2. Number of nuclei decayed after time $t = N_0 - N$ = $N_0 - N_0 e^{-\lambda t} = N_0 (1 - e^{-\lambda t})$

The corresponding graph is as shown in Fig. 25.13.

3. Probability of a nucleus for survival of time t,

$$P(\text{survival}) = \frac{N}{N_0} = \frac{N_0 e^{-\lambda t}}{N_0} = e^{-\lambda t}$$

The corresponding graph is shown in Fig. 25.14.

- 4. Probability of a nucleus to disintegrate in time t is, P(disintergration) = $1 - P(survival) = 1 - e^{-\lambda t}$ The corresponding graph is as shown.
- 5. Half-life and mean life are related to each other by the relation, $t_{1/2} = 0.693 t_{av}$ or $t_{av} = 1.44 t_{1/2}$
- 6. As we said in point number (2), number of nuclei decayed in time t are $N_0(1 - e^{-\lambda t})$. This expression involves power of e. So to avoid it we can use, $\Delta N = \lambda N \Delta t$ where, ΔN are the number of nuclei decayed in time Δt , at the instant when total number of nuclei are N. But this can be applied only when $\Delta t \ll t_{1/2}$.
- 7. In same interval of time, equal percentage (or fraction) of nuclei are decayed (or left un decayed).

$$1.R = R_0 A^{1/3}$$
 $2. \Delta E_{be} = \sum (mc^2) - Mc^2$ (binding energy) $3. \Delta E_{ben} = \frac{\Delta E_{be}}{A}$ (binding energy per nucleon.) $4. \frac{dN}{N} = -\lambda dt$ $5. N = N_0 e^{-\lambda t}$ (radioactive delay), $6. \tau = \frac{1}{\lambda}$ $7. T_{1/2} = \frac{\ln 2}{\lambda} = \tau \ln 2.$

Solved Examples

JEE Main/Boards

Example 1: Sun radiates energy in all direction. The average energy received at earth is 1.4 kW/m^2 . The average distance between the earth and the sun is $1.5 \times 10^{11} \text{ m}$. If this energy is released by conversion of mass into energy, then the mass lost per day by sun is approximately (use 1 day = 86400 sec)

Sol: The sun produces energy by fusion reaction of hydrogen atoms. The loss in mass of sun is calculated

using $\Delta m = \frac{\Delta E}{c^2}$ where ΔE is the amount of energy released during the day.

The sun radiates energy in all directions in a sphere. At a distance R, the energy received per unit area per second is 1.4 KJ (given). Therefore the energy released in area $4\pi R^2$ per sec is $1400 \times 4\pi R^2$ J the energy released per day = $1400 \times 4\pi R^2 \times 86400$ J

Where
$$R = 1.5 \times 10^{11} m$$
, thus

$$\Delta E = 1400 \times 4 \times 3.14 \times (1.5 \times 10^{11})^2 \times 86400$$





P (Disintegration)

1



The equivalent mass is $\Delta m = \Delta E / C^2$

$$\Delta m = \frac{1400 \times 4 \times 3.14 \times (1.5 \times 10^{11})^2 \times 86400}{9 \times 10^{16}}$$
$$\Delta m = 3.8 \times 10^{14} \text{ kg}$$

Example 2: The energy released per fission of uranium (U²³⁵) is about 200 MeV. A reactor using U²³⁵ as fuel is producing 1000 kilowatts power. The number of U²³⁵ nuclei undergoing fission per sec is, approximately

Sol: The number of Uranium nuclei undergoing fission is obtained by

 $N = \frac{\text{Energy produced}}{\text{Energy realesed during one fission}}.$

The energy produced per second is

$$= 1000 \times 10^{3} \text{ J} = \frac{10^{6}}{1.6 \times 10^{-19}} \text{ eV} = 6.25 \times 10^{24} \text{ eV}$$

The number of fissions should be,

$$N = \frac{6.25 \times 10^{24}}{200 \times 10^6} = 3.125 \times 10^{16}$$

Example 3: A star initially has 10⁴⁰ deuterons. It produces energy via the processes ${}_{1}^{2}H + {}_{1}^{2}H \rightarrow {}_{1}^{3}H + {}_{1}^{1}p$ and ${}_{1}^{2}H + {}_{1}^{3}H \rightarrow {}_{2}^{4}He + {}_{0}^{1}n$. If the average power radiated by the star is 10^{16} W, in how much time the deuteron supply of the star get exhausted?

Sol: The star produces the energy by fusing deuterium and tritium into the helium, and releasing proton and neutron. Thus the mass defect is easily obtained per one such conversion. The time in which the deuterium supply is exhausted is found by

 $t = \frac{\text{Number of deutrons present in star}}{\text{number of deutrons used per sec}}$

Here number of deuterons used per second

 $n = \frac{N \times Power}{energy released per reaction}$

where N is the deuteron used per reaction.

Adding the two processes, we get

 $3 {}_{1}^{2}H \rightarrow {}_{2}^{4}He + {}_{1}^{1}p + {}_{0}^{1}n$

Mass defect = $3 \times 2.014 - 4.001 - 1.007 - 1.008$

Power of the star $= 10^{16} \text{ W} = 10^{16} \text{ J} / \text{ s}$

Number of deuterons used in one second

$$=\frac{10^{16}}{0.026\times931\times10^{6}\times1.6\times10^{-19}}\times3=7.75\times10^{27}$$

Now the time in which the deuterons supply exhausted

$$t = \frac{\text{Number of deutrons present in star}}{\text{number of deutrons used per sec}}$$
$$= \frac{10^{40}}{7.75 \times 10^{27}} = 1.3 \times 10^{12} \text{ sec}$$

Example 4: The mean lives of a radioactive material for α and β radiations are 1620 years and 520 years respectively. The material decays simultaneously for α and β radiation. The time after which one fourth of the material remains un-decayed is

Sol: The mean life of the radioactive material for simultaneous α and β decay is $\ \tau = \frac{\tau_{\alpha} \ \tau_{\beta}}{\tau_{\alpha} + \tau_{\beta}}$. The time in which the 3/4th of material decayed is $t = \frac{2.303}{\lambda} \log_{10} 4$. We know that $\lambda \propto \frac{1}{\tau}$. $\tau = \frac{\tau_{\alpha} \tau_{\beta}}{\tau_{\alpha} + \tau_{\beta}} = \frac{1620 \times 520}{1620 + 520} = 394 \text{ years}$

time of decay $t = \tau \times 2.303 \log_{10} \frac{N_0}{N_1}$

 $t = 394 \times 2.303 \log_{10}(4) = 394 \times 2.303 \times 0.602$

t = 546 years

Example 5: A sample contains two substances P and Q, each of mass 10^{-2} kg. The ratio of their atomic weights is 1:2 and their half-lives are 4 s and 8 s respectively. The masses of P and Q that remain after 16s will respectively be-

Sol: The mass of radioactive element decaying after time t is given by $N = \frac{N_0}{2^n}$; $M = \frac{M_0}{2^n}$ where M is the mass (in kg) of the radioactive element. As half-lives are given, value of n is found as, number of half-life

n =
$$\frac{t}{t_{1/2}}$$
.
 $\therefore N = \frac{N_0}{2^n}; M = \frac{M_0}{2^n}; \text{ for } P, n = \frac{16}{4} = 4$
 $\therefore M_P = \frac{10^{-2}}{16} = 6.25 \times 10^{-4} \text{Kg}$
for Q, n = $\frac{16}{8} = 2 \therefore M_Q = \frac{10^{-2}}{2^2} = 2.5 \times 10^{-3}$

Example 6: There is a stream of neutrons with a kinetic energy of 0.0327 eV. If the half-life of neutrons is 700 sec, what fraction of neutrons will decay before they travel 10 m? Given mass of neutron= 1.675×10^{-27} kg.

