303}$

$\Rightarrow k = 7.7 \times 10^{-3}$

Sol 8: (C) Volume strength = $5.6 N_0 = 16.8^\circ$

Now, after 2.303 hours, let normality be N.

When 20 mL of this solution is diluted, Normality becomes

$\dfrac{N.20}{100} = \dfrac{N}{5}$

It is diluted against 0.02 M $KMnO_4$.

Under acidic conditions, normality of $KMnO_4$ = M × 5

= 0.02 × 5 = 0.1 N

Now, using $N_1V_1 = N_2V_2$

$\dfrac{N}{5} . 25 = 0.1 \times 37.5$

N = 0.75 N

Now volume strength

V = N × 5.6 = 0.75 × 5.6 = 4.2 V

Now,

$k = \dfrac{2.303}{t} \log \dfrac{V_0}{V_t}$

t = 2.303 hours, V_0 = 16.8 V,
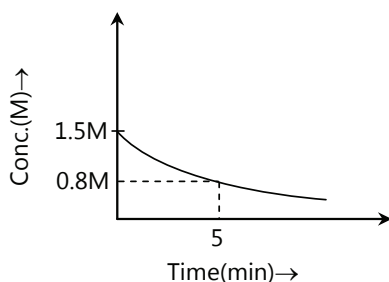
V_f = 4.2 V

$k = \dfrac{2.303}{2.303} \log \dfrac{16.8}{4.2}$

k = 0.60 hr^{-1}

Sol 9: (A) For experiment 1,
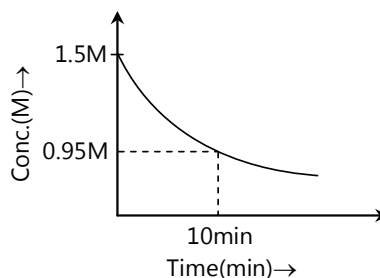
Average rate = $\dfrac{-\Delta[A]}{\Delta t} = \dfrac{0.55}{10} = 0.055$ min^{-1}

For experiment 2,

Average rate, $r_2 = \dfrac{\Delta A}{\Delta t}$

$= \dfrac{0.2}{5}$ M min^{-1} $= \dfrac{1}{25}$ M min^{-1}

$\Rightarrow \dfrac{r_1}{r_2} = \dfrac{0.55}{1/25} = 1.375 \approx 1.5 = \dfrac{[A]_{0_1}}{[A]_{0_2}}$

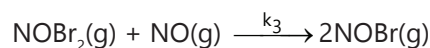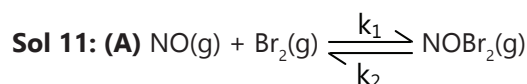Hence the reaction is first order

When (A) = 1.8 M

Rate, $r = 1.8 \times [x]_2$

$= \dfrac{1.8}{25}$ M min^{-1} = 0.072 M min^{-1}

≈ 0.08 M min^{-1}

Sol 10: (A) Since $k_1 << k_2$ second reaction will have the most activation energy

Further, since the overall reaction is exothermic, therefore the final energy of products should be less than the reactants plot which satisfies above 2 is (A).

Sol 11: (A) NO(g) + Br$_2$(g) $\underset{k_2}{\overset{k_1}{\rightleftharpoons}}$ NOBr$_2$(g)

NOBr$_2$(g) + NO(g) $\xrightarrow{k_3}$ 2NOBr(g)

We use equilibrium approach

Since second step is RDS,

Rate, R = $-k_3$[NOBr$_2$] [NO]

From equilibrium of (i),

$\dfrac{k_1}{k_2} = \dfrac{[NOBr_2]}{[NO][Br_2]}$

$\Rightarrow [NOBr_2] = \dfrac{k_1}{k_2}$ [NO] [Br$_2$]

Therefore, rate = $\dfrac{k_3 k_1}{k_2}$[NO]^2[Br$_2$]

Order w. r. t. NO = 2

Sol 12: (B)
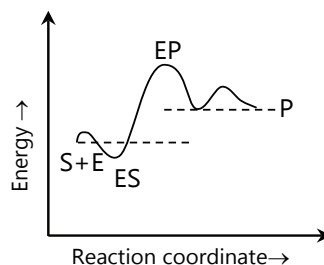
This is the plot for enzyme catalysed reaction.

