FORMULAE SHEET

1. Type of thermal expansion

Coefficient of expansionFor temperature change Δt change in(i) Linear $\alpha = \lim_{\Delta t \to 0} \frac{1}{\ell_0} \frac{\Delta \ell}{\Delta t}$ Length $\Delta \ell = \ell_0 \alpha \Delta t$ (ii) Superficial $\beta = \lim_{\Delta t \to 0} \frac{1}{A_0} \frac{\Delta A}{\Delta t}$ Area $\Delta A = A_0 \beta \Delta t$ (iii) Volume $\gamma = \lim_{\Delta t \to 0} \frac{1}{V_0} \frac{\Delta V}{\Delta t}$ Volume $\Delta V = V_0 \gamma \Delta t$

- For isotropic solids $\alpha_1 = \alpha_2 = \alpha_3 = \alpha$ (let) so $\beta = 2\alpha$ and $\gamma = 3\alpha$
- For anisotropic solids $\beta = \alpha_1 + \alpha_2$ and $\gamma = \alpha_1 + \alpha_2 + \alpha_3$ Here α_1, α_2 and α_3 are coefficient of linear expansion in X, Y, and Z directions.

Variation in density: With increase of temperature volume increases so density decreases and vice-versa.

$$\rho = \frac{\rho_0}{\left(1 + \gamma \Delta t\right)} \approx \rho_0 \left(1 - r \Delta T\right)$$

Thermal Stress: A rod of length ℓ_0 is clamped between two fixed walls with distance ℓ_0 .

If temperature is changed by amount Δt then stress = $\frac{F}{A}$ (area assumed to be constant)

Strain =
$$\frac{\Delta \ell}{\ell_0}$$
; so, $Y = \frac{F / A}{\Delta \ell / \ell_0} = \frac{F \ell_0}{A \Delta \ell} - \frac{F}{A \alpha \Delta t}$ or $F = YA \alpha \Delta t$

- $\Delta Q = mc\Delta T$ where c: Specific heat capacity
- $\Delta Q = nC\Delta T$ C: Molar heat capacity
- Heat transfer in phase change : $\Delta Q = mL$ L: latent heat of substance
- 1 Calorie= 4.18 joules of mechanical work
- Law of Calorimetry: heat released by one of the substances = Heat absorbed by other substances.

Solved Examples

JEE Main/Boards

Example 1: Calculate the amount of heat required to convert 1.00kg of ice at -10°C into steam at 100°C at normal pressure. Specific heat capacity of ice = 2100 $Jk^{-1} K^{-1}$, latent heat of fusion of ice=3.36×10⁵ $JKg^{-1}K^{-1}$, specific heat capacity of water= 4200 $JKg^{-1}K^{-1}$ and latent heat of vaporization of water = 2.25×10⁶ JKg^{-1} .

Sol: Here the temperature of ice and water changes along with change in phases. i. e. ice to water and then water to steam.

Heat required to take the ice from -10 °C to

$$0^{0}C = (1kg)(2100 JKg^{-1}K^{-1})(10K) = 21000 J.$$

Heat required to melt the ice at $0 \circ C$ to water = $(1 \text{kg})(3.36 \times 10^5 \text{ JKg}^{-1}) = 336000 \text{ J}$.

Heat required to take 1 kg of water from $0 \circ C$ to $100 = (1 \text{kg})(4200 \text{JKg}^{-1} \text{K}^{-1})(100 \text{K}) = 420000 \text{J}.$

Heat required to convert 1kg of water at 100°C into steam = $(1kg)(2.25 \times 10^6 \text{ JKg}^{-1}) = 2.25 \times 10^6 \text{ J}.$

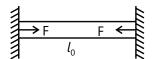


Figure 15.6

Total heat required = 3.03×10^6 J.

Example 2: A 5 g piece of ice at-20°C is put into 10g of water at 30°C. Assuming that heat is exchanged only between the ice and the water, find the final temperature of the mixture. Specific heat capacity of ice. = 2100 JKg⁻¹ °C⁻¹ specific heat capacity of water = 4200 Jkg⁻¹ °C⁻¹ and latent heat of fusion of ice = 3.36×10^5 JKg⁻¹.

Sol: Always proceed in similar questions assuming the final temperature to be the temperature of phase change (i.e. 0 here)

The heat given by the water when it cools down from 30° C to 0° C is

 $(0.0 \text{kg})(4200 \text{JKg}^{-1} \ ^{\circ}\text{C}^{-1})(30 \ ^{\circ}\text{C}) = 1260 \text{ J}$

The heat required to bring the ice to 0°C is

 $(0.005 \text{kg})(2100 \text{ JKg}^{-1} \text{°C}^{-1})(20^{\circ} \text{C}) = 210 \text{ J.}$

The heat required to melt 5 g of ice is

 $(0.005 \text{kg})(3.36 \times 10^5 \text{ JKg}^{-1} \text{ °C}^{-1}) = 1680 \text{ J} \cdot$

We see that whole of the ice cannot be melted as the required amount of heat is not provided by the water. Also, the heat is enough to bring the ice to 0°C. Thus the final temperature of the mixture is 0°C with some of the ice is melted.

Example 3: A thermally isolated vessel contains 100g of water at 0°C. When air above the water is pumped out, some of the water freezes and some evaporates at 0°C itself. Calculate the mass of ice formed if no water is left in the vessel. Latent heat of vaporization of water at $0^{\circ}C = 2.10 \times 10^{6}$ JKg⁻¹ and latent heat of fusion= 3.36×10^{5} JKg⁻¹.

Sol: Some water evaporates and Heat of vaporization comes from water itself and hence remaining water freezes by giving the heat for vaporization.

Total mass of water = M=100g. Latent heat of vaporization of water at $0^{\circ}C = L_1 = 21.0 \times 10^5 J kg^{-1}$ latent heat of fusion of ice= $L_2 = 3.36 \times 10^5 J Kg^{-1}$. Suppose, the mass of the ice formed = m. Then the mass of water evaporated = M - m. Heat taken by the water to evaporate = (M - m)L_1 and heat given by the water in freezing=mL_2. Thus, mL_2 = (M-m) L_1

or,
$$m = \frac{ML_1}{L_1 + L_2} = \frac{(100g)(2.10 \times 10^6 \text{ JKg}^{-1})}{(21.0 + 3.36)10^5 \text{ JKg}^{-1}} = 86g.$$

Example 4: A lead bullet penetrates into a solid object and melts. Assuming that 50% of its kinetic energy was used to heat it, calculate the initial speed of the bullet. The initial temperature of the bullet is 27°C and its melting point is 327°C. Latent heat of fusion of lead = 2.25×10^4 JKg⁻¹ and specific heat capacity of lead = 125JKg⁻¹ K⁻¹

Sol: Kinetic energy of bullet spatially converted into heat and melt it.

Let the mass of bullet = m.

Heat required to take the bullet from 27°C to 327°C =

$$m \times (125 J K g^{-1} K^{-1}) (300 K)$$
$$= m \times (3.75 \times 10^{4} J K g^{-1})$$

Heat required to melt the bullet

$$= m \times (2.10 \times 10^6 \text{ JKg}^{-1})$$

If the initial speed be v, the kinetic energy is $\frac{1}{2}mv^2$ and hence the heat developed is $\frac{1}{2}\left(\frac{1}{2}mv^2\right) = \frac{1}{4}mv^2$. thus, $\frac{1}{4}mv^2 = m(3.75 + 2.5) \times 10^4 \text{ JKg}^{-1}$ or v= 500 ms⁻¹

Example 5: An aluminum vessel of mass 0.5 kg contains 0.2 kg of water at 20°C. A block iron of mass 0.2 kg at 100°C is gently put onto the water. Find the equilibrium temperature of the mixture. Specific heat capacities of aluminum, iron and water are 910 JKg⁻¹K⁻¹, 470 JKg⁻¹K⁻¹ and 4200 JKg⁻¹K⁻¹ respectively.

Sol: Heat lost by the iron block increase the temperature of vessel and water.

Mass aluminum = 0.5kg, Mass of water = 0.2kg; Mass of iron = 0.2kg Temp. of aluminum and water = 20°C = 293K Temperature of iron = 100°C = 373K Specific heat aluminum = 910J/kg-K Specific heat of iron = 470J/kg-K Specific heat of water = 4200J/kg-K Heat gain = Heat lost; \Rightarrow (T-293)(0.5 × 910 + 0.2 × 4200) = 0.2 × 470 × (373 – T)

$$\Rightarrow$$
 (T − 293)(455 + 8400) = 49(373 – T);

$$\Rightarrow (T - 293) \left(\frac{1295}{94}\right) = (373 - T);$$

$$\Rightarrow (T - 293) \times 14 = 373 - T$$

$$\Rightarrow T = \frac{4475}{15} = 298K \quad \therefore \quad T = 298 - 273 = 25^{\circ}C$$

The final temp= $25^{\circ}C$.

Example 6: A Piece of iron of mass 100 g is kept inside a furnace for long time and then put in a calorimeter of water equivalent 10 g containing 240 g of water 20°C. The mixture attains an equilibrium temperature of 60°C.

Find the temperature of furnace. Specific heat capacity of iron= $470 \text{JKg}^{-1} \circ \text{C}^{-1}$.

Sol: This can be calculated in reverse manner, Heat lost by the iron piece is equal to heat required to increase the temperature of water and calorimeter.

Mass of iron = 100g

Water Eq of calorimeter = 10g;

Mass of water = 240g

Let the Temp. of surface = $0^{\circ}C$

 $S_{iron} = 470 J/kg °C$

Total heat gained = Total heat lost.

So,
$$\frac{100}{1000} \times 470 \times (\theta - 60) = \frac{250}{1000} \times 4200 \times (60 - 20)$$

 $\Rightarrow 470 - 47 \times 60 = 25 \times 42 \times 40$

$$\Rightarrow \theta = 4200 + \frac{2820}{47} = \frac{44820}{47} = 953.61^{\circ} \text{C}$$

Example 7: The temperature of equal masses of three different liquids A, B and C are 120°C, 19°C and 280°C respectively. The temperature when A and B are mixed is 160°C, and when B and C are mixed, it is 23°C what will be the temperature when A and C are mixed?

Sol: All liquids have same mass. The heat lost by one equals to heat gain by other, so we can try to solve for the ratio of their heat capacities.

The temp. of A = 12° C The temp. of B = 19° C The temp. of C = 28° C The temp of A + B = 16° C The temp. of B + C = 23° C In accordance with the principle of calorimetry when A& B are mixed

$$\begin{split} M_{CA} \left(16 - 12 \right) &= M_{CB} \left(19 - 16 \right) \\ \Rightarrow M_{CA} 4 &= M_{CB} 3 \Rightarrow M_{CA} = \frac{3}{4} M_{CB} \qquad ...(i) \end{split}$$

And when B and C are mixed;

$$\begin{split} \mathsf{M}_{\mathsf{CB}}\left(23-19\right) &= \mathsf{M}_{\mathsf{CC}}\left(28-23\right) \\ &\Rightarrow 4\mathsf{M}_{\mathsf{CB}} = 5\mathsf{M}_{\mathsf{CC}} \Rightarrow \mathsf{M}_{\mathsf{CC}} = \frac{4}{5}\mathsf{M}_{\mathsf{CB}} \qquad \qquad \dots (ii) \end{split}$$

When A& C are mixed, if T is the common temperature of mixture

$$M_{CA} (T - 12) = M_{CC} (28 - T) = \left(\frac{3}{4}\right) CB(T - 12)$$

$$\Rightarrow \left(\frac{4}{4}\right) M_{CB} (28 - T)$$

$$= 15T - 180 = 488 - 16T \Rightarrow T = \frac{628}{31} = 20.258 = 20.3^{\circ}C$$

Example 8: A glass cylinder can contain $m_0 = 100g$ of mercury at a temperature of $T_0=0^{\circ}C$. When $T_1=20^{\circ}C$, the cylinder can contain $m_1 = 99.7g$ of mercury. In both cases the temperature of the mercury is assumed to be equal to that of the cylinder. Use this data of find the coefficient of linear expansion of glass α , bearing in mind that the coefficient of volume expansion of mercury $\gamma_1 = 18 \times 10^{-5} \text{ deg}^{-1}$

Sol: Get the γ of glass with the information of mercury. Find the relation between the densities at different temperature, and then get coefficient of linear expansion of glass cylinder.

When the cylinder is heated, its volume increases according to the same Law as that of the glass: $V_1 = V_0 (1 + \gamma T_1)$ where γ is the coefficient of volume expansion of glass. If the densities of mercury at the temperature T_0 and T_1 are denoted by ρ_0 and ρ_1 . We can

write that $m_0 = V_0 \rho_0$ and $m_1 = V_1 \rho_1$, where $\rho_1 = \frac{\rho_0}{1 + \gamma T_1}$. This system of equations will give the following expression for γ ;

$$\gamma = \frac{m_1 \left(1 + \gamma_1 T_1\right)}{m_0 T_0} \approx 3 \times 10^{-5} \, \text{deg}^{-1}$$

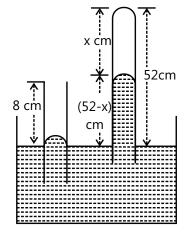
The coefficient of linear expansion, $\alpha = \frac{\gamma}{3} = 10^{-5} \text{ deg}^{-1}$

JEE Advanced/Boards

Example 1: An open glass tube is immersed in mercury in such a way that a length of 8cm extends above the mercury level. The open end of the tube is then closed and raised further by 44 cm. What will be the length of the air column above mercury in the tube? Atmospheric pressure= 76 cm of mercury.

Sol: Air column will get trapped and follow PV=constant.

Let A be the area of cross section of the tube.



Initial Atmospheric pressure of air in the tube outside the mercury surface= P_1 =76 cm of Hg

Initial volume of air, V₁=8A

New pressure of air in the tube

$$P_2 = 76 - (52 - x) = (42 - x) cm of Hq$$

New volume of air, V = xA

As
$$P_1V_1 = P_2V_2$$
; $76 \times 8A = (42 + x)xA$
or $608 = x^2 + 24x$

or $x^2 + 24x - 608$

= 0, x =
$$\frac{-24 \pm \sqrt{(24)^2 - 4 \times 608}}{2}$$

∴ x = 15.2 cm or x = -39.4 cm

Which is negative

:. The length of air column =15.4cm

Example 2: An air bubble starts rising from bottom of a lake. Its diameter is 3.6 mm at the bottom and 4 mm at the surface. The depth of the lake is 250 cm and the temperature at the surface is 40°C. What is the temperature at the bottom of the lake? Given atmospheric pressure=76 cm of Hg and g=980cm/sec².

Sol: Here the amount air remains while P, V and T all parameters changes. Hence PV/T =constant.

Volume of the bubble of lake

$$= V_1 = \frac{4}{3}\pi r_1^3 = \frac{4}{3}\pi (0.18)^3 \,\mathrm{cm}^3$$

Pressure on the bubble P_1

= Atmospheric pressure + Pressure due to a column of 250 cm of water

$$= 76 \times 13.6 \times 980 + 250 \times 1 \times 980$$

 $= (76 \times 13.6 + 250)980$ dyne / cm²; T₁ = ?

Volume of the bubble at the surface of lake

$$V_2 = \frac{4}{3}\pi r_2^3 = \frac{4}{3}\pi \left(0.2\right)^3 \text{cm}^3$$

Pressure on the bubble P₂

=Atmospheric pressure = $76 \times 13.6 \times 980$ dyne / cm²

Example 3: A mixture of 250 gm of water and 200 gm of ice at 0°C is kept in a calorimeter which has a water equivalent of 50 gm. If 200 gm of a steam at 100°C is passed through this mixture, calculate the final temperature and weight of the content of the calorimeter. Latent heat of fusion of ice=80 Cal/gm. latent heat of vaporization of water of steam=540cal/gm., Specific heat of water=1cal/gm./°C.

Sol: Latent heat of vaporization of water is approx. 7 times of latent heat of fusion. So 1g steam can melt about 7g of ice. The mass of steam equals to mass of ice, so part of steam is condensed to melt the ice.

Heat lost by 200 gm. of steam before it is condensed to water at 100° C

0.79

 $= 200 \times 540 = 108000$ cal

Heat gained by 200 gm. of ice at 0°C

$$= \mathsf{mL} + \mathsf{m} \times \mathsf{s} \times \Delta \mathsf{T} = 200 \times 80 \times 1 \times (100 - 0)$$

= 36000 cal

Heat gained by 250gm of water and 50 gm of water equivalent of calorimeter at 100°C to 0°C

 $= 200 \times 80 \times (100 - 0) + 50 \times (100 - 0)$

 $= 300 \times 100 = 30000$ cal

Total heat gained

Amount of heat lost by the system (i) is greater than heat gained by ice. This shows that only a part of the steam will condense to water at 100°C which will be sufficient for melting ice.

Let M be mass of steam which will be sufficient for melting ice,

: Mass M of steam required is given by.

Or M = 66000 / 540 = $\frac{1100}{9}$ = 122.2gm

Final temperature of system= 100°C

Weight contents

= Weight of ice +Water+ Steam condensed

=250+200+122.2=572.2gm

Example 4: A copper calorimeter of mass 100 gm contains 200g of a mixture of ice and water; Steam at 100°C under normal pressure is passed into the calorimeter and the temperature of the mixture is allowed to rise to 50°C. If the mass of the calorimeter and its contents is now 330gm, what was the ratio of ice and water in the beginning? Neglect heat losses. Given that:

Specific heat of copper= 0.42×10^3 J / kg K.