Sol: The fraction of neutrons decayed in the distance of 10 m is calculated by $\frac{\Delta N}{N} = \frac{0.693}{T_{1/2}} \Delta t$. Here $T_{1/2}$ is the half-life of the neutron and Δt is the time taken to cover distance of 10 m.

From the given kinetic energy of the neutrons we first calculate their velocity, thus

$$\frac{1}{2}mu^{2} = 0.0327 \times 1.6 \times 10^{-19}$$

$$\therefore u^{2} = \frac{2 \times 0.0327 \times 1.6 \times 10^{-19}}{1.675 \times 10^{-27}}$$

$$= 625 \times 10^{4} \text{ or } u = 2500 \text{ m/s}$$

With this speed, the time taken by the neutrons to travel a distance of 10 m is, $% \left(\frac{1}{2}\right) =0$

$$t = \frac{10}{2500} = 4 \times 10^{-3} \, \text{s}$$

The fraction of neutrons decayed in time Δt second is,

$$\frac{\Delta N}{N} = \lambda \Delta t \text{ also,} \qquad \lambda = \frac{0.693}{T_{1/2}}$$
$$\frac{\Delta N}{N} = \frac{0.693}{T_{1/2}} \Delta t = \frac{0.693}{700} \times (4 \times 10^{-3}) = 3.96 \times 10^{-6}$$

Example 7: A radioactive sample has 6.0×10^{18} active nuclei at a certain instant. How many of these nuclei will still be in the same active state after two half-lives?

Sol: The number of radioactive nuclei remaining after n half-lives is calculated as $N = \frac{N_o}{2^n}$ where No is the number of nuclei present initially.

In one half-life the number of active nuclei reduces to half the original. Thus, in two half-lives the number is reduced to $\left(\frac{1}{2}\right) \times \left(\frac{1}{2}\right)$ of the original number. The

number of remaining active nuclei is, therefore,

$$6.0 \times 10^{18} \times \left(\frac{1}{4}\right) = 1.5 \times 10^{18}$$

Example 8: The half-life of radium is about 1600 years. In how much time will 1 g of radium (a) reduce to 100 mg (b) lose 100 mg ?

Sol: The weight of radioactive nuclei remaining after n half-lives is calculated as $W = \frac{W_o}{2^n}$ where Wo is the mass present originally. Here $n = \frac{t}{T}$ where T is the half-life.

W =
$$\frac{W_o}{2^{(t/T)}}$$
 where T=1600 yr.

(a)
$$W_0 = 1$$
gm, $W = 0.1$ gm. $2^{(t/T)} = 1/0.1 = 10$

Or
$$\frac{t}{T}\log 2 = 1$$
 or $t = \frac{T}{\log 2} = \frac{1600}{0.301} = 5,333 \text{ yr}$
(b) $W_0 = 1$, $W = 1 - 0.1 = 0.9 \text{ gm}$
 $2^{(t/T)} = \frac{1}{0.9} \text{ or } \frac{t}{T}\log 2 = 0.0458$
 $t = \frac{0.0458 \times 1600}{0.301} = 243.3 \text{ yr}$

Example 9: The activity of a radioactive sample falls from 600/s to 500/s in 40 minutes. Calculate its half-life.

Sol: The activity of any radioactive element is found by $A = A_0 e^{-\lambda t}$. The decay constant is found easily by above equation. The half-life is obtained by $T_{1/2} = \frac{ln2}{\lambda}$. We have $A = A_0 e^{-\lambda t}$

or,
$$500 \, \text{s}^{-1} = (600 \, \text{s}^{-1}) \text{e}^{-\lambda t}$$
 or, $\text{e}^{-\lambda t} = \frac{5}{6}$

or,
$$\lambda t = \ln(6/5) \text{ or}, \lambda = \frac{\ln(6/5)}{t} = \frac{\ln(6/5)}{40 \text{ min}}$$

$$\therefore T_{1/2} = \frac{\ln 2}{\lambda}, \quad \therefore \text{ The half-life is}$$
$$T_{1/2} = \frac{\ln 2}{\ln(6/5)} \times 40 \text{ min} = 152 \text{ min}.$$

JEE Advanced/Boards

Example 1: The disintegration rate of a certain radioactive sample initially is 4750 disintegrations per minute. Five minutes later the rate becomes 2700 disintegrations per minute. Calculate the half-life of the sample.

Sol: The decay constant is obtained using $\lambda = \frac{1}{t} \log_e \left(\frac{A_0}{A}\right)$ where A_0 is the initial activity and A is

the activity at the time t. As decay constant is obtained we can easily calculate the half-life of the sample using

$$T_{1/2} = \frac{\log_e 2}{\lambda}$$

Let N_0 is initial no of nuclei and N is no. of nuclei after five minutes

Initially
$$-\left(\frac{dN}{dt}\right)_0 = \lambda N_0$$

Five minutes later, $-\left(\frac{dN}{dt}\right)_t = \lambda N$

$$\therefore \frac{N_0}{N} = \left(\frac{dN}{dt}\right)_0 / \left(\frac{dN}{dt}\right)_t = \frac{4750}{2700} = 1.76$$

Also N = N₀e^{$-\lambda t$}

$$\lambda = \frac{1}{t} \log_{e} \left(\frac{N_{0}}{N} \right) = \frac{2.3026}{5} \log_{10} \left(1.76 \right)$$

= 0.11306 per min.

Further $T_{1/2} = \frac{\log_e 2}{\lambda} = \frac{0.6931}{0.11306} = 6.13$ minutes.

Example 2: In the interior of the sun, a continuous process of 4 protons, fusing into a helium nucleus and pair of positron, is going on. Calculate

(a) The release of energy per process

(b) Rate of consumption of hydrogen to produce 1 MW power.

Given $_{1}H^{1} = 1.007825$ a.m.u. (atom)

 $_{2}$ He⁴ = 4.002603 a.m.u. (atom)

 $m_{e^+} = m_{e^-} = 5.5 \times 10^{-4} a.m.u.$

(Neglect the energy carried away by neutrons)

Sol: The energy produced in sun during one fusion reaction is $E=\Delta mc^2~J~=\Delta m\times 931.5~MeV$. Take the

ratio of the power required and the energy released from one reaction to get the number of reactions required per second.

(a) During fusion

_

(i) Initially 4 ${}^{1}_{1}H \rightarrow {}^{4}_{2}He + 2 {}^{0}_{+1}e$ and loses 2 bound electrons

$$4_{1}$$
H¹ has 4 bound electrons while
₂He⁴ has only 2 bound electrons

Energy released in fusion = $\Delta m \times 931.5$ MeV

$$= \left\{ 4 \begin{bmatrix} 1 \\ 1 \end{bmatrix} - 1 \begin{bmatrix} 4 \\ 2 \end{bmatrix} + 2 \begin{bmatrix} 0 \\ +1 \end{bmatrix} - 2 \begin{bmatrix} 0 \\ -1 \end{bmatrix} + 2$$

$$= 4(1.0078) - [4.0026 + 4 \times 0.0006] \times 931.5$$

MeV=24.685 MeV

(ii) Later the two positrons combine with 2 electrons to annihilate each other and release energy.