Correct option is (B).

Multiple correct choice type

Sol 13: (A, D) We have, emission rate of SO$_3$

= 6.93 × 10^{-6} gm/L/day

$= \dfrac{6.93 \times 10^{-6}}{80}$ mol/L/day

= 8.6625 × 10^{-8} mol/L/day

For decomposition of SO$_3$,

$k = \dfrac{0.693}{t_{1/2}} = \dfrac{0.693}{100}$ = 6.93 × 10^{-3} day^{-1}

$\dfrac{d[SO_3]}{dt}$ = 8.6625 × 10^{-8} – 693×10^{-3}[SO$_3$]

At steady state, $\dfrac{d[SO_3]}{dt}$ = 0

$\Rightarrow [SO_3] = \dfrac{8.6625 \times 10^{-8}}{6.93 \times 10^{-3}}$

[SO$_3$] = 1.25 × 10^{-5} M

In 10^{-3} of air, moles of SO$_3$ = 1.25 × 10^{-5}×10^3

= 1.25×10^{-2} mol

When dissolved in water (1 L),

[SO$_3$] = 1.25 × 10^{-2} M

Normality of SO$_3$ = 2M = 2.5 × 10^{-2} N

$N_1V_1 = N_2V_2$

2.5 × 10^{-2} × 1000 = 1 × V$_2$

V$_2$ = 25 mL

SO$_3$ + H$_2$O → H$_2$SO$_2$
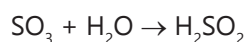
Rate of H$_2$SO$_4$ production

= 980 kg/day = $\dfrac{980 \times 10^3}{98}$ mol/day = 10^4 mol/day

SO$_3$ required = H$_2$SO$_4$ manufactured = 10^4 mol/day

Now V = $\dfrac{\text{number of moles}}{M}$

$= \dfrac{10^4}{1.25 \times 10^{-5}} = 8 \times 10^8$ L/day

If SO_3 emission stopped,

$\dfrac{d[SO_3]}{dt} = -6.93 \times 10^{-3}[SO_3]$

$\Rightarrow [SO_3] = [SO_3]_0\, e^{-6.93 \times 10^{-3}t}$

$[SO_3]_0 = [SO_3]_0\, e^{-6.93 \times 10^{-3}t}$

$[SO_3]_0 = 1.25 \times 10^{-5}$ M

t = 1000 days

$\therefore [SO_3]_0 \approx 1.2 \times 10^{-8}$ M

Sol 14: (A, B, D) $\dfrac{-d[A]}{dt} = k(A)^{1/2}$

$\displaystyle\int_{[A]_0}^{[A]} \dfrac{-d[A]}{[A]^{1/2}} = \int_0^t k\,dt$

$2[A]^{1/2}\Big|_{[A]_0}^{[A]} = kt\Big|_0^t$

(A) $^{1/2} = [A]_0^{1/2} = \dfrac{kt}{2}$

$k = \dfrac{-1}{2}(A_0^{1/2}.A^{1/2})$

$\sqrt{A} = \dfrac{kt}{2} + \sqrt{A_0}$

Straight line

At t = $t_{1/2}$, (A) = $\dfrac{[A]_0}{2}$

$t_{1/2} = \dfrac{2\sqrt{2}k}{[A_0]^{1/2} - \dfrac{[A_0]_0^{1/2}}{\sqrt{2}}}$

$\dfrac{2\left([A_0]_0^{1/2}\,2([2A]_0^{1/2} - \dfrac{[A]}{\sqrt{2}}\right)^{1/2}}{k}$

$= \dfrac{2\sqrt{2}k}{(\sqrt{2}-1)[A]_0} = \dfrac{2[A]_0^{1/2}}{k}(\sqrt{2}-1)$

At t = $t_{3/4}$, (A) = $\dfrac{[A]_0}{4}$

$\therefore t_{3/4} = \dfrac{2k}{[A]_0^{1/2} - \dfrac{[A]_0^{1/2}}{2}}$

$\dfrac{2\left([A]_0^{1/2} - \dfrac{[A]_0^{1/2}}{2}\right)}{k}$

$t_{3/4} = \dfrac{\sqrt{[A]_0}}{k}$

Sol 15: (A, D) Solution will be optically active and dextro after very long time

After 75% conversion of A in to B and C angle of rotation of solution will be 36°