Specific heat of water = 4.2×10^3 J/kg K.

Latent heat of fusion of ice = 3.36×10^5 J / kg K.

Latent heat of condensation of steam

$$= 22.5 \times 10^5 \text{ J/kg K}.$$

Sol: Total amount of heat lost by the steam will bring the water and calorimeter to 50 degree temp. remaining heat would have been used to melt the ice.

Heat is lost by steam in getting condensed and heat is gained by the water, ice and the calorimeter. Let

the calorimeter originally contains x gm of ice and (200-x) gm. of water.

Heat gained by calorimeter

$$=\frac{100}{1000}\times0.42\times10^{3}\times(50-0)=2100J$$

Heat gained by ice

... (i)

$$=\frac{x}{1000}\times\left[3.36\times10^5+\left(4.2\times10^3\times50\right)\right]$$

= x [336 + 210] = x × 546 J

Heat gained by water

$$= \left[\frac{200 - x}{1000}\right] \left[4.2 \times 10^3 \times 50\right] = 42000 - 210 x J$$

Heat lost by steam

$$\left[\frac{330-200-100}{1000}\right] \left[22.5 \times 10^{3} \times 4.2 \times 10^{3} \times 50\right]$$

= 30[2250 + 210] = 30 × 2460 = 73800J
Heat gained = heat lost;
2100+546x+42000-210x = 73800;
336x = 73800-44100 = 29700
Mass of ice = x = $\frac{29700}{336}$ = 88.39gm
Mass of water = 111.61 gm
Ratio of ice to water = 88.39:111.6=1:1.263 ≈

Example 5: A one liter flask contains some mercury. It is found that at different temperatures the volume of air inside the flask remains the same. What is the volume of mercury in the flask? Given coefficient of linear expansion of glass= 3×10^{-6} per degree Celsius.

Coefficient of volume expansion of Hg

= 1.8×10^{-4} per degree Celsius.

Sol: Volume of air in the flask is independent of temperature.

Let x be the volume of mercury in the flask

Volume of air = Volume of flask – Volume of Hg.

= 1000 cm³ - x cm³

At any Temperature 'T' –

Volume of flask = 1000 + 1000 x 3 $\alpha_g \Delta T$(i)

and Volume of Hg = $x + x \times \gamma_m \times \Delta T$...(ii)

Hence volume of air = Volume of flask – Volume of Hg

$$= 1000 - x + (1000 \times 3\alpha_{g} - x \times \gamma_{m}) \times \Delta T$$

Given: Volume of air remains constant at all temperatures

Hence, coefficient of
$$\Delta T$$

i.e. $(1000 \times 3\alpha_g - x \times \gamma_m) = 0$
 $\Rightarrow x = \frac{3 \times 1000 \times \alpha_g}{\gamma_m} = \frac{9 \times 1000 \text{ cm}^3 \times 10^{-6} \text{ /}^{\circ} \text{ C}}{1.8 \times 10^{-4} \text{ /}^{\circ} \text{ C}}$
= 50 cm³

Example 6: A piece of metal weights 46 gm in air. When it is immersed in a liquid of specific gravity 1.24 at 37°C, it weighs 30 gm. When the temperature of the liquid is raised to 42°C, the metal piece weights 30.5 gm. The specific gravity of the liquid at 42°C, is 1.20. Calculate the coefficient of linear expansion of the metal.

Sol: Applying Archimedes' principle, i.e. lose in wt= wt of liquid displaced. We can get volume of metal at two temp. so we can have coefficient of volume expansion. Weight of the piece of metal in air=46gm. weight of the piece of metal in liquid at $27^{\circ}C = 30$ gm

:. Loss of the weight of the piece of metal in liquid = 46-30 = 16gm = Weight of liquid displaced

Volume of liquid Displaced

$$= \frac{\text{Weight of liquid displaced}}{\text{Density}} = \frac{16}{124} \text{ c.c}$$

The volume of metal piece at 27°C, is $\therefore V_{27} = \frac{16}{124}$ c.c

Weight of the piece of metal in air= 46 gm

Weight of the piece of metal in liquid at = $42^{\circ}C$ = 30.5gm

Loss of the weight of the piece of metal in liquid = 46 - 30.5 = 15.5gm

The Volume of the liquid Displaced

$$=\frac{\text{Weight of liquid displaced}}{\text{Density}}=\frac{15.5}{1.20}\text{c.c}$$

The volume of piece of metal at 42°C

= V₄₂ =
$$\frac{15.5}{1.20}$$
 c.c; V₄₂ = V₂₇ (1+γT)
∴ $\frac{15.5}{1.20} = \frac{16}{124}$ (1+γ×15) (∵ T = 42 - 27 = 15)
1+γ15 = $\frac{15.5}{1.20} \times \frac{16}{124}$

Or
$$\gamma = \frac{1}{15} = \left[\frac{15.5}{1.20} \times \frac{1.24}{16} - 1\right] = \frac{1}{15} \times \frac{1}{960}$$

 $\therefore \alpha = \frac{1}{3 \times 15 \times 960} = 2.31 \times 10^{-5} / {}^{0} \text{ C}$

Example 7: A composite rod is made by joining a copper rod end to end with a second rod of different material but of the same cross-section. At 25°C, the composite rod is 1 m in length of which of the copper rod is 30 cm. At 125°C, the length of the composite rod increases by 1.91 mm. When the composite rod is not allowed to expand by holding it between two rigid walls, it is found that the lengths of the two constituents do not change with the rise of temperature. Find the Young's modulus and the coefficient of the linear expansion of the second rod. Given Young's modulus copper = 1.3×10^{11} N/m², coefficient of the linear expansion of copper= $.1.7 \times 10^{-5}$ /⁰ C

Sol: First part, α_2 can be calculated and then same compressive force applied by the wall, this will give the Young's modulus of the material.

Length of copper rod at 25°C, I₁=30m

Length of second rod at 25°C, I₂=70cm

If α_1 and α_2 are respective linear expansion coefficients, the total expansion of the composite rod when the temperature rises by

$$\Delta t \text{ is } \left(l_1 \alpha_1 + l_2 \alpha_2 \right) \Delta t .$$

$$\therefore \left(30 \times 1.7 \times 10^{-5} + 70 \alpha_2 \right) \times 100 = 0.191$$

$$\alpha_2 = 2 \times 10^{-5} / {}^0 \text{C}$$

If the two rods do not change in length of heating, The compressions of the two rods due to thermal stress must be $l_1\alpha_1\Delta t$ and $l_2\alpha_2\Delta t$ respectively. If A area of cross-section of each rod, then

Tension developed in copper rod, $F_1 = Y_1 A \alpha_1 \Delta t$

Tension developed in second rod, $F_2 = Y_2 A \alpha_2 \Delta t$

 F_1 And F_2 should be equal and opposite

Since the composite rod is in equilibrium,

$$\therefore Y_1 \alpha_1 = Y_2 \alpha_2; Y_2 = Y_1 \alpha_1 / \alpha_2$$
$$= \frac{13 \times 10^{11} \times 1.7 \times 10^{-5}}{2 \times 10^{-5}} = 1.1 \times 10^{11} \text{ N/m}^2$$

JEE Main/Boards

Exercise 1

Q.1 What are the S.I and c.g.s. unit of heat? How are they related?

Q.2 What is the specific heat of water in SI units? Does it vary with temperature?

Q.3 What is the specific heat of gas in an isothermal process?

Q.4 What is principle behind calorimeter?

Q.5 Briefly explain the concept of heat and concept of temperature?

Q.6 Explain what is meant by specific heats of a substance. What are its units? How is molar specific heat different from specific heat?

Q.7 Define the two principle specific heat of gas. Which is greater and why?

Q.8 What do you understand by change of state? What change occurs with temperature, when heat is given to a solid body?

Q.9 A faulty thermometer has its fixed point marked at 5 and 95. The temperature of a body as measured by faulty thermometer is 59. Find the correct temperature of the body on Celsius scale.

Q.10 A blacksmith fixed iron ring on the rim of the wooden wheel of a bullock cart. The diameter of the rim and the ring is 5.243 m and 5.231 m respectively at 27°C. To what temperature should the ring be heated so as to fit rim of the wheel? Coefficient of linear expansion of iron= $1.20 \times 10^{-5} \text{ K}^{-1}$.

Q.11 A sheet of brass is 50 cm long and 10 cm broad at 0°C. The area of the surface increases by 1.9 cm² at 100°C. Find the coefficient of linear expansion of brass?

Q.12 A sphere of aluminum of 0.047 kg is placed for sufficient time in a vessel containing boiling water,

so that the sphere is at 100°C. It is then immediately transferred to 0.14 kg copper calorimeter containing 0.25kg of water of 20°C. The temperature of water rises and attains a steady state at 23°C. Calculate the specific heat capacity of aluminum. Specific heat capacity of copper = 0.386×10^3 Jkg⁻¹K⁻¹. Specific heat capacity of water = 4.18×10^3 K⁻¹

Q13 How many grams of ice at-14°C are needed to cool 200 grams of water from 25°C to 10°C. Take sp. Heat of ice=0.5cal/g⁰C and latent heat of ice=80 cal/g

Q.14 A tank of volume $0.2m^3$ contains Helium gas at a temp. of 300K and pressure 10^5 N/m^2 . Find the amount of heat required to raise the temp. to 500K. The molar heat capacity of helium at constant volume is 3.0 ca/ mole-K. Neglect any expansion in the volume of the tank. Take r=8.31J/mole-K.

Q.15 5 moles of oxygen is heated at constant volume from 10°C to 20°C. Calculate the amount of heat required, if C_p =8 cal/mole °C and R=8.36 joule/ mole°C.

Exercise 2

Single Correct Choice Type

Q.1 Overall change in volume and radii of a uniform cylindrical steel wire are 0.2% and 0.002% respectively when subjected to some suitable force. Longitudinal tensile stress acting on the wire is $(Y = 2.0 \times 10^{11} Nm^{-2})$

(A) $3.2 \times 10^9 \text{Nm}^{-2}$	(B) $3.2 \times 10^7 \text{Nm}^{-2}$
(C) $3.6 \times 10^7 \text{Nm}^{-2}$	(D) $4.08 \times 10^8 \text{Nm}^{-2}$

Q.2 A solid sphere of radius R made of material of bulk modulus K is surrounded by a liquid in a cylindrical container. A massless piston of area A floats on the surface of the liquid. When a mass m is placed on the piston to compress the liquid, the fractional change in the radius of the sphere $\delta R / R$ is

(A) Kmg /A	(B) Kmg /3A
(C) mg /A	(D) mg /3AR

Q.3 A cylindrical wire of radius 1 mm, length 1 m, Young's modulus= 2×10^{11} Nm², Poisson's ratio $\mu = \pi / 10$ is stretched by a force of 100 N. Its radius will become

(A) 0.99998mm	(B) 0.99999mm
(C) 0.99997mm	(D) 0.99995mm

Q.4 A block of mass 2.5kg is heated to a temperature of 500°C and placed a large ice block. What is the maximum amount of ice that can melt (approx.)? Specific heat for the body=0.1 cal/gm°C.

(A) 1kg (B) 1.5 kg (C) 2kg (D) 2.5kg

Q.5 1 kg of ice at- 10°C is mixed with 4.4kg of water at 30°C. The final temperature of mixture is: (specific heat of ice is 2100 J/kg/k)

(A) 2.3°C (B) 4.4°C (C) 5.3°C (D) 8.7°C

Q.6 Steam at 100°C is added slowly to 1400 gm of water at 16°C, until the temperature of water is raised to 80°C. The mass of steam required to do this is $(L_V = 540 \text{ cal/gm})$:

(A) 165gm	(B) 125gm
(C) 250gm	(D) 320gm

Q.7 Ice at 0°C is added to 200g of water initially at 70°C in a vacuum flask. When 50g of ice has been added and has all melted the temperature of the flask and contents is 40°C. When a further 80g of ice has been added and has all melted, the temperature of the whole is 10°C. Calculate the specific latent heat of fusion of

ice. $[Takes_w = 1cal / gm^{\circ}C]$

(A) $3.8 \times 10^5 \text{ J/kg}$ (B) $1.2 \times 10^5 \text{ J/kg}$ (C) $2.4 \times 10^5 \text{ J/kg}$ (D) $3.0 \times 10^5 \text{ J/kg}$

Q.8 A continuous flow water heater (geyser) has an electrical power rating=2 KW and efficiency of conversion of electrical power into heat=80%. If water is flowing through the device at the rate of 100 cc/ sec, and the inlet temperature is 10°C, the outlet temperature will be.

(A) 12.2°C (B) 13.8°C (C) 20°C (D) 16°C

Q.9 A rod of length 2m rests on smooth horizontal floor. If the rod is heated from 0°C to 20°C, find the longitudinal strain developed. ($\alpha = 5 \times 10^{-5}$ /⁰ C)

(A)
$$10^{-3}$$
 (B) 2×10^{-3} (C) Zero (D) None

Q.10 A steel tape gives correct measurement at 20°C. A piece of wood is being measured with the steel tape gives correct measurement at 20°C. A piece of wood is being measured with the steel tape at 0°C. The reading is 25 cm on the tape, The real length of the given piece of wood must be:

(A) 25cm (B) <25cm

(C) >25cm (D) Cannot say

Q.11 A metallic rod 1 cm long with a square crosssection is heated through t°C. If Young's modulus of elasticity of the metal is E and the mean coefficient of linear expansion is α per degree Celsius, then the compressional force required to prevent the rod from expanding along its length is: (Neglect the change of cross-sectional area)

(A) EAαt	(B) $EA \alpha t(1 + \alpha t)$
(C) EA α t(1 $-\alpha$ t)	(D) Ε/ αt

Q 12. A solid ball is completely immersed in a liquid. The coefficient of volume expansion of the ball and liquid are 3×10^{-6} and 8×10^{-6} per°C respectively. The percentage change in upthrust when the temperature is increased by 100°C is.

(A) 0.5%	(B) 0.11%	(C) 1.1%	(D) 0.05%

Previous Years' Questions

Q.1. 70 cal of heat are required to raise the temperature of 2 mole of an ideal diatomic gas at constant pressure from 35°C. The amount of heat required (in calorie) to raise the temperature of the same gas through the same range (30°C to 35°C) at constant volume is. **(1985)**

(A) 30 (B) 50 (C) 70 (D) 90

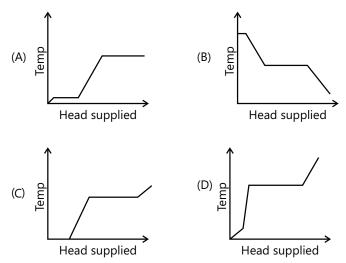
Q.2 Steam at 100°C is passed into 1.1kg of water contained in a calorimeter of water equivalent 0.02kg at 15°C. Till the temperature calorimeter and its constants rises to 80°C. The mass of steam condensed in kg is (1986)

(A) 0.130	(B) 0.065
(C) 0.260	(D) 0.135

Q.3 Two cylinders A and B fitted with piston contain equal amount of an ideal diatomic gas at 300K. The piston of A is free to move, while that of B is held fixed. The same amount of heat is given to the gas in each

cylinder. If the rise in temperature of the gas in A is 30 K, then the rise in temperature of the gas in B is (1988)

Q.4 A block of ice at-10°C is slowly heated and converted to steam at 100°C. Which of the following curves represent the phenomena qualitatively? (2000)



Q.5 Two rods, one made of the aluminum and the other made of steel, having initial length I_1 and I_2 are connected together to form a single rod of length $l_1 + l_2$. The coefficients of linear expansion for aluminum and steel are α_{a} and α_{s} respectively. If the length of each rod increases by the same amount when their temperature

are raised by t°C, then find the ratio (2003)(B) $\frac{\alpha_a}{\Delta}$

$$\begin{array}{c} \alpha_{a} & \alpha_{s} \\ (C) \ \frac{\alpha_{s}}{(\alpha_{a} + \alpha_{c})} & (D) \ \frac{\alpha_{a}}{(\alpha_{a} + \alpha_{c})} \end{array}$$

(A) $\frac{\alpha_{s}}{\Delta}$

Q.6 2 kg ice at-20°C is mixed 5 kg of water at 20°C in an insulating vessel having a negligible heat capacity. Calculate the final mass of water remaining in the container. It is given that the specific heats of water and ice are 1 kcal/kg/°C and 0.5 Kcal/kg/°C while the latent heat of fusion of ice is 80 kcal/kg (2003)

(B) 6kg (A) 7 kg (C) 4kg (D) 2kg

Q.7 Two identical conducting rods are first connected independently to two vessels, one containing water at 100°C and the other containing ice at 0°C.

In the second case, the rods are joined end to end and connected to the same vessels. Let q₁ and q₂ gram per second be the rate of melting of ice in the two cases

respectively	. The ratio	$\frac{q_1}{q_2}$ is		(2004)
(A) $\frac{1}{2}$	(B) ² / ₁	(C) $\frac{4}{1}$	(D) $\frac{1}{4}$	

Q.8 Calorie is defined as the amount of heat required to raise temperature of 1 g of water by 1⁰C and it is defined under which of the following conditions? (2005)

(A) From 14.5°C to 15.5°C at 760 mm of Hg

(B) From 98.5°C to°C 99.5°C at 760 mm of Hg

(C) From 13.5°C to 14.5°C at 76 mm of Hg

(D) From 3.5°C to 4.5°C at 76 mm of Hg

Q.9 This question contains Statement-I and Statement-II. Of the four choices given after the statements, choose the one that best describes the two statements. (2009)

Statement-I: The temperature dependence of resistance is usually given as $R = R_{\alpha}(1 + \alpha \Delta t)$. The resistance of a wire changes from 100 Ω to 150 Ω when its temperature is increased from 27°C to 227°C. This implies that $\alpha = 2.5 \times 10^{-3}$ /°C.