Energy release = $4(0.00055) \times 931 \text{MeV} = 2.049 \text{ MeV}$

:. Total energy release per fusion = 24.685+2.049= 26.734 MeV

(b) $26.735 \text{MeV} = 4.277 \times 10^{-12} \text{ J}$

This energy corresponds to 4(1.007825) a.m.u.

 $1 \text{ MW power} = 10^6 \text{ Js}^{-1}$

Mass of hydrogen required for producing energy of $10^6\,\mathrm{J}$

$$=\frac{10^{6}\times6.692\times10^{-27}}{4.277\times10^{-12}}=1.565\times10^{-9}\,\mathrm{kg}$$

 \therefore Rate of consumption of hydrogen required to produce 1 MW power = $1.565 \times 10^{-9} \text{kgs}^{-1}$

Example 3: The element curium $^{248}_{96}$ Cm has a mean life of 10^{13} seconds. Its primary decay modes are spontaneous fission and α – decay, the former with a probability of 8% and the latter with probability of 92%. Each fission releases 200 MeV of energy. The masses involved in are as follows:

$$_{99}$$
Cm²⁴⁸ = 248.07220u
 $_{94}$ Pu²⁴⁴ = 244.064100u
And $_{2}$ He⁴ = 4.002603u

Calculate the power output from a sample of $10^{20}\,\rm Cm$

atoms.
$$\left(1 \text{amu}=931 \frac{\text{MeV}}{\text{c}^2}\right)$$

Sol: The energy released in each transformation is found by $E = \Delta m \times c^2$ J. As the probabilities of each fission is given the total energy Et released in respective transformation is Probability × E where E is the energy liberated during any one fission reaction. And the power liberated during the entire process is given by

 $P = \frac{E_T}{\tau}$ where ET is the total energy released during fission of all the molecules of the sample.

 α - decay of Cm takes place as follows:

$$_{96}$$
 Cm²⁴⁸ $\rightarrow _{94}$ Pu²⁴⁴ + $_{2}$ He⁴

$$\therefore$$
 Mass defect = Δm ; $\Delta m = (M)_{cm} - [(M)_{pu} + M_{\alpha}]$

$$\Delta m = (248.07220) - [244.064100 + 4.002603]$$

 $\Delta m = 0.005517 u$

Energy released per α – decay

= (0.005517)(931) MeV = 5.136 MeV

Probability of spontaneous fission=8%

Probability of α – decay = 92%

Energy released in each $\frac{248}{96}$ Cm transformation

 $= (0.08 \times 200 + 0.92 \times 5.136)$ MeV = 20.725 MeV

Energy released by 10²⁰ atoms

 $= 20.725 \times 10^{20} \text{ MeV}$

Mean life time = 10^{13} sec

power =
$$\frac{20.725 \times 10^{20} \text{MeV}}{10^{13} \text{ sec}}$$

= $20.725 \times 10^7 \times (1.6 \times 10^{-13}) \frac{\text{joule}}{\text{sec}} = 3.316 \times 10^{-5} \text{ watt.}$

Example 4: In the chain analysis of a rock, the mass ratio of two radioactive isotopes is found to be 100:1. The mean lives of the two isotopes are 4×10^9 year and 2×10^9 year respectively. If it is assumed that at the time of formation of the rock, both isotopes were in equal proportion, calculate the age of the rock. Ratio of atomic weights of the two isotopes is 1.02:1.

 $(\log_{10} 1.02 = 0.0086).$

Sol: The number of the radioactive nuclei remaining at time t is given as $N_t = N_o e^{-\lambda t}$. Here the ratio of the masses are given. The ratio of number of atoms are

given by $\frac{N_1}{N_2} = \frac{m_1}{m_2} \frac{M_2}{M_1}$. Find the value of t from the ratio $\frac{N_{t1}}{N_{t2}}$.

At the time of formation of the rock, both isotopes have the same number of nuclei N₀. Let λ_1 and λ_2 be the decay constants of the two isotopes. If N₁ and N₂ are the number of their nuclei after a time t, we have

$$N_1 = N_0 e^{\lambda_1 t}$$
 and $N_2 = N_0 e^{\lambda_2 t}$ $\frac{N_1}{N_2} = e^{(\lambda_1 - \lambda_2)t}$... (i)

Let the masses of the two isotopes at time t be m_1 and m_2 and let their respective atomic weights be M_1 and M_2 . We have $m_1 = N_1 M_1$ and $m_2 = N_2 M_2$

$$\frac{N_1}{N_2} = \frac{m_1}{m_2} \frac{M_2}{M_1} \qquad ... (ii)$$

Substituting the value given in the problem, we get

$$\frac{N_1}{N_2} = \frac{100}{1} \times \frac{1}{1.02} = \frac{100}{1.02}$$

Let t_1 and t_2 be the mean lives of the two isotopes.

Then
$$t_1 = \frac{1}{\lambda_1}$$
 and $t_2 = \frac{1}{\lambda_2}$
Which gives $\lambda_1 - \lambda_2 = \frac{t_1 - t_2}{t_1 t_2} = \frac{2 \times 10^9 - 4 \times 10^9}{(2 \times 10^9) \times (4 \times 10^9)}$
$$= -0.25 \times 10^{-9}$$

Setting this value in Eqn. (i), we get

$$\frac{N_1}{N_2} = e^{\left(0.25 \times 10^{-9}\right)t} \Rightarrow t = \frac{1}{0.25 \times 10^{-9}} \log_e \frac{100}{1.02}$$

= 18.34×10^9 year

Example 5: A small quantity of solution containing $^{24}_{11}$ Na radioactive nuclei (half-life 15 hours) of activity 1.0 μ Ci is injected into the blood of a person. A sample of the blood of volume 1 cc taken after 5 hours showed an activity of 296 disintegrations per minute. Determine the total volume of blood in the body of the person. Assume that the radioactive solution mixed uniformly in the blood of the person.

(1 Curie = 3.7×10^{10} disintegration per second)

Sol: The activity of the radioactive nuclei is given by $A_o = \lambda N_0$ where λ is the decay constant of the radioactive nuclei. Find the number of radioactive nuclei N_0 present initially. Also find the number of nuclei in the sample of the blood initially. The ratio of these two gives the volume.