Sol 16: (C, D)

(A) is correct

Rate, R = $k[A]^m[B]^n[C]^0$

log R = log k + m log[A] + n log[B]

If all concentration other than (A) are constant,

Then $\dfrac{d(\log k)}{d(\log[A])} = m$

(C) Order of reaction can be fractional

(D) Order of a reaction can only be determined experimentally

Sol 17: (A, C, D)

(A) Unit of A = Unit of k ≠ mol $L^{-1}s^{-1}$

(B) Order of an elementary must atleast be 1 (atleast 1 molecule should be present)

(C) Molecularity can be defined for any elementary reaction.

(D) Decay constant (λ) of radioactive substance is independent of temperature.

Sol 18: (A, C) With increase in $[A]_0$, rate will increase, leading to increase in yield of B. A → B has higher E_a, which means it has lower k and thus with increase in temperature k_1 will increase more than k_2, resulting in increase in yield of B.

Sol 19: (A, B, C)

(D) A zero order reaction is always complex, rest all are correct.

Assertion Reasoning Type

Sol 20: (C) Order of an elementary reaction cannot be fractional, through the overall order of a reaction can be fractional.

$$A \overset{k_1}{\underset{k_2}{\diagdown}} \begin{matrix} 2B \\ 2C \end{matrix}$$
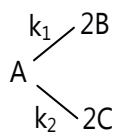
We have, $\dfrac{[B]}{[C]} = \dfrac{k_1}{k_2} = \dfrac{1}{2}$

For every mole of A consumed, $\dfrac{1}{3}$ mole used for forming B and rest for forming C.
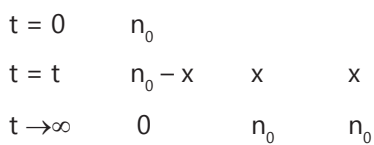
$[A]_0 = 2$ moles

At end of 50% reaction, $A_0 = 1$ mole

$B_n = \dfrac{1}{3} \times 2 \times 1 = \dfrac{2}{3}$ moles

$C_n = \dfrac{2}{3} \times 2 \times 1 = \dfrac{4}{3}$ moles

[Since, for every mole A, 2 moles of B (or C) is produced]

Sol 21: (D) $A(aq) \rightarrow B(aq) + C(aq)$

t = 0	n_0		
t = t	$n_0 - x$	x	x
t →∞	0	n_0	n_0

At $t \rightarrow \infty, \theta_\infty = -5° = n_0.\theta_B + n_0\theta_C$

We have, $\theta_A = 20°$, $\theta_B = 30°$,

$\theta_C = -40°$

$\therefore 30n_0 - 40n_0 = -5$

$n_0 = 0.5$

At time, t = 6.43 min.

$\theta_t = (n_0 - x)\theta_A + x(\theta_B + \theta_C) = 2.5$

$20n_0 + x(30.40 - 20) = 2.5$

$30x = 20 \times 0.5 - 2.5$

$30x = 7.5$

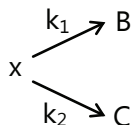$x = 0.25$

For first order conversion,

$k = \dfrac{2.303}{t}\log\dfrac{n_0}{n_0 - x} = \dfrac{2.303}{6.93}\log\dfrac{0.5}{0.5 - 0.25}$

$k = 0.1$ min^{-1}

Sol 22: (A)

$$x \overset{k_1}{\underset{k_2}{\diagdown}} \begin{matrix} B \\ C \end{matrix}$$

(B = y, C = z)