Statement-II: $R = R_i (1 + \alpha \Delta T)$ is valid only when the change in the temperature ΔT is small and $\Delta R = (R - R_a)$ << R_.

(A) Statement-I is true, statement-II is false

(B) Statement-I is true, statement-II is true; statement-II is the correct explanation of statement-I.

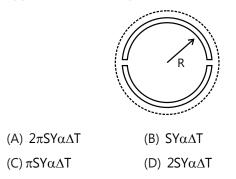
(C) Statement-I is true, statement-II is true; statement-II is not the correct explanation of statement-I.

(D) Statement-I is false, statement-II is true

Q.10 Two conductors have the same resistance at 0°C but their temperature coefficients of resistance are α_1 and α_2 . The respective temperature coefficients of their series and parallel combinations are nearly (2010)

(A)
$$\frac{\alpha_1 + \alpha_2}{2}$$
, $\alpha_1 + \alpha_2$ (B) $\alpha_1 + \alpha_2$, $\frac{\alpha_1 + \alpha_2}{2}$
(C) $\alpha_1 + \alpha_2$, $\frac{\alpha_1 \alpha_2}{\alpha_1 + \alpha_2}$ (D) $\frac{\alpha_1 + \alpha_2}{2}$, $\frac{\alpha_1 + \alpha_2}{2}$

Q.11 A wooden wheel of radius R is made of two semicircular parts (see figure); The two parts are held together by a ring made of a metal strip of cross sectional area S and length L. L is slightly less than 2pR. To fit the ring on the wheel, it is heated so that its temperature rises by DT and it just steps over the wheel. As it cools down to surrounding temperature, it presses the semicircular parts together. If the coefficient of linear expansion of the metal is a, and its Youngs' modulus is Y, the force that one part of the wheel applies on the other part is: **(2012)**



Q.12 Three rods of copper, brass and steel are welded together to form a Y-shaped structure. Area of cross-section of each rod = 4 cm^2 . End of copper rod is maintained at 100°C whereas ends of brass and steel are kept at 0°C. Lengths of the copper, brass and steel rods are 46, 13 and 12 cm respectively. The rods are thermally insulated from surroundings except at ends. Thermal conductivities of copper, brass and steel are

0.92, 0.26 and 0.12 CGS units respectively. Rate of heat flow through copper rod is (2014)

(A) 1.2 cal/s (B)	2.4 cal/s
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(C) 4.8 cal/s (D) 6.0 cal/s

Q.13 A person trying to lose weight by burning fat lifts a mass of 10 kg upto a height of 1 m 1000 times. Assume that the potential energy lost each time he lowers the mass is dissipated. How much fat will he use up considering the work done only when the weight is lifted up ? Fat supplies 3.8×10^7 J of energy per kg which is converted to mechanical energy with a 20% efficiency rate. Take g = 9.8 ms^{-2} (2016)

(A) 6.45 × 10 ⁻³ kg	(B) 9.89 × 10⁻³ kg
(C) 12.89 × 10⁻³ kg	(D) 2.45 × 10⁻³ kg

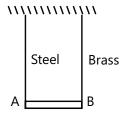
Q.14 A pendulum clock lose 12 s a day if the temperature is 40°C and gains 4 s a day if the temperature is 20°C. The temperature at which the clock will show correct time, and the co-efficient of linear expansion (α) of the metal of the pendulum shaft are respectively: **(2016)**

(A) 60°C ; α = 1.85 × 10 ⁻⁴ /°C
(B) 30° C; $\alpha = 1.85 \times 10^{-3}/{^{\circ}}$ C
(C) 55°C ; $\alpha = 1.85 \times 10^{-2}$ /°C
(D) 25°C ; α = 1.85 × 10 ⁻⁵ /°C

JEE Advanced/Boards

Exercise 1

Q.1 A light rigid bar is suspended horizontally from two vertical wires, one of steel and one of steel brass, as shown in figure. Each wire is 2.00 m long. The diameter of the steel wire is 0.60 mm and the length of the bar AB is 0.20 m. When a mass of 10kg is suspended from the center of AB, bar remains horizontal.



(i) What is the tension in each wire?

(ii) Calculate the extension of the steel wire and the energy stored in it.

(iii) Calculate the diameter of the brass wire.

(iv) If the brass wire is replaced by another brass wire of diameter 1 mm, where should the mass be suspended so that AB would remain horizontal? The Young's modulus for steel= 2.0×10^{11} Pa, the Young's modulus for brass= 1.0×10^{11} Pa.

Q.2 A steel rope has length L, area of cross-section A, Young's modulus Y. [Density=d]

(a) It is pulled on a horizontal frictionless floor with a

constant horizontal force F = [dALg]/2 applied at one end. Find the strain at the midpoint.

(b) If the steel rope is vertical and moving with the force acting vertically upward at the upper, end. Find the strain at a point L/3 from lower end.

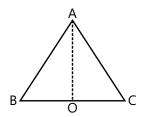
Q.3 An aluminum container of mass 100 gm contains 200 gm of ice at- 20° C. Heat is added to system at the rate of 100 cal/s. Find the temperature of the system after 4 minutes (specific heat of ice=0.5 and L=80 cal /gm, specific heat Al=2.0.cal/gm/°C)

Q.4 A volume of 120 ml of drink (half alcohol + half water by mass) originally at a temperature of 25°C is cooled by adding 20gm ice at 0°C. If all the ice melts, find the final temperature of drink. (Density of drink=0.833 gm/ cc, specific heat of alcohol = 0.6 cal/gm/°C)

Q.5 A hot liquid contained in a container of negligible heat capacity loses temperature at the rate of 3K/min, just before it begins to solidify. The temp remains constant for 30 min.

Find the ratio of specific heat capacity of liquid to specific latent heat of fusion. (Given that of losing heat is constant).

Q.6 Three aluminum rods of equal length form an equilateral triangle ABC. Taking O (midpoint of rid BC) as the origin, find the increase in Y-coordinate of the center of mass per unit change in temperature of the system. Assume the length of each rod is 2m, and $\alpha_{al} = 4\sqrt{3} \times 10^{-6} / ^0 \text{ C}$



Q.7 A thermostat chamber at a small height h above earth's surface maintained at 30°C has a clock fitted in it with an uncompensated pendulum. The clock designer correctly designs it for height h, but for temperature of 20°C. If this chamber is taken to earth's surface, the clock in it would click correct time. Find the coefficient of linear expansion of material of pendulum. (Earth's radius is R)

Q.8 A metal rod A of length 25 cm expands by 0.050cm. When its temperature is raised from 0° C to 100° C,

another rod B of a different metal of length 40cm expands by 0.040cm for the same rise in temperature. A third rod C of 50cm length is made up of pieces of rods A and B placed end to end expands by 0.03 cm on heating from 0°C to 50°C. Find the length of each portion of the composite rod.

Q.9 A wire of cross-section area 4×10^{-4} m² has modulus of elasticity 2×10^{11} N/m² and length 1 m is stretched between two vertical rigid poles. A mass of 1 kg is suspended at its middle. Calculate the angle it makes with horizontal.

Q.10 A copper calorimeter of mass 100 gm contains 200 gm of a mixture of ice and water. Steam at 100°C under normal pressure is passed into the calorimeter and the temperature of the mixture is allowed to rise to 50°C. If the mass of the calorimeter and its contents is now 330 gm, what was the ratio of ice and water in the beginning? Neglect heat losses.

Given: specific heat capacity of copper $= 0.42 \times 10^3 \text{ Jkg}^{-1 \text{ K}-1}$

Specific heat capacity of water

 $= 4.2 \times 10^3 \, \text{Jkg}^{-1 \, \text{K}-1}$

Specific heat of fusion of ice $= 3.36 \times 10^5 \text{ Jkg}^{-1}$

Latent heat of condensation of steam

 $= 22.5 \times 10^5 \, \text{Jkg}^{-1}$

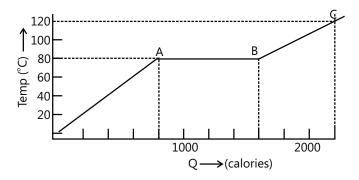
Q.11 Two 50 cm ice cubes are dropped into 250gm of water into a glass. If the water is initially at a temperature of 25°C and the temperature of ice is 15°C. Find the final temperature of water. (Specific heat of ice=0.5cal/gm/°C and L=80 cal/gm). Find the final amount of water and ice.

Q.12 A flow calorimeter is used is measure the specific heat of liquid. Heat is added at a known rate to a steam of the liquid as it passes through the calorimeter at a known rate. Then a measurement of the resulting temperature difference between the inflow and the outflow point of the liquid steam enables us to compute the specific heat of the liquid. A liquid of density 0.2g/ cm³ flows through a calorimeter at the rate of cm³/s. Heat is added by means of a 250-W electric heating oil, and a temperature difference of 25°C is established in steady-state condition between the inflow and the outflow points. Find the specific heat of the liquid.

Q.13 Two identical calorimeters A and B contain equal quantity of water at 20°C. A 5 gm piece of metal X of specific heat 0.2 cal g^{-1} (C°)⁻¹ is dropped into A and 5 gm piece of metal Y into B. The equilibrium temperature in A is 22°C and in B 23°C. The initial temperature of both the metal is 40°C. Find the specific heat of metal Y in cal g^{-1} (C°)⁻¹.

Q.14 The temperature of 100 gm of water is to be raised from 24°C to 90°C by adding steam to it. Calculate the mass of the steam required for this purpose.

Q.15 A substance is in a solid form at 0°C. The amount of heat added to substance and its temperature are plotted in the following graph. If the relative specific heat capacity of the solid substance is 0.5, find from the graph.



(i) The mass of substance;

(ii) The specific latent heat of the melting process, and

(iii) The specific heat of the substance in the liquid state.

Q.16 A solid receives heat by radiation over its surface at the rate of 4kW. The heat convection rate from the surface of solid to the surrounding is 5.2 kW, and heat is generated at a rate of 1.7KW over the volume of the solid. The rate of change of the temperature of the solid is $0.5^{\circ}Cs^{-1}$. Find the heat capacity of the solid.

Q.17 Water is heated from 10°C to 90°C in a residential hot water heater at a rate of 70 liter per minute. Natural gas with a density of 1.2kg/m³ is used in the heater, which has a transfer efficiency of 32%. Find the gas consumption rate in cubic meters per hour. (Heat combustion for natural gas is 8400kcal/kg)

Q.18 If two rods of length L and 2 L having coefficients of linear expansion α and 2α respectively are connected so that length becomes 3 L, determine the average coefficient of linear expansion of the composite rod.

Q.19 A clock pendulum made of invar has a period of 0.5 sec at 20°C. If the clock is used in a climate where average temperature is 30°C, approximately. How much faster or slower will the clock run in 10⁶ sec. ($\alpha_{invar} = 1 \times 10^{-6}$ /°C)

Q.20 A U-tube filled with a liquid of volumetric coefficient of 10^{-5} /°C lies in a vertical plane. The height of liquid column in the left vertical limb is 100 cm. The liquid in the left vertical limb is maintained at a temperature=0°C while the liquid in the right limb is maintained at a temperature=100°C. Find the difference in levels in the two limbs.

Q.21 An iron bar (young's modulus = 10^{11} N/m², $\alpha = 10^{-6}$ /⁰ C) 1 m long and 10^{-3} m² in area is heated from 0°C to 100°C without being allowed to bend or expand. Find the compressive force developed inside the bar.

Q.22 An isosceles triangle is formed with a rod of length I_1 and coefficient of linear expansion α_1 for the base and two thin rods each of length I_2 and coefficient of linear expansion α_2 for the two pieces, if the difference between the apex and the midpoint of the base remain unchanged as the temperatures varied show that

$$\frac{l_1}{l_2} = 2\sqrt{\frac{\alpha_2}{\alpha_1}}$$

Q.23 A steel drill making 180 rpm is used to drill a hole in a block of steel. The mass of the steel block and the drill is 180gm. If the entire mechanical work is used up in producing heat and the rate of rise in temperature of the block and the drill is 0.5°C/s. find

(i) the rate of working of the drill in watts, and

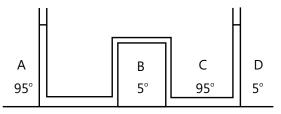
(ii) the torque required to drive the drill.

Specific heat of steel=0.1 and J=4.2 J/cal. Use: $P = \tau \omega$

Q.24 Ice at-20°C is filled up to height h=10cm in a uniform cylindrical vessel. Water at temperature θ °C is filled in another identical vessel up to the same height h= 10 cm. Now water from second vessel is poured into first vessel and it is found that level of upper surface falls through $\Delta h = 0.5$ cm when thermal equilibrium is reached. Neglecting thermal capacity of vessels, change in density of water due to change in temperature and loss of heat due to radiation, calculate initial temperature θ of water.

Given, density of water, $\rho_W = 1 \text{gmcm}^{-3}$ Density of ice, $\rho_i = 0.9 \text{gmcm}^3$ Specific of water, ... $s_W = 1cal / gm^0 C$ Specific heat of ice, Specific $s_i = 0.5cal / gm^0 C$ Latent heat of ice, L = 80cal / gm

Q.25 The apparatus shown in the figure consists of four glass columns connected by horizontal sections. The height of central columns B & C are 49 cm each. The two outer columns A & D are open to the atmosphere. A & C are maintained at a temperature of 95° C while the column B & D are maintained at 5° C. the height of the liquid in A & D measured from the base line are 52.8 cm & 51 cm respectively. Determine the coefficient of thermal expansion of the liquid.

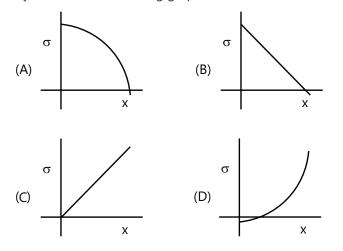


Q.26 Toluene liquid of volume 300 cm³ at 0°C is contained in a beaker and another quantity of toluene of volume 110 cm³ at 100°C is in another beaker. (The combined volume Is 410 cm³). Determine the total Volume of the mixture of the toluene liquid when they are mixed together. Given the coefficient of volume expansion $\gamma = 0.001/C$ and all forms of heat losses can be ignored. Also find the final temperature of the mixture.

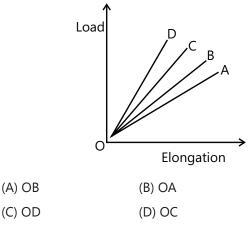
Exercise 2

Single Correct Choice Type

Q.1 A uniform rod is rotating in gravity free region with constant angular velocity. The variation of tensile stress with distance X from axis of rotation is best represented by which of the following graphs.



Q.2 The load versus strain graph for four wires of the same material is shown in the figure. The thickest wire is represented by the line.



Q.3 10 gm of ice at 0°C is kept in a calorimeter of water equivalent 10 gm. How much heat should be supplied to the apparatus to evaporate the water thus formed? (Neglect loss of heat)

(A) 6200 cal	(B) 7200 cal
(C) 13600 cal	(D) 8200 cal

Q.4 Heat is being supplied at a constant rate to a sphere of ice which is melting at the rate 0.1 gm/sec. It melts completely in 100sec. Assumed no loss of heat. The rate of rise of temperature thereafter will be

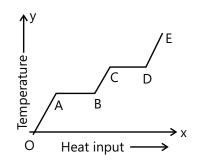
(A) 0.8°C/sec	(B) 5.40°C/sec
(C) 3.6°C/sec	(D) will change with time

Q.5 Ice at 0°C is added to 200g of water initially at 70°C in a vacuum flask. When 50g of ice has been added and has all melted.