We know that
$$T_{1/2} = \frac{0.693}{\lambda}$$
 or
 $\lambda = \frac{0.693}{T_{1/2}} = \frac{0.693}{15 \times 3600} = 1.283 \times 10^{-5}$ / sec. ... (i)

Now activity
$$A_o = \frac{dN}{dt} = \lambda N_o$$
 ... (ii)

Where
$$A_0 = 1$$
 micro curie = $1 \times 3.7 \times 10^4$

= 3.7×10^4 disintegrations / sec

From equation (ii) we have

$$3.7 \times 10^4 = 1.283 \times 10^{-5} \times N_0$$

 $N_0 = \frac{3.7 \times 10^4}{1.283 \times 10^{-5}} = 2.883 \times 10^9$

Let the number of radioactive nuclei present after 5 hours be $N_{1} \mbox{ in } 1 \mbox{ cc sample of blood}.$

Then
$$\frac{dN}{dt} = \lambda N_1$$
 or $\frac{296}{60} = \frac{0.693}{15 \times 3600} N_1$
or $N_1 = \frac{296 \times 15 \times 3600}{60 \times 0.693} = 3.844 \times 10^5$

Let $N_0^\prime\,be$ the number of radioactive nuclei in per cc of sample, then

Then
$$N'_0 = (2)^{t/T} \times N_1$$

 $N'_0 = (2)^{5/15} \times N_1 = (2)^{1/3} \times 3.844 \times 10^5$
 $= 1.269 \times 3.844 \times 10^5 \left[(2)^{1/3} = 1.269 \right] = 4.878 \times 10^5$
Volume of blood $V = \frac{N_0}{N'_0} = \frac{2.883 \times 10^9}{4.878 \times 10^5}$
 $= 0.5910 \times 10^4 \text{ cm}^3 = 5.91 \text{ litres.}$
 $T = \frac{0.693}{\lambda} = \frac{0.693}{0.113} \text{ min} = 6.14 \text{ min}$

Example 6: The half-life of radium is 1620 years. How many radium atoms decay in 1s in a 1g sample of radium? The atomic weight of radium is 226 g/mol.

Sol. Number of radioactive nuclei disintegrated in

1 second is found by $\frac{\Delta N}{\Delta t} = \lambda N$ here λ is the decay constant and N is the number of nuclei present in 1 g sample of radium.

Number of atoms in 1g sample is

$$N = \left(\frac{1}{226}\right) \left(6.02 \times 10^{23}\right) = 2.66 \times 10^{21} \text{ atoms.}$$

The decay constant is

$$\lambda = \frac{0.693}{T_{1/2}} = \frac{0.693}{(1620)(3.16 \times 10^7)} = 1.35 \times 10^{-11} \text{s}^{-1}$$

Taking 1 yr = 3.16×10^7 s;

Now,
$$\frac{\Delta N}{\Delta t} = \lambda N = (1.35 \times 10^{-11})(2.66 \times 10^{21})$$

= $3.6 \times 10^{10} \text{ s}^{-1}$

Thus, 3.6×10^{10} nuclei decay in one second.

Example 7: Determine the age of an ancient wooden piece if it is known that the specific activity of C^{14} nuclide in it amounts to 3/5 of that in freshly felled trees. The half-life of C^{14} nuclide is 5570 years.

Sol: Find the age of wooden piece using equation $A = A_0 e^{-\lambda t}$. Here A is $\frac{3}{5}A_0$ and λ is the decay constant. Specify activity is the activity per unit mass of the substance.

$$A = A_0 e^{-\lambda t}; \quad \text{Here } A = (3/5)A_0$$

$$\therefore \quad \frac{3}{5}A_0 = A_0 e^{-\lambda t} \text{ or } t = \frac{\ln\frac{5}{3}}{\lambda}$$

or $t = \ln\left(\frac{5}{3}\right) / (\ln 2/T) = 5570 \left(\ln\frac{5}{3}\right)$
$$= 4.1 \times 10^3 \text{ years}$$

JEE Main/Boards

Exercise 1

Nuclear Physics

Q.1 Some amount of radioactive substance (half-life= 10 days) is spread inside a room and consequently the level of radiation becomes 50 times permissible level for normal occupancy of the room. After how many days the room will be safe for occupation?

Q.2 The mean lives of a radioactive substance are 1620 and 405 years for α – emission and β –emission respectively. Find out the time during which three forth of a sample will Decay if it is decaying both by α – emission and β –emission simultaneously.

Q.3 A radioactive element decays by β -emission. A detector records n-beta particles in 2 Seconds and in next 2 seconds it records 0.75 n beta particles. Find mean life correct to nearest whole number. Given log2=0.6931, log3=1.0986.

Q.4 Nuclei of radioactive element A are being produced at a constant rate ∞ . The element has a decay constant λ . At time t = 0 there are N₀ nuclei of the element.

(a) Calculate the number N of nuclei of A at time t.

(b) If $\alpha = 2N_0 \lambda$, calculate the number of nuclei of A after one half-life of A and also the limiting value of N at $t \to \infty$

Q.5 Polonium $\binom{210}{84}$ Po) emits $\frac{4}{2}\alpha$ - particles and is converted into lead $\binom{206}{82}$ Pb). The Reaction is used for producing electric power in a space mission. $\frac{210}{84}$ Po has half of 138.6days. Assuming an efficiency of 10% of the thermoelectric machine, how much $\frac{210}{84}$ Po is required to produce 1.2×10^7 J of electric energy per day at the end of 693 days? Also find the initial activity of the material. (Given masses of the nuclei $\frac{210}{84}$ Po = 209.98264 amu, $\frac{206}{82}$ Pb = 205.97440 amu, $\frac{4}{2}\alpha$ = 4.00260 amu, 1 amu = 931 MeV and Avogadro number= 6×10^{23} / mol).

Q.6 A nuclear explosion is designed to deliver 1MW of heat energy, how many fission events must be required

in a second to attain this power level. If this explosion is designed with nuclear fuel consisting of uranium -235 to run a reactor at this power level for one year, then calculate the amount of fuel needed. You can assume that the amount of energy released per fission event is 200 MeV.

Q.7 Draw a diagram to show the variation of binding energy per nucleon with mass number for different nuclei. State with reason why light nuclei usually undergo nuclear fusion.

Q.8 Define decay constant of radioactive sample. Which of the following radiations, α – rays, β – rays, γ – rays

- (i) Are similar to X-rays/
- (ii) Are easily absorbed by matter?
- (iii) Travel with greatest speed?
- (iv) Are similar in nature to cathode rays?

Q.9 Calculate the energy released in the following nuclear reaction:

 ${}_{3}^{6}\text{Li} + {}_{0}^{1}\text{n} \rightarrow {}_{2}^{4}\text{He} + {}_{1}^{3}\text{H}$ (Given; mass of ${}_{3}^{6}\text{Li} = 6.015126 \text{ u}$, mass of ${}_{0}^{1}\text{n} = 1.008665 \text{ u}$, mass of ${}_{2}^{4}\text{He} = 4.002604 \text{ u}$, mass of ${}_{1}^{3}\text{H} = 3.016049 \text{ u}$ and 1 atomic mass unit (1 u)) = 931 MeV)

Q.10 Explain with an example, whether the neutronproton ration in a nucleus increases or decreases due to beta (β) decay.

Q.11 Define the herms; 'half-life period' and 'decay constant' of radioactive sample. Derive the relation between these terms.

Q.12 When a deuteron of mass 2.0141 u and negligible

kinetic energy is absorbed by a lithium $\binom{6}{Li_3}$ nucleus

of mass 6.0155 u, the compound nucleus disintegrates spontaneously into two alpha particles, each of mass 4.0026 u. Calculate the energy in joules carried by each

alpha particle. $(1u = 1.66 \times 10^{-27} \text{kg})$

Q.13 A radioactive sample contains 2.2 mg of pure ${}_{6}^{11}C$ which has half-life period of 1224 seconds. Calculate

(i) The number of atoms present initially.

(ii) The activity when 5 μ g of the sample will be left.

Q.14 Define the terms half-life period and decay constant of a radioactive substance. Write their S.I. units. Establish the relationship between the two.

Q.15 A neutron is absorbed by a ${}_{3}^{6}$ Li nucleus with the subsequent emission of an alpha particle.

(i) Write the corresponding nuclear reaction.

(ii) Calculate the energy released, in MeV, in this reaction.