We have,

$\dfrac{d[x]}{dt} = -(k_1 + k_2)[x]$

$\displaystyle\int_{[x]_0}^{[x]_t} \dfrac{d[x]}{[x]} = -(k_1 + k_2)\int_0^t dt$

$\Rightarrow [x]_t = [x]_0 e^{-kt}, k = k_1 + k_2$

Now, $\dfrac{d[B]}{dt} = k_1[x]_t$

$\dfrac{d[B]}{dt} = k_1[x]_0 e^{-kt}$

$\displaystyle\int_0^{[B]_t} d[B] = k_1[x]_0 \int_0^t e^{-kt}$

$[B]_t = \dfrac{-k_1[x]_0}{k} e^{-kt}\Big|_0^t$

$[B]_t = \dfrac{-k_1[x]_0}{k_1 + k_2}(1 - e^{-kt})$

Similarly $[C]_t = \dfrac{k_2[x]_0}{k_1 + k_2}(1 - e^{-kt})$

$[B]_t + [C]_t = [y] + [x]$

$= \dfrac{k_1[x]_0}{k}(1 - e^{-kt}) + \dfrac{k_2[x]_0}{k}(1 - e^{-kt})$

$= \left(\dfrac{k_1 + k_2}{k}\right)[x]_0(1 - e^{-kt}) = [x]_0 \, e^{(1 - e^{-kt})}$

$\therefore \dfrac{[x]_t}{[y] + [2]} = \dfrac{e^{-kt}}{1 - e^{-kt}} = \dfrac{1}{e^{+(k_1 + k_2)t} - 1}$

Sol 23: (C) Using results of previous question

$[C]_t = \dfrac{k_2[A]_0}{k}(1 - e^{-kt}), k = k_1 + k_2$

$[A]_t = [A]_0 e^{-kt}$

$\dfrac{[C]_t}{[A]_t} = \dfrac{k_2}{k_1 + k_2}\dfrac{(1 - e^{-kt})}{e^{-kt}} = \dfrac{1}{1 + \dfrac{k_1}{k_2}}(e^{-kt} - 1)$

We have, $k_1 = x$ hr^{-1}, $k_2 = 10 k_1$

$= 10 \times$ hr^{-1}, $t = 1$ hr
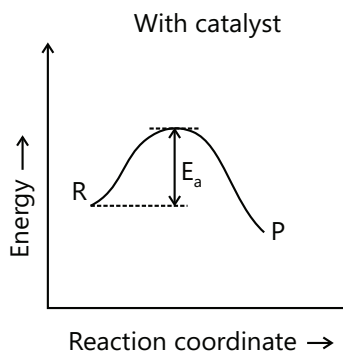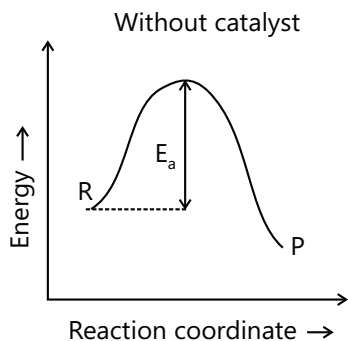
$$\therefore \frac{[C]_t}{[A]_t} = \frac{1}{1+\dfrac{1}{10}}(e^{(x+10x)} - 1)$$

$$\frac{[C]_t}{[A]_t} = \frac{10}{11}(e^{11x} - 1)$$

Sol 24: (C) For reactions with order ≤ 1, time of completion can be determined as those reactions gets fully completed in specific amount of time.

For reactions with order > 1, reaction never goes to 100 % completion and hence time of completion cannot be determined.

Sol 25: (A)

Without catalyst
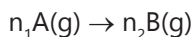

With catalyst

Comprehension Type

Paragraph 1

Sol 26: (B) Total number of moles $= 1 + \dfrac{2}{3} + \dfrac{4}{3} = 3$ moles

Sol 27: (C) Moles of B $= \dfrac{2}{3} = 0.666$ moles.