The temperature of the flask and contents is 40°C. When a further 80g of ice has been added and has all melted, the temperature of the whole is 10°C. Calculate the specific latent heat of fusion of ice. $\left[\text{Take s}_w = 1 \text{cal/gm}^{0} \text{C} \right]$

(A) $3.8 \times 10^5 \text{ J/kg}$	(B) 1.2×10 ⁵ J/kg
(C) $2.4 \times 10^5 \text{ J/kg}$	(D) 3.0×10 ⁵ J/kg

Q.6 A solid material is supplied with heat at a constant rate. The temperature of material is changing with heat input as shown in the figure. What does slope DE represent

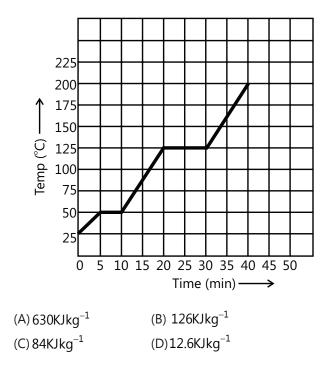


- (A) Latent heat of liquid
- (B) Latent heat of vapour
- (C) Heat capacity of vapour
- (D) Inverse of heat capacity of vapour

Q.7 A block of ice with mass m falls into a lake. After impact, a mass of ice m/5 melts. Both the block of ice and the lake have a temperature of 0°C. If L represents heat of fusion, the minimum distance the ice fell before striking the surface is

L	5L	gL	mL
$(A) \overline{5g}$	(B) <u> </u>	(C) <u>gL</u> 5m	(D) $\frac{mL}{5g}$

Q.8 The graph shown in the figure represents change in the temperature of 5 kg of a substance as it absorbs heat at a constant rate of 42 kJ min⁻¹. The latent heat of vaporization of the substance is:



Q.9 The density of material A is 1500kg/ m^3 and that of another material B is 2000 kg/ m^3 . It is found that the heat capacity of 8 volumes of A is equal to heat capacity of 12 volume of B. The ratio of specific heats of A and B will be

(A) 1:2 (B) 3:1 (C) 3:2 (D) 2:1

Q.10 Find the amount of heat supplied to decrease the volumeofanicewatermixtureby1cm³withoutanychange

in temperature. $(\rho_{ice} = 0.9 \rho_{water}, L_{ice} = 80 \text{ cal / gm}).$

(A) 360 cal	(B) 500 cal
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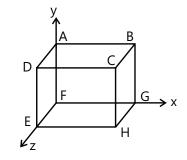
(C) 720 cal (D) None of these

Q.11 Some steam at 100 °C is passed into 1.1kg of water contained in a calorimeter of water equivalent 0.02 kg at 15°C so that the temperature of the calorimeter and its contents rises to 80 °C. What is the mass of steam condensing? (In kg)

(A) 0.130	(B) 0.065
(C) 0.260	(D) 0.135

Q.12 A thin copper wire of length L increases in length by 1% when heated from temperature T_1 to T_2 . What is the percentage change in area when a thin copper plate having dimensions $2L \times L$ is heated from T_1 to T_2 ? (A) 1% (B) 2% (C) 3% (D) 4%

Q.13 The coefficients thermal expansion of steel and metal X are respectively 12×10^{-6} and 12×10^{-6} per °C. At 40°C, the side of a cube of metal X was measured using steel vernier callipers. The reading was 100 mm. assuming that the calibration of the vernier was done at 0°C, then the actual length of the side cube at 0°C will be



(A) >100mm

(B) <100 mm

(C) =100mm

(D) Data insufficient to conclude

Q.14 A cuboid ABCDEFGH is anisotropic with

 $\begin{array}{l} \alpha_x = 1 \times 10^{-5} \ / \ ^\circ C \ \alpha_y = 2 \times 10^{-5} \ / \ ^\circ C \ \alpha_z = 3 \times 10^{-5} \ / \ ^\circ C \ . \end{array}$ Coefficient of superficial. Expansion of faces can be

(A) $\beta_{ABCD} = 5 \times 10^{-5} / °C$ (B) $\beta_{BCGH} = 4 \times 10^{-5} / °C$ (C) $\beta_{CDEH} = 3 \times 10^{-5} / °C$ (D) $\beta_{EFGH} = 2 \times 10^{-5} / °C$

Q.15 The coefficient of apparent expansion of a liquid in a copper vessel is C and in a silver vessel is S. The coefficient of volume expansion of copper is γ_c . What is the coefficient of linear expansion of silver?

(A)
$$\frac{(C + \gamma_{C} + S)}{3}$$
 (B) $\frac{(C - \gamma_{C} + S)}{3}$
(C) $\frac{(C + \gamma_{C} - S)}{3}$ (D) $\frac{(C - \gamma_{C} - S)}{3}$

Q.16 A sphere of diameter 7 cm and mass 266.5gm floats in a bath of a liquid. As the temperature is raised, the sphere just begins to sink at a temperature 35°C. If the density of a liquid at 0°C is 1.527 gm/cc, then neglecting the expansion of the sphere, the coefficient of cubical expansion of the liquid is f:

(A) 8.486×10^{-4} per °C (B) 8.486×10^{-5} per °C (C) 8.486×10^{-6} per °C (D) 8.486×10^{-3} per °C

Q. 17 The volume of the bulb of a mercury thermometer at 0°C is V_0 and cross section of the capillary is A_0 .

The coefficient of linear expansion of glass is α_g per °C and the cubical expansion of mercury γ_m per °C. If the mercury just fills the bulb at 0°C, what is the length of mercury column in capillary at T°C?

(a)
$$\frac{V_0 T \left(\gamma_m + 3\alpha_g\right)}{A_0 \left(1 + 2\alpha_g T\right)}$$
(B)
$$\frac{V_0 T \left(\gamma_m - 3\alpha_g\right)}{A_0 \left(1 + 2\alpha_g T\right)}$$
(c)
$$\frac{V_0 T \left(\gamma_m + 3\alpha_g\right)}{A_0 \left(1 + 3\alpha_g T\right)}$$
(D)
$$\frac{V_0 T \left(\gamma_m - 2\alpha_g\right)}{A_0 \left(1 + 3\alpha_g T\right)}$$

Q.18 A thin walled cylindrical metal vessel of linear coefficient of expansion 10^{-3} °C⁻¹ contains benzene of volume expansion coefficient 10^{-3} °C⁻¹. If the vessel and

its contents are now heated by 10°C, the pressure due to the liquid at the bottom.

(A) Increases by 2% (B	B) decreases by 1%
------------------------	--------------------

(C) decreases by 2% (D) remains unchanged

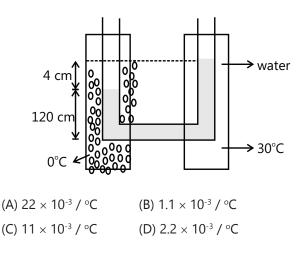
Q.19 A rod of length 20 cm is made of metal. It expands by 0.075 cm when its temperature is raised from 0°C to 100 °C. Another rod of a different metal B having the same length expands by 0.045cm for the same change in temperature, A third rod of the same length is composed of two parts one of metal A and the other of metal B. This rod expands by 0.06 cm for the same change in temperature. The portion made of metal A has the length:

(A) 20cm (B) 10cm (C) 15cm (D) 18cm

Q.20 A glass flask contains some mercury at the room temperature. It is found that at different temperatures the volume of air inside the flask remains the same. If the volume of mercury in the flask is 300cm³, then volume of the flask is (given the coefficient of volume expansion of mercury and coefficient of linear expansion of glass

are $1.8 \times 10^{-4} ({}^{0}C)^{-1}$	respectively)
(A) 4500 cm ³	(B) 450 cm ³
(C) 2000 cm ³	(D) 6000 cm ³

Q.21 Two vertical glass tubes filled with a liquid are connected by a capillary tube as shown in the figure. The tube on the left is put in an ice bath at 0°C while the tube on the right is kept at 30°C in a water bath. The difference in the levels of the liquid in the tube is 4cm while the height of the liquid column at 0°C is 120 cm. The coefficient of volume expansion of liquid is (ignore expansion of glass tube)



Multiple Correct Choice Type

Q.22 A composite rod consists of a steel rod of length 25cm and area 2A and a copper rod of length 50cm and area A. The composite rod is subjected to an axial load F. If the Young's modulus of steel and copper are in the ratio2:1.

(A) The extension produced in copper rod will be more.

(B) The extension in copper and steel part will be in the ratio 2:1.

(C) The stress applied to the copper rod will be more.

(D) No extension will be produced in the steel rod.

Q.23 The wires A and B shown in the figure are mode of the same material and have radii r_A and r_B respectively. The block between them has a mass m. When the force F is mg/3, one of the wires breaks.

(A) A breaks if $r_A = r_B$

(B) A breaks if $r_A < 2r_B$

(C) Either A or B may break if $r_A = 2r_B$

(D) The length of A and B must be known to predict which wire will break

Q.24 Four rods A, B, C, D of same length and material but of different radii r, $r\sqrt{2}$, $r\sqrt{3}$ and 2r respectively are held between two rigid walls. The temperature of all rods is increased by same amount. If the rods do not bend, then

(A) The stress in the rods are in the ratio 1: 2: 3: 4.

(B) The force on the rod exerted by the wall in the ratio 1: 2: 3: 4.

(C) The energy stored in the rods due to elasticity is in the ratio 1: 2: 3: 4.

(D) The strain produced in the rod are in the ratio 1: 2: 3: 4.

Q. 25 A body of mass M is attached to the lower end of a metal wire, whole upper end is fixed. The elongation of the wire is I.

(A) Loss in gravitation potential energy of M is Mgl

(B) The elastic potential energy stored in the wires is Mgl

(C) The elastic potential energy stored in the wires is $1/2\ \mbox{Mgl}$

(D) Heat produced is 1/2 Mgl.

Q.26 An experiment is performed to measure the specific heat of copper. A lump of copper is heated in an oven, and then dropped into a beaker of water. To calculate the specific heat of copper, the experimenter must know or measure the value of all the quantities below EXCEPT the

(A) Heat capacity of water and beaker

(B) Original temperature of the copper and the water

(C) Final (equilibrium) temperature of the copper and the water

(D) Time taken to achieve equilibrium after the copper is dropped into the water

Q.27 When the temperature of a copper coin is raised by 80°C, its diameter increases by 0.2%

(A) Percentage rise in the area of a face is 0.4%

(B) Percentage rise in the thickness is 0.4%

(C) Percentage rise in the volume is 0.6%

(D) Coefficient of linear expansion of copper is $0.25 \times 10^{-4} \ ^0 C^{-1}$

Comprehension Type

(Questions 28 - 31)

Solids and liquids both expand on heating. The density of substance decreases on expanding according to the relation

$$\rho_2 = \frac{\rho_1}{1 + \gamma \left(T_2 - T_1\right)}$$

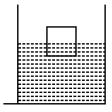
Where, $\rho_1 \rightarrow$ density at T₁; $\rho_2 \rightarrow$ density at T₂

 $\gamma \rightarrow$ coeff. of volume expansion of substances

When a solid is submerged in a liquid, liquid exerts an upward force on solid which is equal to the weight of liquid displaced by submerged part of solid.

Solid will float or sink depending on relative densities of solid and liquid.

A cubical block of solid floats in a liquid with half of its volume submerged in the liquid as shown in figure (at temperature T)



 $\alpha_s \rightarrow$ coeff. of linear expansion of solid

- $\gamma_{\ell} \rightarrow \text{ coeff. of volume expansion of solid;}$
- $\rho_{s} \rightarrow$ Density of solid at temp.T ;
- $\rho_\ell \rightarrow$ Density of liquid at temp.T

Q.28 The relation between density of solid and liquid at temperature T is

(A) $\rho_s = 2\rho_\ell$	(B) $\rho_{\rm s} = (1/2)\rho_{\ell}$
(C) $\rho_s = \rho_\ell$	(D) $\rho_{s} = (1/4)\rho_{\ell}$

Q.29 If temperature of system increases, then fraction of solid submerged in liquid

(A) Increases (B) decreases

(C) Remain the same (D) Inadequate information

Q.30 Imagine fraction submerged does not change on increasing temperature.

The relation between γ_{I} and α_{c} is

- (A) $\gamma_{\ell} = 3\alpha_{s}$ (B) $\gamma_{\ell} = 2\alpha_{s}$
- (C) $\gamma_{\ell} = 4\alpha_s$ (D) $\gamma_{\ell} = (3/2)\alpha$

Q.31 Imagine the depth of the block submerged in the liquid does not change on increasing temperature then

(A) $\gamma_{\ell} = 2\alpha$	(B) $\gamma_{\ell} = 3\alpha$
(C) $\gamma_{\ell} = (3/2)\alpha$	(D) $\gamma_{\ell} = (4/3)\alpha$

Assertion Reasoning Type

Q.32 Statement-I: The coefficient of volume expansion has dimension K⁻¹.

Statement-II: The coefficient of volume expansion is defined as the change in volume per unit volume per unit change in temperature.

(A) Statement-I is true, statement-II is true and Statement-II is correct explanation of statement-I

(B) Statement-I is true, statement-II is true and statement-II is not correct explanation of statement-I

(C) Statement-I is true, statement-II is false

(D) Statement-I is false, statement-II is true

Q.33 Statement-I: Water kept in an open vessel will quickly evaporate on the surface of the moon.

Statement-II: the temperature at the surface of the moon is much higher than saturation point of the water.

Q.34 Statement-I: When a solid iron ball is heated, percentage increase in its volume is largest.

Statement-II: Coefficient of superficial expansion is twice that of linear expansion whereas coefficient of volume expansion is three time of linear expansion.

Q.35 Statement-I: A beaker is completely filed with water at 4°C. It will over flow, both when heated or cooled.

Statement-II: There is expansion of water below and above 4°C.

Q.36 Statement-I: latent heat of fusion of ice is 336000 Jkg⁻¹

Statement-II: latent heat refers to change of state without any change in temperature.

Q.37 Statement-I: Specific heat of a body is always greater than its thermal capacity.

Statement-II: Thermal capacity is the heat required for raising temperature of unit mass of the body through unit degree.

Previous Year's Questions

Q.1 A bimetallic strip is formed out of two identical strips-one of copper and other of brass. The coefficient of linear expansion of the two metals are α_c and α_B . On heating, the temperature of the strip goes up by ΔT and the strip bends to form an arc of radius of curvature R. then, R is (1999)

- (A) Proportional to ΔT
- (B) Inversely proportional to ΔT
- (C) Proportional to $\alpha_{\rm B} \alpha_{\rm C}$
- (D) Inversely proportional to $\left|\alpha_{\rm B} \alpha_{\rm C}\right|$

Q.2 300g of water at 25°C is added to 100g of ice at 0°C. The final temperature of the mixture is ...°C (1989)

Q.4 At given temperature, the specific heat of a gas at a constant pressure is always greater than its specific heat at constant volume. (True or False) (1987)

Q.5 The temperature of 100g of water is to be raised from 24°C to 90°C by adding steam to it. Calculate the mass of the steam required for this purpose, (1996)

Q.6 A cube of coefficient of linear expansion α_s is floating in a bath containing a liquid of coefficient of volume expansion γ_1 . When the temperature is raised by ΔT , the depth up to which the cube is submerged in the liquid remain the same. Find the relation between γ_1 and α_s showing all the steps. (2004)

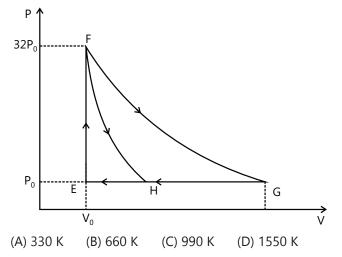
Q.7 In an insulated vessel, 0.05 kg steam at 373 K and 0.45kg of ice at 253 K are mixed. Find the final temperature of the mixture (in Kelvin). *(2006)*

Given, L _{fusion} = 80 cal/g=336 J/g, L _{vaporization} = 540 cal/g = 2268 J/g, S _{ice} = 2100 J/kg, K=0.5 cal/g-K and S _{water} = 4200 J/kg, K = 1cal/g-K

Q.8 A piece of ice (heat capacity = $2100Jkg^{-1}cC^{-1}$ and latent heat = $3.36 \times 10^5 Jkg^{-1}$) of mass m gram is at -5°C at atmospheric pressure. It is given 420J of heat so that the ice starts melting. Finally when the ice- water mixture is in equilibrium, it is found that 1 g of ice has melted. Assuming there is no other heat exchange in the process, the value of m is? **(2010)**

Q.9 A metal rod AB of length 10x has its one end A in ice at 0°C and the other end B in water at 100°C. If a point P on the rod is maintained at 400°C, then it is found that equal amounts of water and ice evaporate and melt per unit time. The latent heat of evaporation of water is 540 cal/g and latent heat of melting of ice is 80 cal/g. If the point P is at a distance of λx from the ice end A, find the value of λ . [Neglect any heat loss to the surrounding.] **(2009)**

Q.10 Steel wire of length 'L' at 40°C is suspended from the ceiling and then a mass 'm' is hung from its free end. The wire is cooled down from 40°C to 30°C to regain its original length 'L'. The coefficient of linear thermal expansion of the steel is 10^{-5} /°C, Young's modulus of steel is 10^{11} N/m² and radius of the wire is 1 mm. Assume that L >> diameter of the wire. Then the value of 'm' in kg is nearly: (2011) **Q.11** Parallel rays of light of intensity I = 912 Wm⁻² are incident on a spherical black body kept in surroundings of temperature 300 K. Take Stefan-Boltzmann constant $\sigma = 5.7 \times 10^{-8}$ Wm⁻² K⁻⁴ and assume that the energy exchange with the surroundings is only through radiation. The final steady state temperature of the black body is close to **(2014)**



Q.12 An incandescent bulb has a thin filament of tungsten that is heated to high temperature by passing an electric current. The hot filament emits blackbody radiation. The filament is observed to break up at random locations after a sufficiently long time of operation due to non-uniform evaporation of tungsten from the filament. If the bulb is powered at constant voltage, which of the following statement(s) is(are) true? **(2016)**

(A) The temperature distribution over the filament is uniform

(B) The resistance over small sections of the filament decreases with time

(C) The filament emits more light at higher band of frequencies before it breaks up

(D) The filament consumes less electrical power towards the end of the life of the bulb

Q.13 The ends Q and R of two thin wires, PQ and RS, are soldered (joined) together. Initially each of the wires has a length of 1 m at 10°C. Now the end P is maintained at 10°C, while the end S is heated and maintained at 400°C. The system is thermally insulated from its surroundings. If the thermal conductivity of wire PQ is twice that of the wire RS and the coefficient of linear thermal expansion of PQ is 1.2×10^{-5} K⁻¹, the change in length of the wire PQ is **(2016)**