Given mass ${}_{3}^{6}$ Li = 6.015126 u;

Mass (neutron) = 1.0086554 u;

Mass (alpha particle) = 4.0026044 u and

Mass (triton) = 3.0100000 u. Take 1 u = 931 MeV/C^2 .

Q.16 Define the term 'activity' of a radionuclide. Write its SI unit.

Q.17 Draw graph showing the variation of potential energy between a pair of nucleons as a function of their separation. Indicate the regions in which the nuclear force is

(i) Attractive (ii) Repulsive

Q.18 Draw the graph to show variation of binding energy per nucleon with mass number of different atomic nuclei. Calculate binding energy/nucleon of $^{40}_{20}$ Ca nucleus.

Q.19 State two characteristic properties of nuclear force.

Q.20 Calculate the energy, released in MeV, in the following nuclear reaction

 $\sum_{92}^{238} U \rightarrow_{90}^{234} Th +_{2}^{4} He + Q \qquad \left[Mass of \frac{238}{92} U = 238.05079 \text{ u} \right]$ Mass of $234_{90}^{234} Th = 234.043630 \text{ u} Mass of \frac{4}{2} He = 4.002600 \text{ u}$ $Iu = 931.5 MeV / c^{2}$

Q.21 Two nuclei have mass numbers in the ration 1:8. What is the ration of their nuclear radii?

Q.22 The mass of a nucleus in its ground state is always less than the total mass of its Constituents neutrons and protons. Explain.

Q.23 Draw a plot showing the variation of binding energy per nucleon versus the mass number A. Explain with the help of this plot the release of energy in the processes of nuclear fission and fusion.

Q.24 Define the activity of a radionuclide. Write its S.I. unit. Give a plot of the activity of a radioactive species versus time.

Q.25 Draw a plot of the binding energy per nucleon as a function of mass number for a large Number of nuclei, $2 \le A \le 240$. How do you explain the constancy of binding energy per nucleon in the range 30 < A < 170 using the property that nuclear force is short-range?

Radioactivity

Q.26 Classify each of the following nuclides as "beta $\begin{pmatrix} 0 \\ -1 \end{pmatrix}$ emitter", or "positron $\begin{pmatrix} 0 \\ -1 \end{pmatrix}$ emitter": ${}^{49}_{20}$ Ca ${}^{195}_{80}$ Hg ${}^{5}_{8}$ B ${}^{150}_{67}$ Ho ${}^{30}_{13}$ Al ${}^{94}_{36}$ Kr. Note: ${}^{84}_{36}$ Kr ${}^{200}_{80}$, Hg and ${}^{165}_{67}$ Ho are stable.

Q.27 Of the three isobars ${}^{114}_{48}$ Cd ${}^{114}_{49}$ In and ${}^{114}_{50}$ Sn, which is likely to be radioactive? Explain your choice.

Q.28 Complete the following nuclear equations;

- (a) ${}^{14}_{7}N + {}^{4}_{2}He \rightarrow {}^{17}_{8}O + \dots$
- (b) ${}^{9}_{4}\text{Be} + {}^{4}_{2}\text{He} \rightarrow {}^{12}_{6}\text{C} + \dots$
- (c) ${}_{4}^{9}Be(p,\alpha)$
- (d) ${}^{30}_{15}P \rightarrow {}^{30}_{14}S + \dots$
- (e) ${}_{1}^{3}H \rightarrow {}_{2}^{3}He + \dots$
- (f) $^{43}_{20}$ Ca(∞ ,.....) \rightarrow^{46}_{21} Sc

Q.29 The activity of the radioactive sample drops to 1/64 of its original value in 2 hr find the decay constant (λ) .

Q.30 The nucleidic ration of ³H to ${}_{1}^{1}$ H in a sample of water is 8.0×10^{-18} : 1. Tritium undergoes decay tritium atoms would 10.0 g of such a sample contains 40 year after the original sample is collected?

Q.31 The half-life period of $\frac{125}{53}$ I is 60 days. What % of radioactivity would be present after 240 days?

Q.32 At any given time a piece of radioactive material $(t_{1/2} = 30 \text{ days})$ contains 10^{12} atoms.

Calculate the activity of the sample in dps.

Q.33 Calculate the age of a vegetarian beverage whose tritium content is only 15% of the level in living plants. Given $t_{1/2}$ for ${}_{1}^{3}H = 12.3$ years.

Q.34 An isotopes of potassium ⁴⁰₁₉K has a half-life of

 1.4×10^9 year and decays to Argon $^{40}_{18}$ Ar which is stable.

(i) Write down the nuclear reaction representing this decay.

(ii) A sample of rock taken from the moon contains both potassium and argon in the ratio 1/3. Find age of rock.

Q.35 At a given instant there are 25% undecayed radioactive nuclei in a sample. After 10 sec the number of undecayed nuclei remain 12.5%. Calculate :

(i) mean-life of the nuclei and

(ii)The time in which the number of undecayed nuclear will further reduce to 6.25% of the reduced number.

Q.36 Calculate the energy released in joules and MeV in the following nuclear reaction :

 $_1^2H +_1^2H \rightarrow_2^3He +_0^1n$ Assume that the masses of $_1^2H$,

³₂He and neutron (n) respectively are 2.020, 3.0160 and

1.0087 in amu.

Q.37 (a) Calculate number of α – and β -particles emitted when ${}^{238}_{92}$ U changes into radioactive ${}^{206}_{82}$ Pb.

(b) Th^{234} disintegrates and emits 6β – and 7α – particles to form a stable element. Find the atomic number and mass number of the stable product.

Q.38 One of the hazards of nuclear explosion is the generation of Sr^{90} and its subsequent incorporation in

bones. This nuclide has a half-life of 28.1 year. Suppose one microgram was absorbed by a new-born child, how much Sr⁹⁰ will remain in his bones after 20 years?

Q.39 (i) $^{210}_{84}$ Po decays with α – particle to $^{206}_{82}$ Pb with a half-life of 138.4 day. If 1.0 g of $^{210}_{84}$ Po is placed in a sealed tube, how much helium will accumulate in 69.2 day? Express the answer in cm³ at 1atm and 273K. Also report the volume of He formed if 1 g of $^{210}_{64}$ Po is used.

(ii) A sample of U^{238} (half-life = 4.5×10^9 yr) ore is found to contain 23.8 g of U^{238} and 20.6 g of Pb²⁰⁶. Calculate the age of the ore.

Q.40 Ac²²⁷ has a half-life of 22 year w.r.t radioactive decay. The decay follows two parallel paths, one leading the Th^{227} and the other leading to Fr^{223} . The percentage yields of these two daughters nucleides are 2% and 98% respectively. What is the rate constant in yr^{-1} , for each of these separate paths?

Exercise 2

Nuclear Physics

Single Correct Choice Type

Q.1 Let u be denoted one atomic mass unit. One atom of an element of mass number A has mass exactly equal to Au

- (A) For any value of A
- (B) Only for A = 1
- (C) Only for A = 12
- (D) For any value of A provided the atom is stable

Q.2 The surface area of a nucleus varies with mass number A as

(A) $A^{2/3}$ (B) $A^{1/3}$ (C) A (D) None

Q.3 Consider the nuclear reaction $X^{200} \rightarrow A^{110} + B^{90}$ If the binding energy per nucleon for X,A and B is 7.4 MeV, 8.2. MeV and 8.2 MeV respectively, what is the energy released?