Paragraph 2

Sol 28: (B) We have,

$n_1A(g) \rightarrow n_2B(g)$

time 0   a   0

time t   a $- n_1x$ n_2x

$$\therefore \text{Rate} = k[A] = \frac{-1}{n_1}\frac{d[A]}{dt} = k[A]$$

$$\Rightarrow \int_a^{a_t} \frac{d[A]}{dt} = -n_1k\int_0^t dt$$

$$\ell n\frac{a_t}{a} = -n_1kt$$

$a_t = a\,e^{-n_1kt}$

Sol 29: (D) $n_1A(g) \rightarrow n_2B(g)$

t = 0   a   0

t = 1 $a\,e^{-n_1kt}$ $\dfrac{n_2}{n_1}a(1 - e^{-n_1kt})$

Total moles present

$$= a\left[e^{-n_1kt} + \frac{n_2}{n_1} - \frac{n_2}{n_1}e^{-n_1kt}\right]$$

$$= a\left(\frac{n_2}{n_1} - \left(\frac{n_2}{n_1} - 1\right)e^{-n_1kt}\right)$$

Concentration is to remain same at time t,

$$\therefore \frac{\text{total moles present}(n)}{V} = \frac{a_0}{V_0}$$

$$\Rightarrow V = \frac{V_0 n}{a_0} = V_0\left[\frac{n_2}{n_1} - \left(\frac{n_2}{n_1} - 1\right)e^{-n_1kt}\right]$$

Sol 30: (B) If $n_1 = 1$, $n_2 = 2$

at time t,

$n_A = ae^{-kt}$

$V = V_0(2 - (2 - 1)e^{-kt})$

$= V_0(2 - e^{-kt})$

$$(A) = \frac{n_A}{V} = \frac{ae^{-kt}}{V_0(2 - e^{-kt})} = (A)_0\left(\frac{e^{-kt}}{2 - e^{-kt}}\right)$$

Paragraph 3

Sol 31: (C) $(B) = \dfrac{k_1[A]_0}{k_2 - k_1}[e^{-k_1 t} - e^{-k_2 t}]$

$\dfrac{d[B]}{dt} = \dfrac{k_1[A]_0}{k_2 - k_1}(-k_1 e^{-k_1 t} + k_2 e^{-k_2 t})$

When (B) is maximum, $\dfrac{d[B]}{dt} = 0$

$\dfrac{d[B]}{dt} = 0$

$\Rightarrow -k_1 e^{-k_1 t} + k_2 e^{-k_2 t} = 0$

$k_1 e^{-k_1 t} = k_2 e^{-k_2 t}$

$= \dfrac{k_1}{k_2}$

$(k_1 - k_2)t = \ln\dfrac{k_1}{k_2}$; $\Rightarrow t = \dfrac{1}{k_1 - k_2}\ln\dfrac{k_1}{k_2}$

Sol 32: (C) For $k_1 = 1000$ s^{-1}, $k_2 = 20$ s^{-1},

$[A]_t = [A]_0\, e^{-1000t}$

$[B]_t = \dfrac{1000}{20 - 1000}[A]_0[e^{-1000t} - e^{-20t}]$

$\approx [A]_0 e^{-20t}$, $t_{max} = \dfrac{1}{1000 - 20}\ell n\dfrac{1000}{20}$

$[B]_t$ will increase till t_{max} and then decay exponentially

$[C]_t = [A]_0 - ([A]_t + [B]_t)$

$= [A]_0 - [A]_0\, e^{-1000t} - [A]_0 e^{-20t}$

$= [A]_0(1 - e^{-1000t} - e^{-20t})$

$\approx [A]_0(1 - e^{-20t})$

$[C]_t$ will approach $[A]_0$ asymptotically.

Paragraph 4

We have $\dfrac{df}{dt} = k(1 - f)$

$\displaystyle\int_0^f \dfrac{df}{1 - f} = \int_0^f k\,dt$

$-\ln(1 - f)\big|_0^f = k\,f\big|_0^f$

$-\ln(1 - f) = kt$

$f = 1 - e^{-kt}$

Sol 33: (B) Slope of $\ln(1 - f)$ vs f graph

$= -k = \dfrac{-3}{200}$ hr^{-1}

$\Rightarrow k = \dfrac{3}{200}$ hr^{-1}

When $f = \dfrac{1}{2}$

$\dfrac{1}{2} = 1 - e^{-kt}$

$t = \dfrac{\ell n2}{k} = \dfrac{0.693 \times 200}{3} = 46.2$ hrs.