(A) 0.78 mm (B) 0.90 mm (C) 1.56 mm (D) 2.34 mm

PlancEssential Questions

JEE Main/Boards		JEE Advanced/Boards		
Exercise	1	Exercise 1		
Q. 10	Q.14	Q.1	Q.6	Q.8
		Q.13	Q.15	Q.25
Exercise 2		Exercise 2		
Q.8	Q.10	Q. 1	Q.2	Q.19
		Q.23	Q.24	

Answer Key

JEE Main/Boards EXERCISE 1

Q.1 1 joule=10 ⁻⁷ e	ergs	Q.2 4180 J kg ⁻¹ K ⁻¹ , yes		Q.3 c = $\frac{\Delta Q}{m\Delta T}$	
Q.4 Heat gained= × fall in its tempe		of the body sp. heat	× rise its temperatu	ire=mass of the oth	er body × sp. Heat
Q.9 60°C		Q.10 217.73°C		Q.11 1.9× 10 ⁻⁵ K ⁻¹	
Q.12 911 J kg ⁻¹ K ⁻¹	1	Q.13 31g		Q.14 4813.2cal.	
Q.15 300 cal					
Exercise 2					
Single Correct Choice Type					
Q.1 D	Q.2 B	Q.3 D	Q.4 B	Q.5 D	Q.6 A
Q.7 A	Q.8 B	Q.9 C	Q.10 B	Q.11 B	Q.12 D
Previous Year's Questions					
Q.1 B	Q.2 D	Q.3 D	Q.4 A	Q.5 C	Q.6 B
Q.7 C	Q.8 A	Q.9 A	Q. 10 D	Q.11 D	Q.12 C
Q.13 C	Q.14 D				

JEE Advanced/Boards

Exercise 1

Q.1 (i) 50N, (ii) 1.77 cm, 0.045 J (iii) 8.48×10 ⁻⁴ m (iv) x=0.12m Q.2 (a) (dgL)/4Y, (b) (dgL)/6Y						
Q.3 25.5°C	Q.4 4°C	Q.5 1/90	Q.6 4×10 ⁻⁶ m/°C Q.7 h/5R			
Q.8 10cm, 40cm	Q.9 1/200 rad	Q.10 1: 1.26	Q.11 0 °C,125 / 4 g ice, 1275/4g water			
Q.12 5000 J/°C Kg	Q.13 27/85	Q.14 12gm	Q.15 (i) 0.02kg (ii)	40,000calkg ⁻¹ K ¹ (iii) 750 cal/ kg °C	
Q.16 1000 J (C°) ⁻¹	Q.17 104.16 M ³ λ	⁻¹ Q.18 5α / 3	Q.19 5sec slow	Q.20 0.1cm		
Q.21 10,000N	Q.23 (a) 37.8J/s (w	vatts,), (b) 2.005 N-r	n	Q.24 45°C		
Q.25 2×10 ⁻⁴ °C	Q.26 Decrease by	0.75cm³, 25°C				
Exercise 2						
Single Correct Ch	noice Type					
Q.1 A	Q.2 C	Q.3 D	Q.4 A	Q.5 A	Q.6 D	
Q.7 A	Q.8 C	Q.9 D	Q.10 C	Q.11 A	Q.12 B	
Q.13 A	Q.14 C	Q.15 C	Q.16 A	Q.17 B	Q.18 C	
Q.19 B	Q.20 D	Q.21 C				
Multiple Correct	Choice Type					
Q.22 A, C	Q.23 A, B, C	Q.24 B, C	Q.25 A, C, D	Q.26 D	Q.27 A, C, D	
Comprehension ⁻	Туре					
Q.28 B	Q.29 D	Q.30 A	Q.31 A			
Assertion Reasor	ning Type					
Q.32 A	Q.33 A	Q.34 A	Q.35 B	Q.36 B	Q.37 D	
Previous Year's Questions						
Q.1 B, D	Q.2 6.25 grams	Q.3 L = $\frac{Pt}{M}$	Q.4 true	Q.5 12g	Q.6 $\gamma_I = 2\alpha_s$	
Q.7 273 K	Q.8 8	Q.9 9	Q.10 3	Q.11 A	Q.12 A, D	
Q.13 A						

Solutions

JEE Main/Boards

Exercise 1

Sol 1: S.I unit of heat = joules C.g.s unit of heat = erg. and of 1 joule = 1 newton × 1m = 10^5 Dyne × 10^2 cm = 10^7 Dyne × cm

 $1 \text{ Joule} = 10^{-7} \text{ Erg}$

Sol 2: Specific heat of water at approximately room temp is $4180 \text{ J Kg}^{-1} \text{ K}^{-1}$.

Yes, the specific heat of water varies with the temp.

Sol 3: Now for isothermal process $\Delta T = 0$, but if heat is not zero \Rightarrow specific heat $\rightarrow \infty$

$$C = \frac{\Delta Q}{m\Delta T} \text{ as } \Delta T \to 0$$
$$C \to \infty.$$

Sol 4: When two bodies at different temp are mixed, the heat will pass from a body at higher temp to a lower temp body until the temp of the mixture becomes constant. The principle of calorimetry implies that heat lost by a body at a higher temperature is equal to heat gained by another body at a lower temperature assuming that there is no loss of heat to the surroundings.

Sol 5: Heat \Rightarrow Heat is the energy that is transferred from one body to another because of temperature difference.

Temperature \Rightarrow Temperature of a body is basically a measure of the energy that the particles of that body have. [Vibrational energy]

Sol 6: Specific heat is amount of energy required to increase the temperature of 1 kg of a substance by 1° C so its units: J. kg⁻¹K⁻¹ Molar specific heat is energy required to increase the temperature of 1 mole of a substance by 1° C.

Sol 7: The principal specific heat capacities of a gas:

(a) The specific heat capacity at constant value (C_v) is defined as the quantity of heat required to raise the temperature of 1 kg of gas by 1 K, if the volume of gas remains constant.

(b) The specific heat capacity at constant pressure (C_p) is defined as the quantity of heat required to raise the temperature of 1 kg of gas by 1K, if the pressure of gas is constant. C_p is always greater than C_v since if the volume of the gas increases, work must be done by the gas to push back the surroundings.

Sol 8: Change of state occurs because of the weakening of the intermolecular forces between the molecules of the substance, once heat is given to the body. As temp increases, the molecular vibrations increases and the intermolecular forces weaken.

Sol 9: Correct thermometer = 0°C and 100°C

So ratio =
$$\frac{95-5}{0+100-0}$$
 = 0.9
So 0.9 scale of faulty = 1 scale of correct

$$\Rightarrow 5 + 0.9 x = 59$$
$$\Rightarrow x = \frac{54}{0.9} = 60$$
so x = 60°C

Sol 10: We have
$$L = L_0 (1 + \alpha \Delta T)$$

$$\Rightarrow L/L_0 = 1 + \alpha \Delta T$$

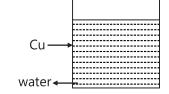
$$\Rightarrow \Delta T = \frac{(1 - L / L_0)}{\alpha} = \left(\frac{1 - 5.231 / 5.243}{1.2 \times 10^{-5}}\right)$$

$$\Rightarrow \Delta T = 190.73 \text{ K} \Rightarrow T - 27 = 190.73$$

$$\Rightarrow T = 217.73^{\circ}\text{C}$$

Sol 11: $A_0 = 500 \text{ cm}^2$. $\Delta A = 1.9 \text{ cm}^2$ Now, $\Delta A = 2\alpha A_0 (\Delta T)$ $\Rightarrow 1.9 \text{ cm}^2 = 2 \times \alpha (500 \text{ cm}^2)(100\text{K})$ $\Rightarrow \alpha = 1.9 \times 10^{-5} \text{ K}^{-1}$

Sol 12:



Now, amount of heat lost by the aluminium ball = amount of heat gained by

(Container + water)

$$\Rightarrow M_{A} \cdot S_{A} \cdot \Delta T_{A}$$

$$= M_{C} \cdot S_{C} \cdot \Delta T_{C} + M_{W} \cdot S_{W} \cdot \Delta T_{W} \cdot$$

$$\Rightarrow S_{A} = \frac{M_{C} \cdot S_{C} \cdot \Delta T_{C} + M_{W} \cdot S_{W} \cdot \Delta T_{W}}{M_{A} \cdot \Delta T_{A}}$$

$$= \frac{0.14 \times 0.386 \times 10^{3} \times (23 - 20) + 0.25 \times 4.13 \times 10^{3} \times (23 - 20)}{0.047 \times (100 - 23)}$$

$$= 0.911 \times 10^{3} = 911 \text{ J Kg}^{-1} \text{K}^{-1}$$

Sol 13: Let the mass of ice be m (in grams) then head gained by ice

= m . S_i . Δ T + m . L + m . S_w . Δ T = m . (0.5) × (14) + m . (80) + m . 1 × 10 = 17m + 80 m = 97m And heat lost by water = m . S_w . Δ T = 200 × 1 × (25 – 10) = 200 × 15 So assuming no heat loss to surroundings $200 \times 15 = 97 \text{ m}$ $\Rightarrow m = \frac{200 \times 15}{97} = 30.93 \text{ gm} \approx 31 \text{ gm}.$

Sol 14: We have PV = nRT $\Rightarrow n = \frac{PV}{RT} = \frac{10^5 \times 0.2}{8.31 \times 300}$ $= \frac{2 \times 100}{8.31 \times 3} = 8.022 \text{ moles}$ Now volume = Const. So heat supplied = n . Cv . ΔT 8.022 mol × 3.0 $\frac{\text{cal}}{\text{mole.K}} \times (500 - 300)\text{K}$ = 4813.2 cal Sol 15: We have $C_p = C_v + R$ R= 8.36 joules/mole $^{\circ}\text{C} = \frac{8.36}{4.18} \text{ cal/mole}^{\circ}\text{C}$ R= 2 cal/mole $^{\circ}\text{C}$ so $C_p = C_v + R \Rightarrow C_v = C_p - R$ = (8 - 2) cal/mole $^{\circ}\text{C} = 6 \text{ cal/mole}^{\circ}\text{C}$ So $Q = nC_v\Delta T$ = 5 × 6 × (20 - 10) = 300 cal.

Exercise 2

Single Correct Choice Type

Sol 1: (D)
$$V = A \times \lambda$$

$$\Rightarrow \frac{dV}{V} = \frac{dA}{A} + \frac{d\ell}{\ell}$$

$$\Rightarrow \frac{0.2}{100} = -2 \times \frac{dr}{r} + \frac{d\ell}{\ell}$$

$$\Rightarrow \frac{d\ell}{\ell} = \frac{0.2}{100} - \left(\frac{-2 \times 0.002}{100}\right)$$

$$\frac{d\ell}{\ell} = \frac{0.2 + 0.004}{100} \Rightarrow \frac{0.204}{100}$$
So stress = Y × strain

$$= 2 \times 10^{11} \times \frac{0.204}{100} = 4.08 \times 10^8 \text{ N/m}^2.$$
Sol 2: (B) $\frac{1}{K} = \frac{-1.\partial V}{V\partial p}$ and $\Delta P = \frac{\text{mg}}{A}$ So

$$\frac{\Delta P}{K} = \frac{dV}{V} = \frac{4\pi R^2 \cdot dR}{\frac{4\pi}{3}R^3} = \frac{3dR}{R}$$
$$= \frac{mg}{3AK} = \frac{dR}{R}$$

After correction

Sol 3: (D) Stress = Y × Strain

$$\Rightarrow$$
 Strain = Stress/Y

$$= \frac{100}{\pi r^2} \times \frac{1}{2 \times 10^{11}} = \frac{1}{2 \times 10^9 \times 3.14 \times 10^{-6}}$$
$$= \frac{1}{6.28 \times 10^3} = \frac{10}{6.28} \times 10^{-4} = 1.6 \times 10^{-4}$$
Now, $\mu \cdot \frac{d\ell}{\ell} = \frac{-dr}{r} \Rightarrow dr = -1 \text{ mm} \times \mu \times \frac{d\ell}{\ell}$
$$= \frac{-1.6 \times 10^{-4} \times 3.14}{10}, r - r_0 = -5.024 \times 10^{-5}$$

Sol 4: (B) 2.5 × 10³ gm. (0.1 cal/gm^oC) . (500 – 0) = m × L $\Rightarrow \frac{2.5 \times 100 \times 0.1 \times 500}{80} = m.$ = 1.5625 × 10³ g

Sol 5: (D) 1 cal = 4.2 J ⇒ Specific heat of ice = $\frac{21000}{42}$ cal/Kg. K = 500 cal/kg. K = 0.5 cal/gm . K So suppose the mixture is at temperature T, then $m_i \cdot S_i \cdot (\Delta T) + m_i L = + m_i \cdot S_w (T - 0)$ = $m_w \cdot S_w (30 - T)$ ⇒ 1000 × 0.5 × 10 + 80 × 1000 + 1000 × 1 × T = 4400 × 1 × (30 - T) ⇒ 5000 + 80000 + 1000T = 4400 × 30 - 4400T ⇒ 5400T = 47000 ⇒ T = 8.7°C

Sol 6: (A) ms $\Delta T = m_s \cdot L_v$ $\Rightarrow 1400 \times 1 \times 64 = m \times 540$

....

Sol 7: (A) Let the heat capacity of the flask be M Then L = latent heat of fusion Then 50 L + 50(40 - 0) = $200 \times (70 - 40) + (70 - 40) \times M$ ⇒50 L + 2000 = 6000 + 30 M \Rightarrow 5L = 3M + 400 ...(i) And 80L + 80 (10 - 0)=250 × (40 - 10) + M (30) ⇒80L + 800 = 7500 + 30 M ⇒8L = 3M + 670 \Rightarrow 8L = 5L - 400 + 670 \Rightarrow L = 90 cal/gm \Rightarrow 90 × 4.2 × 10³ J/kg = 3.8 × 10⁵ J/Kg **Sol 8: (B)** $\frac{dV}{dt}$ = 100 cm³/sec $\Rightarrow \frac{dm}{dt} = \rho \cdot \frac{dV}{dt} = 100 \text{ gm/sec.}$ Now, power used in heating = $2000 \times 0.8 = 1600$ W. Now, power = $\frac{d(ms\Delta T)}{dt}$ = s. ΔT . $\frac{dm}{dt}$ Now assuming ΔT is same So $1600 = \frac{100}{1000} \frac{\text{kg}}{\text{sec}} \times 4200 \frac{\text{J}}{\text{kg}.\text{K}} \times \Delta \text{T}$ $\Rightarrow \frac{1600 \times 10}{4200} = \Delta T = 3.8^{\circ}C.$ \Rightarrow T – 10° = 3.8° \Rightarrow T = 13.8°C (B)

Sol 10: (B) Refer theory

Sol 11: (B) Actual length = $L_0(L + \alpha \Delta T) = L_0(1 + \alpha t)$ Change in length = $L_0(1 + \alpha t) - L_0 = L_0 \alpha t$ So strain = $\frac{L_0 \alpha t}{L_0(1 + \alpha t)} = \frac{\alpha t}{(1 + \alpha t)}$ \Rightarrow Stress = $E \times \text{strain} = \frac{E \alpha t}{(1 + \alpha t)}$ \Rightarrow Force = $A \times \text{stress} = \frac{E A \alpha t}{1 + \alpha t}$ **Sol 12: (D)** $\rho_\ell(t) \cdot V_s(t) \cdot g = \frac{\rho_\ell}{(1 + 8 \times 10^{-6} \times 10^2)}$ $\times v_s(1 + 3 \times 10^{-6} \times 10^2) \times g$ $= \rho_\ell \cdot v_s \cdot g \cdot (1 + 3 \times 10^{-4}) (1 - 8 \times 10^{-4})$ so difference = $\rho_\ell \cdot v_s \cdot g (-5 \times 10^{-4})$

Previous Years' Questions

Sol 1: (B)
$$Q_1 = nC_p \Delta T$$
, $Q_2 = nC_v \Delta T$,
 $\frac{Q_2}{Q_1} = \frac{C_v}{C_p} = \frac{1}{\gamma}$ or $Q_2 = \frac{Q_1}{\gamma} = \frac{70}{1.4} = 50$ cal

Sol 2: (D) Heat required

 $Q = (1.1 + 0.02) \times 10^3 \times 1 \times (80 - 15)$

= 72800 cal.

. .

Therefore, mass of steam condensed (in kg)

m =
$$\frac{Q}{L} = \frac{72800}{540} \times 10^{-3} = 0.135 \text{ kg}$$

Sol 3: (D) A is free to move, therefore, heat will be supplied at constant pressure

$$\therefore \quad dQ_{A} = nC_{p}dT_{A} \qquad ...(i)$$

B is held fixed, therefore, heat will be supplied at constant volume.

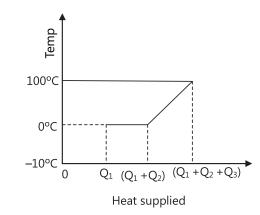
$$\therefore \quad dQ_{B} = nC_{v}dI_{B} \qquad ...(II)$$

But $dQ_{A} = dQ_{B} \qquad (given)$
$$\therefore \quad nC_{p}dT_{A} = nC_{v}dT_{B} \therefore dT_{B} = \left(\frac{C_{p}}{C_{v}}\right)dT_{A}$$

$$= \gamma(dT_{A}) [\gamma = 1.4 \text{ (diatomic)}]$$

 $(dT_{A} = 30 \text{ K}) = (1.4) (30 \text{ K}); \therefore \quad dT_{B} = 42 \text{ K}$

Sol 4: (A) The temperature of ice will first increase from – 10°C to 0°C. Heat supplied in this process will be



 $Q_1 = ms_i(10)$

where, m = mass of ice

 $s_i = specific heat of ice$

Then, ice starts melting. Temperature during melting will remain constant (0°C).