(A) 200 MeV	(B) 160 MeV
(C) 110 MeV	(D) 90 MeV

Q.4 The binding energy per nucleon for C^{12} is 7.68 MeV and that for C^{13} is 7.5 MeV. The energy required to remove a neutron from C^{13} is

(A) 5.34 MeV	(B) 5.5 MeV
(C) 9.5 MeV	(D) 9.34 MeV

Q.5 The binding energies of nuclei X and Y are E_1 and E_2 respectively. Two atoms of X fuse to give one atom of Y and an energy Q is released. Then:

(A) $Q = 2E_1 - E_2$	(B) $Q = E_2 - 2E_1$
(C) $Q = 2E_1 + E_2$	(D) $Q = 2E_2 + E_1$

Q.6 There are two radio-nuclei A and B. A is an alpha emitter and B is a beta emitter. Their disintegration constants are in the ratio of 1:2. What should be the ratio of number of atoms of two at time t = 0 so that probabilities of getting α – and β – particles are same at time t=0.

(A) 2:1 (B)1:2 (C)e (D) e⁻¹

Q.7 A certain radioactive substance has a half-life of 5 years. Thus for a particular nucleus in a sample of the element, the probability of decay in ten years is

(A) 50% (B) 75% (C) 100% (D) 60%

Q.8 Half-life of radium is 1620 years. How many radium nuclei decay in 5 hours in 5 gm radium? (Atomic weight of radium = 223)

(A) 9.1×10 ¹²	(B) 3.23×10 ¹⁵
(C) 1.72×10 ²⁰	(D) 3.3×10^{17}

Q.9 The decay constant of the end product of a radioactive series is

(A) Zero

(B) Infinite

(C) Finite (non zero)

(D) Depends on the end product.

Q.10 A radioactive nuclide can decay simultaneously by two different processes which have decay constants λ_1 and λ_2 . The effective decay constant of the nuclide is λ , then :

(A)
$$\lambda = \lambda_1 + \lambda_2$$

(B) $\lambda = 1/2(\lambda_1 + \lambda_1)$
(C) $\frac{1}{\lambda} = \frac{1}{\lambda_1} + \frac{1}{\lambda_2}$
(D) $\lambda = \overline{\lambda_1 \lambda_2}$

Radioactivity

Single Correct Choice Type

Q.11 $^{27}_{13}$ Al is a stable isotope. $^{29}_{13}$ Al is expected to be disintegrated by

(A) α emission (B) β emission

(C) Positron emission (D) Proton emission.

Q.12 Loss of a β – particle is equivalent to

- (A) Increase of one proton only
- (B) Decrease of one neutron only
- (C) Both (A) and (B)
- (D) None of these

Q.13 Two radioactive material A_1 and A_2 have decay constant of $10\lambda_0$ and λ_0 . If initially they have same number of nuclei, then after time $\frac{1}{9\lambda_0}$ the ratio of number of their undecayed nuclei will be

(A)
$$\frac{1}{e}$$
 (B) $\frac{1}{e^2}$ (C) $\frac{1}{e^3}$ (D) $\frac{\sqrt{e}}{1}$

Q.14 The half-life of a radioactive isotopes is three hours. If the initial mass of the isotope were 256 g, the mass of it remaining undecayed after 18 hours would be

(A) 16.0 g (B) 4.0 g (C) 8.0 (D) 12.0 g

Q.15 A consecutive reaction $A \xrightarrow{k_1} B \xrightarrow{k_2} C$ is characterised by

- (A) Maxima in the concentration of A
- (B) Maxima in the concentration of B
- (C) Maxima in the concentration of C
- (D) High exothermicity

Q.16 Consider the following nuclear reactions: $^{238}_{92}M \rightarrow^{X}_{Y}N + 2 {}^{4}_{2}He; {}^{X}_{Y}N \rightarrow^{A}_{B}L + 2\beta^{+}$

The number of neutrons in the element L is

(A) 142 (B)144 (C)140 (D)146

Q.17 The half-life of a radioisotope is four hours. If the initial mass of the isotope was 200 g, the mass remaining after 24 hours undecayed is

(A) 1.042 g (B) 2.084 g (C) 3.125 g (D) 4.167 g

Q.18 Helium nuclei combines to form an oxygen nucleus. The binding energy per nucleon of oxygen nucleus is if $m_0 = 15.834$ amu and $m_{He} = 4.0026$ amu

(A) 10.24 MeV	(B) 0 MeV
(C) 5.24 MeV	(D) 4 MeV

Q.19 A radioactive element gets spilled over the floor of a room. Its half-life period is 30 days. If the initial activity is ten times the permissible value, after how many days will it be safe to enter the room?

(A) 1000 days	(B) 300 days
(C) 10 days	(D) 100 days

Q.20 Which of the following nuclear reactions will generate an isotope ?

- (A) neutron particle emission
- (B) position emission
- (C) α-particle emission
- (D) β-particle emission

Q.21 Read the following:

(i) The half-life period of a radioactive element X is same as the mean-life time of another radioactive element Y. Initially both of them have the same number of atoms. Then Y will decay at a faster rate than X.

(ii) The electron emitted in beta radiation originates from decay of a neutron in a nucleus

(iii) The half-life of²¹⁵ at is 100 ms. The time taken for the radioactivity of a sample of of^{215} At to decay to $1/16^{th}$ of its initial value is 400 us.

(iv) The volume (V) and mass (m) of a nucleus are related as V \propto m.

(v) Given a sample of Radium-226 having half-life of 4 days. Find the probability. A nucleus disintegrates within 2 half-lives is $\frac{3}{4}$

Select the correct code for above.

(A) TTTTT	(B) TFTTF
(C) FTFTF	(D) FTTTF

Q.22 The radioactive sources A and B of half-lives of t hours respectively, initially contain the same number of radioactive atoms. At the end of t hours, their rates of disintegration are in the ratio:

(A) 2√2:1	(B) 1:8
(C) $\sqrt{2}$:1	(D) n:1

Q.23 The ratio of ¹⁴C to ¹²C in a living matter is measured to be $\frac{{}^{14}C}{{}^{14}C} = 1.3 \times 10^{-12}$ at the present time. Activity of 12.0 gm carbon sample is 180 dpm. The half-life of ¹⁴C is nearly ______x 10^{-12} sec. [Given: N_A = 6x10²³] (A) 0.18 (B) 1.8 (C) 0.384 (D) 648

Q.24 Which of the following processes represent a gamma – decay?