Sol 34: (A) $f = 1 - e^{-kt}$

$f = [1 - e^{-3t/200}]$

Paragraph 5

Sol 35: (C) For $t = 100$ min, $x = \dfrac{3}{4}a$

$\therefore k = \dfrac{1}{100}\ln\dfrac{a}{a - \dfrac{3}{4}a} = \dfrac{\ell n2}{50}$ min^{-1}
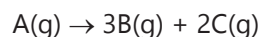
When $x = 0.9\,a$,

$k = \dfrac{1}{t}\ln\dfrac{a}{a - 0.9a}$

$t = \dfrac{1}{k}\ln 10 = \dfrac{50\ln 10}{\ln 2} = \dfrac{50}{\ln 2} = \dfrac{50}{0.3}$; $= 166.66$ min

Sol 36: (B) $[A]_0 = \dfrac{2}{12.5} = 0.16$

We have,

$\dfrac{1}{3}\dfrac{d[B]}{dt} = k[A]$

$\qquad\qquad A(g) \rightarrow 3B(g) + 2C(g)$

At time 0 0.16

At time t 0.16–x   3x   2x

Also, $\dfrac{d[A]}{dt} = -k[A]$

$[A] = [A]_0\, e^{-kt}$

$= 0.16\ e^{1.386\times 10^{-2}\times 100}$

$= 0.04$

i. e. , $0.16 - x = 0.04$

$x = 0.12$

$(B) = 3x = 0.36.$

Match the Columns

Sol 37: (A) → s

We have,

$$\frac{1}{2}\frac{d[B]}{dt} = \frac{-d[A]}{dt}$$

Straight line with slope equal to 2.

(B) → r

$[A] = [A]_0 e^{-kt}$

exponential decay

(C) → p

$(B) = 2([A]_0 - [A]); = 2[A]_0 (1 - e^{-kt})$

Exponential graph will approach $2(A)_0$ asymptotically.

(D) → q

For zero order,

$[A] = [A]_0 - kt$

Straight line with slope $-k$.

Sol 38: We will draw all graphs given in Column-II and then match them with Column-I.

(p) ln (A) vs t (order 1)

We have, $[A] = [A]_0 e^{-kt}$

$\ln[A] = \ln[A]_0 - kt$

Straight line with negative slope matches (A).

(q) $t_{1/2}$ vs $(A)_0$ (order = 1)

$$t_{1/2} = \frac{0.693}{k}$$

It is independent of $[A]_0$, straight line parallel to x-axis. Matches (B)

(r) r vs t (order > 0)

$r = k[A]^n$, n > 0

for order > D, rate decreases with increasing t as (A) decreases with t

∴ decreasing graph (not straight line) matches (C).

(s) r vs t (order = 0)

For order, r is constant of time, graph is straight line parallel to x-axis.

(t) $t_{1/2}$ vs $[A]_0$ (order > 1)

We know,

$$t_{1/2} \propto \frac{1}{[A_0]^{n-1}}$$

decreasing graph

Matches (C).

(U) $\dfrac{1}{[A]}$ vs t(order = 2)

we have,

$$\frac{-d[A]}{dt} = \frac{-k}{[A]^2}$$

$$\Rightarrow \int_{[A]_0}^{[A]} \frac{d[A]}{[A]^2} = -k\int_0^t dt$$

$$\Rightarrow \frac{-1}{[A]_0}\Bigg|_{[A_0]}^{[A]} = -kt\Big|_0^t$$

$$\Rightarrow \frac{1}{[A]_0} - \frac{1}{[A]} = -kt$$

$$\Rightarrow \frac{1}{[A]} = kt + \frac{1}{[A]_0}$$

Straight line with positive slope and positive intercept.

Matches no option in Column-I.

(V) r vs [A] (order = 1)

r = k[A]

Straight line with positive slope.

Matches (D)

(A) → p

(B) → q, s

(C) → r, t

(D) → v

Previous Years' Questions

Sol 1: (A) The rate constant (k) of all chemical reactions depends on temperature.

$k = Ae^{-E_a/RT}$

where, A = Pre-exponential factor,

E_a = Activation energy.