Heat supplied in this process will be

 $Q_2 = mL$, L = latent heat of melting.

Now the temperature of water will increase from 0°C to 100°C. Heat supplied will be

 $Q_3 = ms_w (100)$

where, $s_w =$ Specific heat of water.

Finally, water at 100°C will be converted into steam at 100°C and during this process temperature again remains constant. Temperature versus heat supplied graph will be as shown in figure.

Sol 5: (C) Given
$$\Delta \ell_1 = \Delta \ell_2$$
 or $\ell_1 \alpha_a t = \ell_2 \alpha_5 t$
 $\therefore \quad \frac{\ell_1}{\ell_2} = \frac{\alpha_s}{\alpha_a} \text{ or } \frac{\ell_1}{\ell_2 + \ell_2} = \frac{\alpha_s}{\alpha_a + \alpha_s}$

Sol 6: (B) Heat released by 5 kg of water when its temperature falls from 20°C to 0°C is,

 $Q_1 = mC\Delta\theta = (5)(10^3)(20-0) = 10^5 cal$

when 2 kg ice at – 20° C comes to a temperature of 0° C, it takes an energy

$$Q_2 = mC\Delta\theta = (2)(500)(20) = 0.2 \times 10^5 cal$$

The remaining heat

 $Q = Q_1 - Q_2 = 0.8 \times 10^5$ cal will melt a mass m of the ice,

Where, m = $\frac{Q}{L} = \frac{0.8 \times 10^5}{80 \times 10^3} = 1 \text{ kg}$

So, the temperature of the mixture will be 0° C, mass of water in it is 5 + 1 = 6 kg and mass of ice is 2 - 1 = 1 kg.

Sol 7: (C)
$$\frac{dQ}{dt} = L\left(\frac{dm}{dt}\right)$$

or $\frac{\text{Temperaute difference}}{\text{Thermal resistance}} = L\left(\frac{dm}{dt}\right)$
or $\frac{dm}{dt} \propto \frac{1}{\text{Thermal resistance}}$; $q \propto \frac{1}{R}$

In the first case rods are in parallel and thermal resistance is $\frac{R}{2}$ while in second case rods are in series and thermal resistance is 2R.

$$\frac{q_1}{q_2} = \frac{2R}{R/2} = \frac{4}{1}$$

Sol 8: (A) 1 Calorie is the heat required to raise the temperature of 1 g of water from 14.5°C to 15.5°C at 760 mm of Hg.

Sol 9: (A) A current loop ABCD is held fixed on the plane of the paper as shown in the figure. The arcs BC (radius = b) and DA (radius = a) of the loop are joined by two straight wires AB and CD. A steady current I is flowing in the loop. Angle made by AB and CD at the origin O is 30°. Another straight thin wire with steady current I_1 flowing out of the plane of the paper is kept at the origin.

Sol 10: (D) Let ${\rm R_{_0}}$ be the initial resistance of both conductors

 $\therefore \text{ At temperature q their resistance will be,}$ $R_{1} = R_{0} (1 + \alpha_{1} \theta) \text{ and } R_{2} = R_{0} (1 + \alpha_{2} \theta)$ for, series combination, $R_{s} = R_{1} + R_{2}$ $R_{s0} (1 + \alpha_{s} \theta) = R_{0} (1 + \alpha_{1} \theta) + R_{0} (1 + \alpha_{2} \theta)$ where $R_{s0} = R_{0} + R_{0} = 2R_{0}$ $\therefore 2R_{0} (1 + \alpha_{s} \theta) = 2R_{0} + R_{0} \theta(\alpha_{1} + \alpha_{2} \theta)$ or $\alpha_{s} = \frac{\alpha_{1} + \alpha_{2}}{2}$ For parallel combination, $R_{p} = \frac{R_{1}R_{2}}{R_{1} + R_{2}}$ $R_{p0} (1 + \alpha_{p}\theta) = \frac{R_{0}(1 + \alpha_{1}\theta)R_{0}(1 + \alpha_{2}\theta)}{R_{0}(1 + \alpha_{1}\theta) + R_{0}(1 + \alpha_{2}\theta)}$ Where, $R_{p0} = \frac{R_{0}R_{0}}{R_{0} + R_{0}} = \frac{R_{0}}{2}$ $\therefore \frac{R_{0}}{2} (1 + \alpha_{p}\theta) = \frac{R_{0}^{2}(1 + \alpha_{1}\theta + \alpha_{2}\theta + \alpha_{1}\alpha_{2}\theta)}{R_{0}(2 + \alpha_{1}\theta + \alpha_{2}\theta)}$

As α_1 and α_2 are small quantities

 $\therefore \alpha_1 \alpha_2$ is negligible

or
$$\alpha_{p} = \frac{\alpha_{1} + \alpha_{2}}{2 + (\alpha_{1} + \alpha_{2})\theta} = \frac{\alpha_{1} + \alpha_{2}}{2} \Big[1 - (\alpha_{1} + \alpha_{2})\theta \Big]$$
as
$$(\alpha_{1} + \alpha_{2})^{2} \text{ is negligible}$$

$$\therefore \qquad \alpha_{p} = \frac{\alpha_{1} + \alpha_{2}}{2}$$

Sol 11: (D) If temperature increases by ΔT ,

Increase in length L, $\Delta L = L\alpha \Delta T$

$$\therefore \frac{\Delta L}{L} = \alpha \Delta T$$

Let tension developed in the ring is T.

$$\therefore \frac{\mathsf{T}}{\mathsf{S}} = \mathsf{Y} \frac{\Delta \mathsf{L}}{\mathsf{L}} = \mathsf{Y} \alpha \Delta \mathsf{T}$$
$$\therefore \mathsf{T} = \mathsf{S} \mathsf{Y} \alpha \Delta \mathsf{T}$$

From FBD of one part of the wheel,

F = 2T

Where, F is the force that one part of the wheel applies on the other part.

 \therefore F = 2SY $\alpha\Delta$ T

Sol 12: (C)
$$Q = Q_1 + Q_2$$

$$\begin{array}{c} & & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} B \\ & & \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} B \\ & & \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} B \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.92 \times 4(100 - T) \\ & & \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.26 \times 4 \times (T - 0) \\ & & \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.92 \times 4(100 - T) \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.26 \times 4 \times (T - 0) \\ & & \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.12 \times 4 \times T \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.26 \times 4 \times (T - 0) \\ & & \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.12 \times 4 \times T \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.26 \times 4 \times (T - 0) \\ & & \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.12 \times 4 \times T \\ & & \\ \end{array}$$

$$\begin{array}{c} 0.22 \times 4 \times 60 \\ & & \\ \end{array}$$

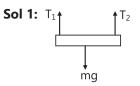
$$\begin{array}{c} 0.26 \times 4 \times (T - 0) \\ & & \\ \end{array}$$

Sol 13: (C) Let m mass of fat is used. $m(3.8 \times 10^7) \frac{1}{5} = 10(9.8)(1)(1000)$ $m = \frac{9.8 \times 5}{3.8 \times 10^3} = 12.89 \times 10^{-3} \text{kg}$

Sol 14: (D)

JEE Advanced/Boards

Exercise 1



(i) $2T = mg = 10 \times 10 = 100$ (from force and moment balance

$$\Rightarrow T = 50 \text{ N (Tension in each wire)}$$

$$T_{1} = T_{2} \text{ (moment)}$$

$$2T = \text{mg (Force eq.)}$$
(ii) $\frac{\Delta \ell}{\ell} = \text{strain} = \frac{\text{stress}}{Y} = \frac{50 / \pi (0.3 \times 10^{-3})^{2}}{2 \times 10^{11}}$

$$= \frac{50}{\pi \times (0.3)^{2} \times 2 \times 10^{5}}$$

$$= \frac{50}{\pi \times 2 \times (0.3)^{2}} \times 10^{-5}$$

$$= 8.85 \times 10^{-4}$$

$$\Rightarrow \Delta \ell = 8.85 \times 10^{-4} \times 2$$

$$= 1.77 \text{ cm.}$$
Now energy = $\frac{1}{2} \times \text{stress} \times \text{strain} \times A\ell$

$$= \frac{1}{2} \times Y \times (\text{strain})^{2} \times A\ell$$

$$= \frac{1}{2} \times 2 \times 10^{10} \times (8.85 \times 10^{-4})^{2} \times \pi \cdot (0.3 \times 10^{-3})^{2}$$

$$= (8.85)^{2} \times 10^{3} \times \pi \times (0.3)^{2} \times 10^{-6} \times 2$$

$$= (8.85)^{2} \times \pi \times (0.3)^{2} \times 2 \times 10^{-3}$$

$$= 0.045 \text{ J}$$
(iii) $\Delta \ell$ for both has to be same.

$$\Rightarrow \text{ Strains has to be same (ℓ is same for both)$$
Thus, $\frac{F/A_{1}}{y_{1}} = \frac{F/A_{2}}{y_{2}}$

$$\Rightarrow A_{2}Y_{2} = A_{1}Y_{1} \Rightarrow 2 \times 10^{11} \times \pi (0.3 \times 10^{-3})^{2}$$

$$= 1 \times 10^{11} \times \pi \times r_{1}^{2}$$

$$\Rightarrow r_{1} = \sqrt{2} \times 0.3 \times 10.3 \text{ m.}$$

$$\Rightarrow d = 0.848 \times 10^{-3} \text{ m}$$

= 0.848 × 10⁻⁴ m

(iv) For strains to be some (given condition is possible only when the mass is suspended at some distance from centre)

$$\frac{F_{s} / A_{s}}{y_{s}} = \frac{F_{B} / A_{B}}{y_{B}}$$

$$\Rightarrow \frac{F_{s}}{A_{s}.y_{s}} = \frac{F_{B}}{A_{B}.y_{B}}$$

$$\Rightarrow \frac{F_{s} \times 4}{\pi d_{s}^{2} \times y_{s}} = \frac{F_{B} \times 4}{d_{B}^{2} \times y_{B} \times \pi}$$

$$\frac{F_{s}}{F_{B}} = \frac{ds^{2} \times y_{s}}{d_{B}^{2} \times y_{B}}$$

$$= \frac{(0.6)^{2} \times 2 \times 10^{11}}{(1)^{2} \times 1 \times 10^{11}}$$

$$F_{s} \uparrow \qquad \uparrow F_{B} \uparrow \qquad \downarrow L_{A} \downarrow L_{B} \uparrow \qquad \downarrow L_{A} \downarrow \qquad \downarrow L_{B} \uparrow \qquad \downarrow L_{B} \downarrow L_{B} \downarrow \qquad \downarrow L_{B} \downarrow \qquad \downarrow L_{B} \downarrow \qquad \downarrow L_{B} \downarrow L_{B} \downarrow \qquad \downarrow L_{B} \downarrow \downarrow L_{B} \downarrow L_{B} \downarrow \qquad \downarrow L_{B} \downarrow L_{B} \downarrow L_{B} \downarrow L_{B} \downarrow \downarrow L_{B} \downarrow L_{$$

Mass = d(AL) so acceleration = $g/2 = \frac{Force}{Mass}$

Now take a small element of length dx.

$$\sigma_x \longleftarrow \sigma_{x + dx}$$

Then we have $(\sigma_{x + dx} - \sigma_x) A = \rho A \cdot dx(g/2)$

$$\Rightarrow \frac{d\sigma}{dx}(\delta_{x}) = \frac{\rho g}{2} dx$$
$$\Rightarrow \int_{0}^{\sigma} d\sigma = \frac{\rho g}{2} \int_{0}^{x} x$$

$$\sigma = \frac{\rho gx}{2}$$
Now $\varepsilon(x) = \frac{\sigma(x)}{y} = \frac{\rho gx}{2y}$.
Thus $\varepsilon(L/2) = \frac{\rho gL}{4y}$
(b) $(dx) = \frac{\varphi gL}{\varphi}$
Acceleration = $\frac{(dALg - dALg/2)}{dAL}$
 $= g/2 \text{ m/s}^2$
 $\int_{\sigma_{x+dx}} \int_{\rho} A.dx.g = \frac{\rho g}{2} \text{ m/s}^2$
 $\int_{\sigma_{x+dx}} \sigma_x A + \rho Agdx = \rho Adx(g/2)$
 $\Rightarrow \left(\frac{\partial \sigma}{\partial x}\right) \cdot \delta x = \frac{-\rho g}{2} .\delta x$
 $\Rightarrow \int_{\frac{dLg}{2}}^{\sigma} d\sigma = -\frac{\rho g}{2} \int_{0}^{x} dx$
 $\Rightarrow \sigma = \frac{dLg}{2} - \frac{-dgx}{2}$
 $\sigma(x) = \frac{dg}{2} [L - x]$
So $\varepsilon(x) = \frac{\sigma(x)}{y} = \frac{dg}{2} [L - x]$
 $At x = 2L/3$
 $\varepsilon(x) = \frac{dg}{2y} \cdot [L - 2L/3] = \frac{dgL}{6y}$

Sol 3: Total heat supplied to the system = $100 \text{ cal/s} \times 240 \text{ sec}$

- = 24 × 1000
- = 24000 cal

Heat to change temperature from – 20°C to 0°C

- $= 100 \times 0.2 \times (0 (-20)] + 200 \times 0.5 \times (0 + 20)$
- = 400 + 2000 = 2400 cal

$$\Rightarrow$$
 24000 - 2400

= 21600 cal are left

Heat used to change the state of all ice

= 80 × 200

- = 16000 cal
- \Rightarrow Heat left = 21600 16000

= 5600 cal

So this much each is used to heat the water produced and the container:

 $5600 = 100 \times 0.2 \times (T - 0) + 200 \times 1 \times (T - 0)$ 5600 = 20 T + 200T

5600

 $\Rightarrow T = \frac{5600}{220} = 25.45^{\circ}C$

Note: This approach is to be used as we don't know the final state of water.

Sol 4: Mass of drink = 0.833 × 120 = 100 gm

So 50 gm alcohol + 50 gm of water. Let the temperature be T, then

$$m_{i}L_{f} + m_{i}S_{w} (T - 0) = m_{w} S_{w} (25 - T) + m_{A}S_{A}$$
.(25 - T)

⇒ 20 × 80 + 20 × 1 × T = 50 × 1 × (25 - T) + 50
× 0.6 × (25 - T)

⇒ 1600 + 20 T = 80 × (25 - T)

⇒ 100 T = 80 × 25 - 1600

ΔT = 20 - 16 = 4°C

Sol 5: Let the mass be m, the heat loss rate = R in J/min.

Then m.S_e . $\frac{dT}{dt} = R$ $\Rightarrow mS_2.(3) = R$ And also m . L_f = 30 R. $\Rightarrow m . L_f = 30 \times m S_L . (3)$ $\Rightarrow \frac{1}{90} = \frac{S_2}{L_f} \Rightarrow 1:90$

Sol 6:
$$y_{com} = \frac{y_{BC}m_{BC} + y_{AB}.m_{AB} + y_{AC}.m_{AC}}{m_{BC} + m_{AB} + m_{AC}}$$

$$= \frac{m.(0) + \frac{\sqrt{3a}}{4}.m + \frac{\sqrt{3a}}{4}m}{3m}$$

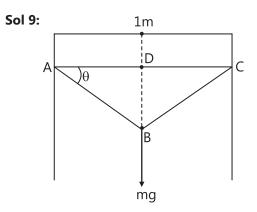
$$y_{com} = \frac{a}{2\sqrt{3}}$$
Now $\frac{dy_{com}}{dT} = \frac{1}{2\sqrt{3}} \times \frac{da}{dT} = \frac{1}{2\sqrt{3}} \times a_0 \cdot \alpha$
As $= a_0(1 + \alpha(T - T_1)) = \frac{a_0 \cdot 4\sqrt{3} \times 10^{-6}}{2\sqrt{3}}$
 $= 4 \times 10^{-6} \text{ m/°C}$

$$\frac{da}{dT} = a_0 \alpha$$

Sol 8: da = $a_0 \cdot \alpha \Delta T \Rightarrow 0.05 = 25 \cdot \alpha_A \cdot 100$ $\Rightarrow \alpha_A = 0.2 \times 10^{-4} = 2 \times 10^{-5}/{}^{\circ}C$ Similarly 0.04 = 40 $\cdot \alpha_B \cdot 100$

$$\Rightarrow 10^{-5} / {}^{\circ}C = \alpha_{B}$$
Now
$$x \qquad 50 - x$$
B

Now, $0.03 = x \cdot \alpha_A \cdot (\Delta T) + (50 - x)\alpha_B \cdot \Delta T$ $0.03 = x \times 2 \times 10^{-5} \times 50 + (50 - x) \cdot 10^{-5} \times 50$ $0.03 = 100x \times 10^{-5} - 50x \times 10^{-5} + 2500 \times 10^{-5}$ $0.03 = 50x \times 10^{-5} + 0.025$ $\Rightarrow 0.005 = 50x \times 10^{-5}$ $\Rightarrow x = 10 \text{ cm}$ So $L_A = 10 \text{ cm}, L_B = 50 - 10 = 40 \text{ cm}$



We have $2T \cos (90^\circ - \theta) = mg$ $\Rightarrow 2T \sin \theta = mg$ $\Rightarrow 2T \theta \approx mg [\theta \text{ is small}]$ - mg

$$\Rightarrow T = \frac{mg}{2\theta} \qquad ...(i)$$

Now strain =
$$\frac{AB + BC - AC}{AC} = \frac{2.AB - 2AD}{2AD}$$

= $\frac{AB - AD}{AD} = \frac{\sqrt{AD^2 + BD^2} - AD}{AD}$
= $\frac{AD\left[1 + \left(\frac{BD}{AD}\right)^2 \frac{1}{2}\right] - AD}{AD}$
= $\frac{1}{2} \cdot \left(\frac{BD}{AD}\right)^2$, Now as BD = AD tan θ .
Strain = $\frac{1}{2} \cdot \tan^2 \theta \approx \frac{\theta^2}{2}$ [for small θ]
Now, Stress = Y × Strain
 $\Rightarrow \frac{T}{A} = Y \times \frac{\theta^2}{2}$
 $\Rightarrow \frac{mg}{2A\theta} = \frac{Y \times \theta^2}{2}$
 $\Rightarrow \frac{mg}{AY} = \theta^3 \Rightarrow \theta = 3\sqrt{\frac{mg}{AY}}$
= $3\sqrt{\frac{1 \times 10}{4 \times 10^{-4} \times 2 \times 10^{11}}}$
= $3\sqrt{\frac{1}{8 \times 10^6}} = \frac{1}{200}$ rad

Sol 10: Let the mass of ice = m and water = 200 - m So 30 gm (330 - 300) steam is introduced in the system. Latent heat of condensation for water = $\frac{2250}{4.2}$ cal/gm K.