(A)
$$\stackrel{A}{_{Z}}X + y \rightarrow \stackrel{A}{_{Z-1}}X + a + b$$

(B) $\stackrel{A}{_{Z}}X + \stackrel{1}{_{0}}n \rightarrow \stackrel{A-3}{_{Z-2}}X + c$
(C) $\stackrel{A}{_{Z}}X \rightarrow \stackrel{A}{_{Z}}X + f$
(D) $\stackrel{A}{_{Z}}X + \stackrel{1}{_{-1}}e \rightarrow \stackrel{A}{_{-1}}X + g$

Q.25 Let F_{pp} , F_{pn} and F_{nn} denote the magnitudes of net force by a proton on a proton, by a proton on a neutron and by a neutron on a neutron respectively. Neglect gravitational force. When the separation is 1 fm,

(A) $F_{pp} > F_{pn} = F_{nn}$ (B) $F_{pp} = F_{pn} = F_{nn}$ (C) $F_{pp} > F_{pn} > F_{nn}$ (D) $F_{pp} < F_{pn} = F_{nn}$

Q.26 The average (mean) life at a radio nuclide which decays by parallel path is

$$A \xrightarrow{\lambda_1} B; \quad \lambda_1 = 1.8 \times 10^{-2} \text{ sec}^{-1}$$
$$2A \xrightarrow{\lambda_2} C; \quad \lambda_2 = 10^{-3} \text{ sec}^{-1}$$

(A) 52.63 sec (B) 500 sec

(C) 50 sec (D) None

Q.27 Two radioactive nuclides A and B have half lives of 50 min respectively. A fresh sample contains the nuclides of B to be eight time that of A. How much time should elapse so that the number of nuclides of A becomes double of B

(A) 30 (B) 40 (C) 50 (D) None

Q.28 A sample of ¹⁴CO₂ was to be mixed with ordinary CO_2 for a biological tracer experiment. In order that 10 cm^3 of diluted gas should have 10^4 dis/min, what activity (in μ Ci) of radioactive carbon is needed to

prepare 60 L of diluted gas at STP. [1 Ci = 3.7×10^{10} dps] (A) 270 μ Ci (B)27 μ Ci (C) 2.7 μ Ci (D)2700 μ Ci

Q.29 Wooden article and freshly cut tree show activity of 7.6 and 15.2 min⁻¹ gm⁻¹ of carbon ($t_{1/2} = 5760$ years) respectively. The age of article in years. Is

(A) 5760 (B) $5760x\left(\frac{15.2}{7.6}\right)$ (C) $5760\times\left(\frac{7.6}{15.2}\right)$ (D) $5760\times(15.2-7.6)$

Q.30 A radioactive sample had an initial activity of 56 dpm (disintegration per min it was found to have an activity of 28 dpm. Find the number of atoms in a sample having an activity of 10 dpm.

(A) 693 (B) 1000 (C) 100 (D) 10,000

Q.31 The radioactivity of a sample is R_1 at a time T_1 and R_2 at a time T_2 . If the half-life of the specimen is T, the number of atoms that have disintegrated in the time $(T_2 - T_1)$ is proportional to

(A) $(R_1T_1 - R_2T_2)$	(B) $(R_1 - R_2)$
(C) $(R_1 - R_2) / T$	(D) (R ₁ -R ₂)T/0.693

Previous Years' Questions

Q.1 The half-life of the radioactive radon is 3.8 days. The time, at the end of which $1/20^{\text{th}}$ of the radon sample will remain undecayed, is (given $\log_{10} 3 = 0.4343$) (1981)

(A) 3.8 days	(B) 16.5 days
(C) 33 days	(D) 76 days

Q.2 Beta rays emitted by a radioactive material are (1983)

(A) Electromagnetic radiations

(B) The electrons orbiting around the nucleus

- (C) Charged particles emitted by the nucleus
- (D) Neutral particles

Q.3 The equation ;

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(1987)
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 $4_{1}^{1}H \rightarrow {}_{2}^{4}He^{2+} + 2e^{-} + 26 \text{ MeV}$ represents

ecay

(C) Fusion (D) Fission

Q.4 During a negative beta decay (1987)

(A) An atomic electron is ejected

(B) An electron which is already present within the nucleus is ejected

(C) A neutron in the nucleus decays emitting an electron

(D) A part of the binding energy of the nucleus is converted into an electron

Q.5 A star initially has 10^{40} deuterons. It produces energy via the processes ${}_{1}H^{2} + {}_{1}H^{2} \rightarrow {}_{1}H^{3}p$ and ${}_{1}H^{2} + {}_{1}H^{3} \rightarrow {}_{2}He^{4} + n$. If the average power radiated by the star is 10^{16} W, the deuteron supply of the star is exhausted in a time of the order of **(1993)**

(A) 10^6 s (B) 10^8 s (C) 10^{12} s (D) 10^{16} s

Q.6 Fast neutrons can easily be slowed down by(1994)

- (A) The use of lead shielding
- (B) Passing them through heavy water
- (C) Elastic collisions with heavy nuclei
- (D) Applying a strong electric field

Q.7 Consider α -particles, β -particles and λ -rays each having an energy of 0.5 MeV. In increasing order of penetrating powers, the radiations are **(1994)**

(A) α, β, γ (B) α, γ, β (C) β, γ, α (D) γ, β, α

Q.8 A radioactive sample S_1 having an activity of 5 μ Ci has twice the number of nuclei as another sample S_2 which has an activity of 10 μ Ci. The half lives of S_1 and S_2 can be (2008)

- (A) 20 yr and 5 yr, respectively
- (B) 20 yr and 10 yr, respectively
- (C) 10 yr each
- (D) 5 yr each

Q.10 In the uranium radioactive series the initial nucleus is $^{238}_{92}$ U and the final nucleus is $^{206}_{92}$ Pb. When

Q.11 Consider the reaction: ${}_{1}^{2}H + {}_{1}^{2}H = {}_{2}^{4}He + Q$. Mass of the deuterium atom = 2.0141u. Mass of helium atom = 4.0024u. This is a nuclear reaction in which the energy Q released is MeV. (1996)

Q.12 This question contains Statement-I and Statement-I. II. Of the four choices given after the statements, choose the one that best describes the two statements.

Statement–I: Energy is released when heavy nuclei undergo fission or light nuclei undergo fusion.

and

Statement–II: For heavy nuclei, binding energy per nucleon increases with increasing Z while for light nuclei it decrease with increasing Z. *(2008)*

(A) Statement-I is false, statement-II is true.

(B) Statement-I is true, statement-II is true; statement-II is correct explanation for statement-I.

(C) Statement-Iis true, statement– 2 is true; statement-II is nota correct explanation for statement-I.

(D) Statement-I is true, statement-II is False.

Q.13 Suppose an electron is attracted towards the origin by a force k/r where 'k' is a constant and 'r' is the distance of the electron from the origin. By applying Bohr model to this system, the radius of the nth orbital of the electron is found to be ' r_n ' and the kinetic energy of the electron to be T_n . Then which of the following is true? (2008)

 $\begin{array}{ll} \text{(A)} \ T_n \propto 1/n^2, \ rn \ \propto n^2 & \text{(B)} \ T_n \ independent \ of \ n, \ r_n \ \propto n \\ \text{(C)} \ T_n \propto 1/n, \ rn \ \propto n & \text{(D)} \ T_n \ \propto 1/n, \ rn \ \propto n^2 \\ \end{array}$

Q.14 The above is a plot of binding energy per nucleon $E_{b'}$ against the nuclear mass M; A, B, C, D, E, F correspond to different nuclei. Consider four reactions: **(2009)**

(ii) C \rightarrow A + B + ϵ

(iii) D + E \rightarrow F + ϵ and

(iv)
$$F \rightarrow D + E + \epsilon$$

where ϵ is the energy released? In which reactions is ϵ positive?