Sol 2: (C) A catalyst increases the rate of reaction but by the same factor to both forward and backward

directions. Hence, a catalyst shorten the time required to reach the equilibrium.

Sol 3: (D) Rate will be directly proportional to both concentration and intensity, i.e, rate of formation of AB * $\propto$ C. I.

Sol 4: (D) Order of a reaction can take any real value, i.e, negative, integer, fraction, etc.

Sol 5: (A) According to Arrhenius equation, rate constant increases exponentially with temperature : $k = Ae^{-E_a/RT}$

Sol 6: (A) Living plants maintain an equilibrium between the absorption of C^{14} (produced due to cosmic radiation) and the rate of decay of C^{14} present inside the plant. This gives a constant amount of C^{14} per gram of carbon in a living plant.

Sol 7: (B) Fossil whose age is closest to half-life of C–14 (5770 yr) will yield the most accurate age by C–14 dating.

Sol 8: (A) $\lambda T = \ln\dfrac{N_0}{N}$
where N_0 = Number of C^{14} in the living matter and N = Number of C^{14} in fossil. Due to nuclear explosion, amount of C^{14} in the near by area increases. This will increase N_0 because living plants are still taking C–14 from atmosphere, during photosynthesis, but N will not change because fossil will not be doing photosynthesis.

$\Rightarrow$ T (age) determined in the area where nuclear explosion has occurred will be greater than the same determined in normal area.

Also, $\lambda T_1 = \ln\dfrac{C_1}{C}$

$\lambda T_2 = \ln\dfrac{C_2}{C}$

$\Rightarrow T_1 - T_2 = \ln\dfrac{C_1}{C_2}$

C = Concentration of C–14 in fossil.

Sol 9: Rate of reaction is constant with time.

Sol 10: $k = \dfrac{\ln 2}{t_{1/2}} = \dfrac{0.693}{5770}$ yr^{-1} = 1.2 × 10^{-4} yr^{-1}

Also kt = $\ln\dfrac{1}{f} = \dfrac{\ln 2}{5770}$ × 11540 = ln 4

$\Rightarrow$ f = $\dfrac{1}{4}$ = 0.25

Sol 11: k = 1.5 × 10^{-6} s^{-1}

kt = $\ln\dfrac{100}{100-x}$

$\Rightarrow \ln\dfrac{100}{100-x}$

= 1.5 × 10^{-6} s^{-1} × 10 × 60 × 60s; = 0.0054

$\Rightarrow \dfrac{100}{100-x}$ = 1.055

$\Rightarrow$ x = 5.25% reactant is converted into product

Half-life = $\dfrac{\ln 2}{k} = \dfrac{0.693}{1.5\times 10^{-6}}$ = 462000 s; = 128.33 h

Sol 12: The minimum rate of decay required after 6.909 h is 346 particles min^{-1}.

$\Rightarrow$ Rate = kN

$\Rightarrow$ N = $\dfrac{Rate}{k} = \dfrac{346\times 66.6\times 60}{0.693}$

= 1.995 × 10^6 atoms

$\Rightarrow$ kt = $\ln\dfrac{N_0}{N}$

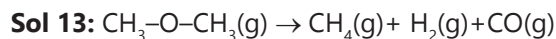$\Rightarrow \dfrac{\ln 2}{66.6}$ × 6.909 = $\ln\dfrac{N_0}{N}$ = 0.0715

$\Rightarrow \dfrac{N_0}{N}$ = 1.074

$\Rightarrow N_0$ = 1.074 × N = 1.074 × 1.995 × 10^6

= 2.14 × 10^6 atoms of Mo

$\Rightarrow$ Mass of Mo required

= $\dfrac{2.14\times 10^6}{6.023\times 10^{23}}$ × 99 = 3.56 × 10^{-16}g

Sol 13: $CH_3-O-CH_3(g) \rightarrow CH_4(g) + H_2(g) + CO(g)$

At 12 min : 0.40 – p   p   p   p

Total pressure = 0.4 + 2p

Also k × 12 = $\ln\dfrac{0.40}{0.40-p}$

= $\dfrac{\ln 2}{14.5}$ × 12 = $\ln\dfrac{0.40}{0.40-p}$

$\Rightarrow$ p = 0.175

$\Rightarrow$ Total pressure = 0.4 + 2p

= 0.4 + 2 × 0.175

= 0.75 atm.