= 535.71 cal/gm k.

Now, heat lost = $535.71 \times 30 + 30 \times 1 \times (100 - 50)$

= 17571.3 cal

So heat gained by The mixture = $0.1 \times 100 \times (50 - 0) + m \times 80 + 200 \times 1 (50 - 0) = 500 + 10000 + 80 m$

⇒17571.3 = 10500 + 80 m

 \Rightarrow M_{ice} = 88.4 gm

So $m_{water} = 200 - 88.4 = 111.6 \text{ gm}$ So ratio = 88.4 : 111.6 = 1 : 1.26

Sol 11: Heat required to fully melt the ice :

 $2 \times 50 \times 0.5 \times (15) + 2 \times 50 \times 80$ = 750 + 8000 = 8750 cal Heat required to convert the water at 0°C

= 250 × 25 = 6250 cal

So the whole water will be converted at 0°C

Now 6250 - 750 = 5500 cal energy is coming from melting of ice

$$\Rightarrow 5500 = mL \Rightarrow m_i = \frac{5500}{80} = 68.75 \text{ gm}$$

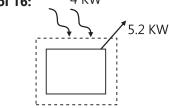
So ice melted = 68.75 gm
Ice remained = 100 - 68.75

= 31.25 gm

And water = 250 gm + 68.75 gm = 318.75 gm

Sol 14: Let the mass = m. So $100 \times 1 \times (90 - 24)$ =mL + m . 1 × (100 - 90) $100 \times 66 = 540 \text{ m} + 10 \text{ m}.$ $\Rightarrow \text{m} = \frac{6600}{550} = 12 \text{ gm}.$

Sol 15: (i) Now, from graph, 800 cal produces 80°C temperature diff. $\Rightarrow m \cdot S \times \Delta T = E$ $\Rightarrow m \times 0.5 \times 1 \text{ cal / gm °C} \times 80 = 800$ $\Rightarrow m = 20 \text{ gm} = 0.02 \text{ Kg}$ (ii) Heat supplied = 1600 - 800 = 800 cal $\Rightarrow 800 = mL_f = L_f = 40 \text{ cal/gm} = 40,000 \text{ cal/kg}.$ (iii) m $\cdot S_{\ell} \cdot \Delta T = E$ $\Rightarrow 0.02 \times S (120 - 80) = (2200 - 1600)$ $0.02 \times S \times 40 = \frac{600}{40}$ $S = \frac{600}{40 \times 0.02} = \frac{15 \times 100}{0.02} = 750 \text{ cal /kg °C}$ Sol 16: 4 KW



Heat stored in system = 4 + 1.7 - 5.2 = 0.5 kW

Now power P = $C_p \cdot \frac{dT}{dt}$ $\Rightarrow 0.5 \times 10^3 = C_p \cdot 0.5$ \Rightarrow C_p = 10³ J/°C = 1000 J/K. **Sol 17:** 70 litre = 70,000 cm³ = 70,000 gm = 70 kg. of water Now heat required per minute $= m \times S_w \cdot (\Delta T)$ $= 70 \times 1000 \text{ cal/kg}^{\circ}\text{C} \times (90 - 10)$ = 70 × 1000 × 80 = 56 × 10⁵ cal/min Now, $0.32x = 56 \times 10^5$ \Rightarrow x = 56 × 10⁵/0.32 = 1.75 × 10⁷ cal/min So mH = 1.75×10^{7} . \Rightarrow m = $\frac{1.75 \times 10^7}{8400 \times 10^3} = \frac{1.75}{0.84} = 2.08$ kg/min So for 1 hour = 2.08 kg × 60 = 125 kg/hour. So volume = $\frac{Mass}{Density} = \frac{125 \text{ kg/ hour}}{1.2 \text{ kg/ m}^3}$ $= 104.16 \times m^3$ / hour Sol 18: L 2L $L_T = L_A + L_B$ $\Rightarrow \frac{dL_{T}}{dT} = \frac{dL_{A}}{dT} + \frac{dL_{B}}{dT}$ $= \alpha . L + (2\alpha) . (2L) = 5\alpha\lambda.$ Now $\frac{1}{L_{T}} \cdot \frac{dL_{T}}{dT} = \frac{5\alpha L}{3L} = \frac{5\alpha}{3}$ $\Rightarrow \alpha_{T} = \frac{5\alpha}{3}$ **Sol 19:** T = $2\pi \sqrt{\frac{L}{a}}$ $\frac{dT}{T} = \frac{1}{2} \times \frac{dL}{L}$ [for small changes] [for quantity $A = a^m b^n$ $\frac{dA}{A} = m \cdot \frac{da}{a} + n \cdot \frac{db}{b}$]

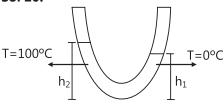
So
$$\frac{dL}{L} = (\alpha \cdot \Delta T) = 10^{-6} \cdot (10) = 10^{-5}$$

 $\Rightarrow \frac{dT}{T} = \frac{1}{2} \times 10^{-5}$
 $\Rightarrow dT = 0.5 \times \frac{1}{2} \times 10^{-5}$

[Time period is increasing, so cock has been slowed down]

So in 0.5 sec it loses
$$\Rightarrow 0.5 \times \frac{1}{2} \times 10^{-5}$$
 sec
In 10⁶ sec it loses $\Rightarrow \frac{0.5 \times \frac{1}{2} \times 10^{-5}}{0.5} \times 10^{6} = 5$ sec

Sol 20:



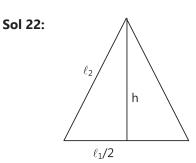
We have
$$\rho_1 g \cdot h_1 = \rho_2 \cdot g \cdot h_2$$

 $\rho_0 g h_1 = \frac{\rho_0 g \times h_2}{[1+10^5 (\Delta T)]}$
 $h_1 [1+10^{-3}] = h_2$
 $\Rightarrow h_2 = 100 + 0.1 = 100.1 \text{ cm}$
 $\Rightarrow \Delta h = 100.1 - 100 = 0.1 \text{ cm}.$

We have = $L_0 (1 + \alpha \Delta T) - L_0 = L_0 (\alpha \Delta T)$ And actual length = $L_0 (1 + \alpha \Delta T) = L$ So strain = $\frac{L_0 (\alpha \Delta T)}{L_0 (1 + \alpha \Delta T)} = \frac{\alpha \Delta T}{1 + \alpha \Delta T}$ \Rightarrow Stress = Y × Strain = $\frac{Y \alpha \Delta T}{1 + \alpha \Delta T}$ So compressions force = $\frac{A \times Y \alpha \Delta T}{1 + \alpha \Delta T} = \frac{Y A \alpha \Delta T}{1 + \alpha \Delta T}$

$$= \frac{10^{11} \times 10^{-5} \times 10^{-6} \times 100}{1 + 10^{-6} \times 100}$$

$$= \frac{10^4}{1+10^{-4}} = 10^4 \text{ N}.$$



Now using Pythagoras theorem

$$\ell_2^2 = h^2 + \frac{\ell_1^2}{4}$$

Now after increasing temp T,

$$\ell_{2}^{2} (1 + \alpha_{2}, \Delta T)^{2} = h^{2} + \frac{\ell_{1}^{2}}{4} (1 + \alpha_{1}, \Delta T)^{2}$$
$$h^{2} = \left(\ell_{2}^{2} - \frac{\ell_{1}^{2}}{4}\right) + 2 \cdot \left[\ell_{2}^{2} \cdot \alpha_{2} - \frac{\ell_{1}^{2}}{4} \cdot \alpha_{1}\right] \Delta T$$
$$+ \left[\ell_{2}^{2} \cdot \alpha_{2}^{2} - \frac{\ell_{1}^{2}}{4} \cdot \alpha_{1}^{2}\right] (\Delta T)^{2}$$

Now h^2 is independent of ΔT

So,
$$\ell_2^2 . \alpha_2 - \frac{\ell_1^2}{4} . \alpha_1 = 0$$
 [coeff. of ΔT]

[Now, as ($\Delta T)^2$ has coeff proportional to α^2 and hence negligible]

$$\Rightarrow \ell_2^2 \cdot \alpha_2 = \frac{\ell_2^2 \cdot \alpha_1}{4} \qquad \Rightarrow \boxed{\frac{\ell_1}{\ell_2} = 2\sqrt{\frac{\alpha_2}{\alpha_1}}}$$

Hence proved.

Sol 23: (i) Entire energy = Heat energy So power = m(0.1) $\times \frac{dT}{dt}$ = 180 \times 0.1 \times 0.5 = 9 cal/s= 9 \times 4.2 = 37.8 J/s = 37.8 watts (ii) We have P = $\tau \omega$ So 37.8 = $\tau \times \frac{180}{60} \times 2\pi$ $\Rightarrow \tau = \frac{37.8}{6\pi}$ = 2.005 Nm. Sol 24: h T = -20°C h T = θ° C

А

Now when both are mixed, 0°C will be the common temperature.

Now, Change in volume

= A.
$$(\Delta h) = \frac{m}{\rho_i} - \frac{m}{\rho_w} = \frac{m [\rho_w - \rho_i]}{\rho_i \cdot \rho_w}$$

Where m = Mass of ice melted,

$$\Rightarrow m = \frac{A(\Delta h)\rho_i\rho_w}{(\rho_w - \rho_i)}$$

So energy gained by this much ice

$$= mL = \frac{A(\Delta h)\rho_i \rho_w \times L}{(\rho_w - \rho_i)}$$

Conservation of energy \Rightarrow

Energy by ice to change temp. + Energy to melt = Energy to convert water temp to 0° C

$$\rho_{i} \cdot A \cdot h \cdot S_{i} \cdot (0 + 20) + \frac{A.(\Delta h).\rho_{i}.\rho_{w}.L}{(\rho_{v} - \rho_{i})}$$

$$= \rho_{w}A.h.S_{w}\theta$$

$$\Rightarrow \rho_{i}h.S_{i}.20 + \frac{\Delta h.\rho_{i}\rho_{w}.L}{(\rho_{v} - \rho_{i})} = \rho_{w}h.S_{w}\theta$$

$$\Rightarrow \theta = \frac{\rho_{i}.S_{i} \times 20}{\rho_{w} \times S_{w}} + \left(\frac{\Delta h}{h}\right)\frac{\rho_{i}}{(\rho_{w} - \rho_{i})} \cdot \frac{L}{S_{w}}$$

$$= 9 + 36 = 45^{\circ}C$$

Sol 25: Pressure at the bottom of A is same from both the sides.

$$p_{A}.g.h_{A} = p_{0}.g.h_{0} - p_{c}.g.h_{C} + p_{B}.g.h_{B}$$

$$p_{A}h_{A} = p_{0}.h_{0} - p_{C}h_{C} + p_{B}.h_{B} [p_{B} = p_{0} = p_{0}]$$

$$\frac{p_{0}}{[1 + \alpha.(95 - 5)]} \cdot h_{A} = p_{0}.h_{D} - \frac{p_{0}.h_{C}}{1 + \alpha(95 - 5)} + p_{0}.h_{B}$$

$$\frac{h_{A}}{(1 + 90\alpha)} = h_{0} - \frac{h_{C}}{(1 + 90\alpha)} + h_{B}$$

$$\Rightarrow \frac{(h_{A} + h_{C})}{(1 + 90\alpha)} = (h_{0} + h_{B})$$

$$\frac{52.8 + 49}{1 + 90\alpha} = (51 + 49)$$

$$\Rightarrow 1 + 90\alpha = \frac{52.8 + 49}{100}$$

$$1 + 90\alpha = \frac{101.8}{100} \Rightarrow 90\alpha = \frac{1.8}{100}$$

$$\Rightarrow \alpha = 0.2 \times 10^{-3}$$

$$= 2 \times 10^{-4}/^{\circ}C$$

Sol 26: Let the density at $0^{\circ}C = \rho_0$

Then density at 100°C = $\frac{\rho_0}{1 + \gamma.\Delta T}$

$$= \frac{\rho_0}{1+0.1} = \frac{\rho_0}{1.1}$$

Density at some temperature

$$T = \frac{\rho_0}{1 + \gamma . (T - 0)} = \frac{\rho_0}{(1 + \gamma T)}$$

And from heat transfer.

$$300 \rho_{o} S(T - 0) = \frac{110\rho_{o}}{1.1} S (100 - T)$$

$$300 T = 100 (100 - T)$$

$$\Rightarrow 400 T = 100 \times 100$$

$$\Rightarrow T = 25^{\circ}C$$

Now from the expansion and contraction we have

$$V = V_{0_1}(1 + \alpha \Delta T_1) + V_{0_2}(1 + \alpha \Delta T_2)$$

$$V = V_{0_1} + V_{0_2}$$

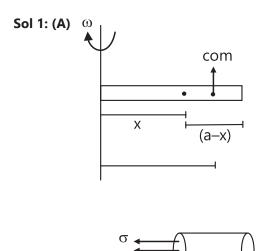
$$\Rightarrow V - V_0 = \Delta V = V_{0_1} \alpha \Delta T_1 + V_{0_2} \alpha \Delta T_2$$

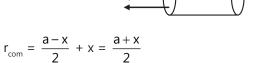
$$= 300 \times 0.001 \times 25 + 110 \times 0.001 \times (-75)$$

$$= -0.75 \text{ cm}^3$$
So the volume decreases by 0.75 cm³

Exercise 2

Single Correct Choice Type





Now $\sigma_x \times A = F$ required for centripetal force

So
$$\sigma_x \times A = \rho \cdot (a - x) \cdot \omega^2 \frac{(a + x)}{2}$$

 $\Rightarrow \sigma_x = \frac{\rho \cdot (a^2 - x^2)}{2A} \omega^2 \Rightarrow \text{Quadratic}$

Sol 2: (C) Stress = y × Strain $\Rightarrow \frac{F}{A} = y \times \frac{\Delta \ell}{\ell} \Rightarrow \frac{F}{\Delta \ell} = \text{Slope} = \frac{Ay}{\ell}$

Sol 3: (D) Heat = $mL_1 + (m_w + m_c) \cdot C_w \cdot \Delta T + mL_v$ = $10 \times 80 + (10 + 10) \times 1 \times 100 + 10 \times 540$ = 800 + 5400 + 2000 = 8200 cal

Sol 4: (A)
$$\Delta H = mL.$$

$$\Rightarrow \frac{dH}{dt} = \frac{dm}{dt} \times L = 80 \times 0.1 \text{ gm/sec}$$

$$= 8 \text{ cal/sec}$$
So total heat supplied = 800 cal (8 × 100 sec)
So 800 cal = m × L \Rightarrow m = 10 gm
So $\frac{dH}{dt} = mS\frac{dT}{dt} = 10 \times 1 \text{ cal/gm } K^{-1} \times \frac{dT}{dt} = 8$

$$\Rightarrow \frac{dT}{dt} = 0.8 \text{ °C/sec}$$

Sol 5: (A) Let the heat capacity of the flask be m

Then L = Latent heat of fusion
Then

$$50 L + 50(40 - 0) =$$

 $200 \times (70 - 40) + (70 - 40) \times m$
 $\Rightarrow 50 L + 2000 = 6000 + 30 m$
 $\Rightarrow 5L = 3m + 400$ (i)
And
 $80L + 80 (10 - 0) = 250 \times (40 - 10) + m (30)$
 $\Rightarrow 80L + 800 = 7500 + 30 M$
 $\Rightarrow 8L = 3M + 670$
 $\Rightarrow 8L = 5L - 400 + 670$
 $\Rightarrow L = 90 cal/gm$
 $\Rightarrow 90 \times 4.2 \times 10^{3} J/kg = 3.8 \times 10^{5} J/Kg$

Sol 6: (D) Slope = $\frac{\Delta T}{H} \Rightarrow$ Increase of heat capacity

Sol 7: (A) Assuming all potential energy is converted to heat energy

mgh =
$$\frac{mL}{5}$$
 \Rightarrow h = L/5g

Sol 8: (C) Vap. \Rightarrow between 20 – 30 min

 \Rightarrow Heat supp = (30 – 20) × 42 KJ = 420 kJ ⇒ mL = 420 \Rightarrow L = 84

Sol 9: (D) 8 volumes of A = 12 volume of B \Rightarrow 2 volumes of A = 3 volumes of B So, suppose the volume V, Then $C_{2V} = C_{3V}$ Thus, ρ_A . (2V). $S_A = \rho_B$. (3V). S_B \Rightarrow 1500 × 2 S_A = 3 × 2000 × S_B \Rightarrow S_A/S_B = 2/1

Sol 12: (B) We have,
$$\frac{\Delta L}{L} = \alpha \Delta T = 0.01$$

So $\frac{dA}{A} = 2\alpha \Delta T = 0.02$

Sol 13: (A) Let the length be = L Now L $(1 + 2 \times 10^{-6} \times 40)$ $= 100 \text{ mm.} (1 + 12 \times 10^{-6} \times 40)$ L is Length at 40°C

$$\Rightarrow L = 100 \times \frac{(1+12 \times 10^{-6} \times 40)}{(1+2 \times 10^{-6} \times 40)}$$

⇒L > 100 mm

Sol 14: (C)
$$B_{ABCD} = B_{EFGH} = \alpha_x + \alpha_y$$

= 3 × 10⁻⁵
(A) and (B) are incorrect.
Also $B_{BCGH} = \alpha_y + \alpha_z = (2 + 3) \times 10^{-5}$
= 5 × 10⁻⁵ \Rightarrow (B) incorrect.
(C) $\Rightarrow \alpha_x + \alpha_y = (2 + 1) \times 10^{-5} = 3 \times 10^{-5}$
(C) is correct.

Sol 15: (C) We have,
$$x - \gamma_c = C$$

And $x - \gamma_s = S$

$$\Rightarrow C + \gamma_{c} - \gamma_{s} = S$$
$$\Rightarrow \gamma_{s} = (C + \gamma_{c} - S)$$
$$\Rightarrow \alpha_{s} = \frac{(C + \gamma_{c} - S)}{3}; (C)$$

Sol 16: (A) Volume of sphere

$$= \frac{4\pi}{3} \times R^{3} = \frac{4}{3} \times \frac{22}{3} \times \left(\frac{7}{2}\right)^{3} = 179.66(m^{3})$$

So density of sphere = 1.4833

Now, the density of sphere = Density of water (for just scenting)

$$\Rightarrow 1.4833 \text{ gm/cm}^{3} = \frac{1.527}{1 + \gamma.\Delta T} = \frac{1.527}{1 + 35\gamma}$$
$$\Rightarrow \gamma = 8.486 \times 10^{-4}$$

Sol 17: (B) Change in volume of Mercury = $V_0 \gamma_m$.T Change in volume of bulb = $V_0 3\alpha_0 T$ So excess volume of mercury = $V_0(\gamma_m - 3\alpha_q)T$ And new area of glass = $A_0 (1 + 2\alpha_g T)$

$$\Rightarrow \text{Length} = \frac{V_0.(\gamma_m - 3\alpha_g)T}{A_0(1 + 2\alpha_g T)}$$

Sol 18: (C) $3\alpha_{\rm B} = 10^{-3} \,{}^{\circ}{\rm C}^{-1}$ and $3\alpha_{\rm C} = 3 \times 10^{-3} \,{}^{\circ}{\rm C}^{-1}$ So when heated, the ratio of volumes increases by benzene = $3\alpha_{p}$. $\Delta T = 10^{-2}$ (Cylindrical vessel = 3×10^{-2}) so new vol : Benzene = $10^{-2} V_0 + V_0$ (Cylindrical vessel) = $(1 + 3 \times 10^{-2})v_0$ Change in volume = $2 \times 10^{-2} V_0$.

So the height will decrease as the volume of cylindrical vessel would be more.

Sol 19: (B) We have $\Delta L = L\alpha \Delta T$ \Rightarrow 0.075 = 20 × α_A × 100 $3.75 \times 10^{-5} = \alpha_{A}$ And $0.045 = 20 \times \alpha_{_{\rm B}} \times 100$ \Rightarrow 2.25 × 10⁻⁵ = $\alpha_{\rm B}$ Now, let the length of A part be x com.

Н

so $\Delta L = x \cdot \alpha_{A} \cdot \Delta T + (20 - x) \alpha_{B} \cdot \Delta T$ $0.06 = 20 \alpha_{B} \cdot \Delta T + x \cdot \Delta T (\alpha_{A} - \alpha_{B})$ $0.06 = 0.045 + x \times 100 \cdot [1.5 \times 10^{-5}]$ $\Rightarrow 0.015 = x \times 1.5 - 10^{-3}$ \Rightarrow x = 10 cm

Sol 20: (D) Now the volume of air is same $\Rightarrow \Delta V =$ Same (independent of ΔT) change in vol. of mercury - change in vol of glass = 0 $\Rightarrow \gamma_{m}.V_{m}.\Delta T - \gamma_{q}.V_{q}.\Delta T = 0$ $\Rightarrow \boxed{\gamma_m.V_m = \gamma_g.V_g}$ \Rightarrow 1.8 \times 10⁻⁴ \times 300 = x \times 9 \times 10⁻⁶ \Rightarrow x = 20 × 300 = 6000 cm³

Sol 21: (C) We have

$$\rho_{1}gh_{1} = \rho_{2}gh_{2} \quad [\text{pressure is same}]$$

$$\Rightarrow \rho_{0} \times g \times 120 = \frac{124 \times g \times \rho_{0}}{(1 + \gamma.\Delta T)}$$

$$\Rightarrow (1 + \gamma.\Delta T) = \frac{124}{120}$$

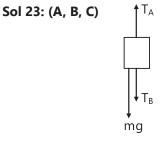
$$\Rightarrow \gamma.\Delta T = \Rightarrow \gamma = \frac{1}{900}$$

Multiple Correct Choice Type

Sol 22: (A, C) Steel (E) Copper (2E) 25 cm 50 cm Stress in steel = $\frac{F}{2A}$, stress in copper = $\frac{F}{A}$ Strain in steel = $\frac{F}{2AE}$, strain in copper = $\frac{F}{AE}$

Extension =
$$\frac{L_0.F}{2AE}$$
, extension in copper = $\frac{2L_0.F}{AE}$

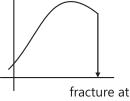
F



Now $T_{B} = F = mg/3$

And
$$T_A = mg + T_B = \frac{4mg}{3}$$

Now, if $r_{_A} = r_{_B}$ then as $T_{_B} < T_{_A}$, the $\sigma_{_A} > \sigma_{_B}$ and hence A will break.



more σ

If
$$r_A > 2r_B \Rightarrow \sigma_A > \sigma_B \Rightarrow (B)$$

If $r_A = 2r_B$

New length

=
$$L_0 (1 + \alpha \Delta T)$$
 and change in length = ΔL
= $L_0 \alpha \Delta T$
So strain in each rod = $\left(\frac{\alpha \Delta T}{1 + \alpha \Delta T}\right)$
 \Rightarrow Stress = $E\left(\frac{\alpha \Delta T}{1 + \alpha \Delta T}\right)$
And Force = $\frac{A.E.(\alpha \Delta T)}{(1 + \alpha \Delta T)}$
So, (B) Energy
= $\frac{1}{2} \times$ Stress \times strain \times Volume.
Same for all $A \times \ell$
Same

for all

So Energy α area \Rightarrow (C)

Sol 25: (A, C, D) (A) Stress = $\frac{Mg}{A}$, strain = $\frac{\ell}{L}$ So energy stored = $\frac{1}{2} \times \frac{mg}{A} \times \frac{\ell}{2} \times AL = \frac{mg\ell}{2}$

Sol 26: (D) No kinetics involved

Sol 27: (A, C, D)
$$\beta = 2\alpha \Rightarrow (A)$$

(C) $\Rightarrow \beta = 3\alpha \Rightarrow (C)$
0.002 = $\alpha \Delta T = \alpha \times 80$
 $\Rightarrow \alpha = \frac{2}{8} \times 10^{-4} \Rightarrow 0.25 \times 10^{-4}$

$$\begin{split} &\textbf{Sol 28: (B)} ~(\rho_\ell)(V/2) \times g = (\rho_s) \times V \times g \\ \Rightarrow \rho_\ell ~= 2 \, \rho_s \,. \end{split}$$

Sol 29: (D) Let the fraction be f, ΔT = Change in temp

So
$$\frac{\rho_L}{(1+\gamma_L\Delta T)}$$
 . (f.v) × g = $\frac{\rho_s}{(1+\gamma_S\Delta T)}$ v × g
 \Rightarrow f = $\frac{\rho_s}{\rho_L}$. $\frac{(1+\gamma_L\Delta T)}{(1+\gamma_S\Delta T)}$
f = $\frac{1}{2}$ × $\frac{(1+r_L\Delta T)}{(1+r_S\Delta T)}$

Now the f depends on whether

 $\gamma_{\rm L} > \gamma_{\rm s} \text{ or } \gamma_{\rm s} > \gamma_{\rm L}$

Sol 30: (A) We have

$$\begin{split} & \frac{1 + \gamma_L T}{1 + \gamma_S T} = 1 \text{ for all T.} \\ & \Rightarrow \gamma_L = \gamma_S \Rightarrow \gamma_L = 3\alpha_s. \end{split}$$

Sol 31: (A) We have

$$\frac{\rho_{\ell}}{(1+\gamma_{L}.\Delta T)} \cdot A_{0} (1 + 2\alpha_{s}\Delta T) \cdot h.g = \rho_{\ell}.A_{0}.h \times g$$
$$\Rightarrow 1 + 2\alpha_{s}\Delta T = 1 + \gamma_{L}\Delta T$$
$$\Rightarrow \boxed{\gamma_{L} = 2\alpha_{s}}$$

Sol 32: (A) Correct explanation.

Sol 33: (A) Refer theory.

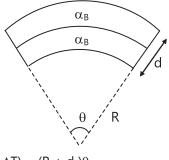
Sol 34: (A) Statement-I may be true statement-II is true. But statement-I is only possible when $\beta \omega > B_{container}$ Sol 35: (B) Factual

Sol 36: (B) L_f = 80 cal/gm = 80 × 4.2 × 10³ = 8 × 4.2 × 10⁴ J/kg = 336000

Sol 37: (D) for mass > 1 kg We have thermal capacity = m.S. \Rightarrow Thermal cap > S

Previous Years' Questions

Sol 1: (B, D) Let ℓ_0 be the initial length of each strip before heating. Length after heating will be



$$\ell_{\rm B} = \ell_0 (1 + \alpha_{\rm B} \Delta T) = (R + d) \theta$$

and
$$\ell_c = \ell_0(1 + \alpha_c \Delta T) = R\theta$$

$$\therefore \qquad \frac{R+d}{R} = \left(\frac{1+\alpha_{B}\Delta T}{1+\alpha_{C}\Delta T}\right)$$
$$\therefore \qquad 1 + \frac{d}{R} = 1 + (\alpha_{B} - \alpha_{c}) \Delta T$$

[From binomial expansion]

$$\therefore \quad R = \frac{d}{(\alpha_{B} - \alpha_{C})\Delta T}$$
or
$$R \propto \frac{1}{\Delta T} \propto \frac{1}{|\alpha_{B} - \alpha_{C}|}$$

Sol 2: Heat liberated when 300 g water 25°C goes to water at 0°C : Q = ms $\Delta\theta$ = (300) (1) (25) = 7500 call

From Q = mL, this much heat can melt mass of ice given by

$$m = \frac{Q}{L} = \frac{7500}{80} = 93.75 \text{ g}$$

i.e., whole ice will not melt.

Hence, the mixture will be at 0°C

Mass of water in mixture

= 300 + 93.75 = 393.75 g and

Mass of ice in mixture

= 100 – 93.75 = 6.25 g

Sol 3: Heat lost in time t = Pt = ML

$$\therefore$$
 L = $\frac{Pt}{M}$

Sol 4: $C_p = C_v + R \therefore C_p > C_v$

Sol 5: Let m be the mass of the steam required to raise the temperature of 100 g of water from 24°C to 90°C.

Heat lost by steam = Heat gained by

Water : $m (L + s\Delta\theta_1) = 100s\Delta\theta_2$ or $m = \frac{(100)(s)(\Delta\theta_2)}{L + s(\Delta\theta_1)}$

Here, s =Specific heat of water= 1 cal/g-°C,

L=Latent heat of vaporization = 540 cal/kg.

$$\Delta \theta_1 = (100 - 90) = 10^{\circ} \text{C}$$

and $\Delta \theta_2 = (90 - 24) = 66^{\circ}C$

Substituting the values, we have

$$m = \frac{(100)(1)(66)}{(540) + (1)(10)} = 12 g$$

$$\therefore m = 12 g$$

Sol 6: When the temperature is increased, volume of the cube will increase while density of liquid will decrease. The depth upto which the cube is submerged in the liquid remains the same.

Upthrust = Weight. Therefore, upthrust should not change

F = F'

 $\therefore V_i \rho_1 g = V'_i \rho'_1 g$ (V_i=volume immersed)

$$\therefore$$
 (Ah_i) (ρ_i) (g)

 $= A(1 + 2\alpha_{s}\Delta T) (h_{i}) \left(\frac{\rho_{L}}{1 + \gamma_{1}\Delta T}\right)g$

Solving this equation, we get $\gamma_1 = 2\alpha_s$

Sol 7: 0.05 kg steam at 373 K

 $\xrightarrow{Q_1}$ 0.05 kg water at 373 K

0.05 kg water at 373 K

 $\xrightarrow{Q_2}$ 0.05 kg water at 273 K

0.45 kg ice at 253 K $\xrightarrow{Q_3}$ 0.45 kg ice at 273 K 0.45 kg ice at 273 K $\xrightarrow{Q_4}$ 0.45 kg water at 273 K $Q_1 = (50) (540) = 27,000$ $Q_2 = (50) (1) (100) = 5000$ $Q_3 = (450) (0.5) (20) = 4500$ $Q_4 = (450 (80) = 36000$

Now since $Q_1 + Q_2 > Q_3$ but $Q_1 + Q_2 < Q_3 + Q_4$ ice will come to 273 K from 253 K, but whole ice will not melt. Therefore, temperature of the mixture is 273K.

Sol 8: Language of question is slightly wrong. As heat capacity and specific heat are two different physical quantities. Unit of heat capacity is $J-kg^{-1}$ not $J-kg^{-1} \circ C^{-1}$. The heat capacity given in the question is really the specific heat. Now applying the heat exchange equation.

 $420 = (m \times 10^{-3}) (2100) (5) + (1 \times 10^{-3}) (3.36 \times 10^{5})$

Solving this equation we get, m = 8g

 \therefore The correct answer is 8.

$$\frac{dm_{ice}}{dt} = \frac{dm_{vapour}}{dt}$$
$$\frac{400kS}{\lambda x L_{ice}} = \frac{300kS}{(100 - \lambda)x L_{vapour}}$$
$$\lambda = 9$$

Sol 10: (3) Change in length $\Delta L = \frac{MgL}{YA} = L \propto \Delta T$ $\therefore m \approx 3kg$

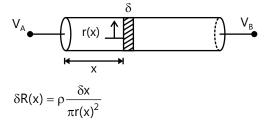
Sol 11: (A) Rate of radiation energy lost by the sphere

= Rate of radiation energy incident on it

$$\Rightarrow \sigma \times 4\pi r^2 \left[T^4 - (300)^4 \right] = 912 \times \pi r^2$$
$$\Rightarrow T = \sqrt{11} \times 10^2 \approx 330 K$$

Sol 12: (A, D) If the temperature distribution was uniform (assuming a uniform cross section for the filament initially) the rate of evaporation from the

surface would be same everywhere. But because the filaments break at random locations; it follows that the cross-sections of various filaments are non-uniform.



The temperature of points A and B are decided by ambient temperature are identical. Then the average heat flow through the section S is O. After sufficiently long time, this condition implies that the temperature across the filament will be uniform. If the instantaneous current is i(t) through the filament then by conservation of energy :

$$\frac{(V_B - V_A)^2}{R(t)^2} \times \frac{dx}{\kappa \pi r(x)^2} = e\sigma 2\pi r 9x).\delta(x)T^4 + \rho \pi r(x)^2.dxL_v$$

in above κ = Material conductivity

R(t) = Resistance of whole filament as a function of time

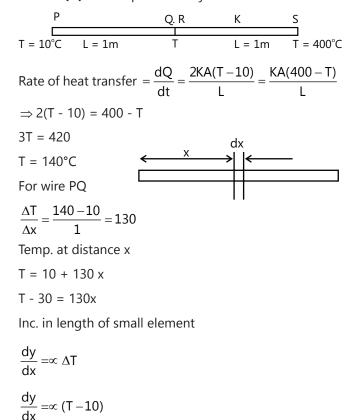
 ρ = Material density

 $\rm L_{v}$ = Latent heat of vapourisation for the material at temperature T

Since R(t) increases with time

$$P(t) = \frac{(V_B - V_A)^2}{R(t)} decreases$$

Sol 13: (A) Let temperature of junction = T



$$\frac{dy}{dx} = \infty (130x)$$

$$\int_0^{\Delta L} dy = 130 \propto \int_0^L x \, dx$$

$$\Delta L = \frac{130 \propto x^2}{2}$$

$$\Delta L = \frac{130 \times 1.2 \times 10^{-5} \times 1}{2}$$

$$\Delta L = 78 \times 10^{-5} \text{ m} = 0.78 \text{ mm}$$