Sol 14: (A) $\ln \dfrac{k_2}{k_1} = \dfrac{E_a}{R}\left(\dfrac{T_2 - T_1}{T_1 T_2}\right)$

$\Rightarrow \ln\left(\dfrac{4.5 \times 10^7}{1.5 \times 10^7}\right) = \dfrac{E_a}{8.314}\left(\dfrac{50}{323 \times 373}\right)$

$\Rightarrow E_a = 22$ kJ

Also $\ln k = \ln A - \dfrac{E_a}{RT}$

At 50°C :

$\ln A = \ln (1.5 \times 10^7) - \dfrac{22 \times 1000}{8.314 \times 323} = 8.33$

$\Rightarrow A = 4.15 \times 10^3 \text{ s}^{-1}$

(b) $N_2O_5 \text{ (g)} \rightarrow 2NO_2 \text{ (g)} + \dfrac{1}{2}O_2 \text{ (g)}$

$\quad 600 - p \qquad 2p \qquad \dfrac{p}{2}$

Total pressure = $690 = 600 + \dfrac{3}{2}p$

$\Rightarrow p = 240$ mm

$\Rightarrow$ Partial pressure of $N_2O_5(g)$

remaining

$= 600 - 240$

$= 360$ mm

$\Rightarrow$ Mole-fraction $= \dfrac{360}{960} = 0.375$

Sol 15: (A) Partial pressure becomes half of initial in every 100 min, therefore, order = 1.
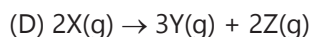
(B) $k \times 100 = \ln \dfrac{800}{400} = \ln 2$

$\Rightarrow k = 6.93 \times 10^{-3} \text{ min}^{-1}$

(C) For 75% reaction; time required

$= 2 \times$ half-life

$= 200$ min

(D) $2X(g) \rightarrow 3Y(g) + 2Z(g)$

$\quad\; 800 - x \quad \dfrac{3}{2}x \quad x$

Total pressure $= 800 + \dfrac{3}{2}x$

Also $800 - x = 700$

$\Rightarrow x = 100$

$\Rightarrow$ Total pressure

$= 800 + \dfrac{3}{2} \times 100 = 950$ mm

Sol 16: (D) $aG + bH \longrightarrow$ Product

rate $\propto [G]^a [H]^b$

$a = 1, b = 2$

Sol 17: (A) $k_1 = \dfrac{0.693}{t_{1/2}} = \dfrac{0.693}{40}$

$k_0 = \dfrac{A_0}{2t_{1/2}} = \dfrac{1.386}{2 \times 20}$

$\dfrac{k_1}{k_0} = \dfrac{0.693}{40} \times \dfrac{40}{1.386} = \dfrac{0.693}{1.386} = 0.5 \text{ mol}^{-1}$ litre

Sol 18: $t_{1/8} = \dfrac{2.303 \log 8}{k} = \dfrac{2.303 \times 3 \log 2}{k}$

$t_{1/10} = \dfrac{2.303}{k}\log 10 = \dfrac{2.303}{k}$

$\left[\dfrac{t_{1/8}}{t_{1/10}}\right] \times 10 = \dfrac{\left(\dfrac{2.303 \times 3 \log 2}{k}\right)}{\left(\dfrac{2.303}{k}\right)} \times 10 = 9$

Sol 19: (D) Overall order of reaction can be decided by the data given $t_{75\%} = 2t_{50\%}$

∴ It is a first order reaction with respect to P.

From graph [Q] is linearly decreasing with time, i.e. order of reaction with respect to Q is zero and the rate expression is $r = k [P]^1[Q]^0$.

Hence (D) is correct.

Sol 20: (C) $\dfrac{r_1}{r_2} = \dfrac{1}{8} = \dfrac{[M]^n}{[2M]^n} \Rightarrow n = 3$

Sol 21: (B, C, D) A high activation energy usually implies a slow reaction.