Q.15 The transition from the state n = 4 to n = 3 in a hydrogen like atom results in ultraviolet radiation. Infrared radiation will be obtained in the transition from (2009)

(A) 2 →1	(B) 3 →2

J) J-J
1

Q.16 The binding energy per nucleon for the parent nucleus is E_1 and that for the daughter nuclei is E_2 . Then (2010)

(A) $E_2 = 2E_1$	(B) $E_1 > E_2$
(C) E ₂ > E ₁	(D) $E_1 = 2E_2$

Q.17 The speed of daughter nuclei is (2010)

(A) c
$$\frac{\Delta m}{M + \Delta m}$$
 (B) c $\sqrt{\frac{2\Delta m}{M}}$
(C) c $\sqrt{\frac{\Delta m}{M}}$ (D) c $\sqrt{\frac{\Delta m}{M + \Delta m}}$

Q.18 A radioactive nucleus (initial mass number A and atomic number Z) emits 3 a-particles and 2 positrons. The ratio of number of neutrons to that of protons in the final nucleus will be (2010)

(A)
$$\frac{A-Z-8}{Z-4}$$
 (B) $\frac{A-Z-4}{Z-8}$
(C) $\frac{A-Z-12}{Z-8}$ (D) $\frac{A-Z-4}{Z-8}$

Z – 4

Q.19 Energy required for the electron excitation in Li⁺⁺ from the first to the third Bohr orbit is: (2011)

Z – 2

(A) 36.3 eV	(B) 108.8 eV
(C) 122.4 eV	(D) 12.1 eV

Q.20 The half life of a radioactive substance is 20 minutes. The approximate time interval $(t_2 - t_1)$ between

the time t_2 when $\frac{2}{3}$ of it has decayed and time t_1 and $\frac{1}{3}$ of it had decayed is : (2011) (A) 14 min (B) 20 min (C) 28 min (D) 7 min

Q.21 Hydrogen atom is excited from ground state to another state with principal quantum number equal to 4. Then the number of spectral lines in the emission spectra will be (2012)

(A) 2 (B) 3 (C) 5 (D) 6

Q.22 Assume that a neutron breaks into a proton and an electron. The energy released during this process is (Mass of neutron = 1.6725×10^{-27} kg; mass of proton = 1.6725×10^{-27} kg; mass of electron = 9×10^{-31} kg) (2012)

(A) 0.73 MeV	(B) 7.10 MeV
(C) 6.30 MeV	(D) 5.4 MeV

Q.23 As an electron makes a transition from an excited state to the ground state of a hydrogen - like atom/ion: (2015)

(A) its kinetic energy increases but potential energy and total energy decrease

(B) kinetic energy, potential energy and total energy decrease

(C) kinetic energy decreases, potential energy increases but total energy remains same

(D) kinetic energy and total energy decrease but potential energy increases

Q.24 Half-lives of two radioactive elements A and B are 20 minutes and 40 minutes, respectively, Initially, the samples have equal number of nuclei. After 80 minutes, the ratio of decayed numbers of A and B nuclei will be : (2016)

(A) 4 : 1 (B) 1 : 4 (C) 5 : 4 (D) 1 : 16

JEE Advanced/Boards

Exercise 1

Nuclear Physics

Q.1 The binding energies per nucleon for deuteron $(_1H^2)$ and helium $(_2He^4)$ are 1.1 MeV and 7.0 MeV respectively. The energy released when two deuterons fuse to form a helium nucleus $(_2He^4)$ is _____

Q. 2 An isotopes of Potassium ${}^{40}_{19}$ K has a half-life of 1.4×10^9 year and decay to Argon ${}^{40}_{18}$ Ar which is stable.

(i) Write down the nuclear reaction representing this decay.

(ii) A sample of rock taken from the moon contains both potassium and argon in the ratio 1/7. Find age of rock.

Q.3 At t=0, a sample is placed in a reactor. An unstable nuclide is produced at a constant rate R in the sample by neutron absorption. This nuclide β -decays with half-life τ . Find the time required to produce 80% of the equilibrium quantity of this unstable nuclide.

Q.4 Suppose that the Sun consists entirely of hydrogen

atom and releases the energy by the nuclear reaction,

 $4_1^1 H \rightarrow {}_2^4 He$ with 26 MeV of energy released. If the total output power of the Sun is assumed to remain constant at 3.9 x 10^{26} W, find the time it will take to burn all the hydrogen, Take the mass of the Sun as $1.7x \ 10^{30}$ kg.

Q.5 U^{238} and U^{235} occur in nature in an atomic ratio 140:1. Assuming that at the time of earth's formation the two isotopes were present in equal amounts. Calculate the age of the earth.

(Halflife of $u^{238} = 4.5 \times 109$ years and that of $U^{235} = 7.13 \times 10^8$ years)

Q.6 The kinetic energy of an α -particle which flies out of the nucleus of a Ra²²⁶ atom in radioactive disintegration in 4.78 MeV. Find the total energy the escape of the α -particle.

Q.7 A small bottle contains powdered beryllium Be & gaseous radon which is used as a source of α -particles. Neutrons are produced when α -particles of the radon react with beryllium. The yield of this reaction is (1/4000) i.e. only one α -particle out of 4000 induces the reaction.

Find the amount of radon (Rn^{222}) originally introduced into the source. If it produces 1.2 x 10⁶ neutrons per second after 7.6 days. [$T_{1/2}$ of R_a = 3.8 days]

Q.8 An experiment is done to determine the half-life of radioactive substance that emits one β -particle for each decay process. Measurement show that an average of 8.4 β are emitted each second by 2.5 mg of the substance. The atomic weight of the substance is 230. Find the half-life of the substance.

Q.9 A wooden piece of great antiquity weighs 50 gm and shows C^{14} activity of 320 disintegrations per minute. Estimate the length of the time which has elapsed since this wood was part of living tree, assuming that living plant show a C^{14} activity of 12 disintegrations per minute per gm. The half-life of C^{14} is 5730 yrs.

Q.10 When two deuterons $\binom{2}{1}H$ fuse to from a helium nucleus $_{2}He^{4}$, 23.6 MeV energy is released. Find the binding energy of helium if it is 1.1 MeV for each nucleon of deutrim.

Q.11 A π^+ meson of negligible initial velocity decays to a μ^+ (muon) and a neutrino. With what kinetic energy (in eV) does the muon move? (The rest mass of neutrino can be considered zero. The rest mass of the π^+ meson is 150 MeV and the rest mass of the muon is 100 MeV.) Take neutrino to behave like a photon.

Take $\sqrt{3} = 1.41$.

Q.12 A body of mass m_0 is placed on a smooth horizontal surface. The mass of the body is decreasing exponentially with disintegration constant λ . Assuming that the mass is ejected backward with a relative velocity u. Initially the body was at rest. Find the velocity of body after time t.

Q.13 Show that in a nuclear reaction where the outgoing particle is scattered at an angle of 90⁰ with the direction of the bombarding particle, the Q-value is expressed as

$$Q = K_p \left(1 + \frac{m_p}{M_o} \right) - K_1 \left(1 + \frac{m_1}{M_o} \right)$$

Where, I=incoming particle, P=product nucleus, T=target nucleus, O=outgoing particle.

Radioactivity

Q.14 In a nature decay chain series starts with $_{90}$ Th²³² and finally terminates at $_{82}$ Pb²⁰⁸. A thorium ore sample was found to contain 8 x 10⁻⁵ ml of helium at 1 atm & 273 K and 5 x 10⁻⁷ gm of Th²³². Find the age of ore sample assuming that source of He to be only due to decay of Th²³². Also assume complete retention of helium within the ore. (Half-life of Th²³² = 1.39 x 10¹⁰ Y)

Q.15 A radioactive decay counter is switched on at t=0. A β -active sample is present near the counter. The counter registers the number of β -particles emitted by the sample. The counter registers 1 x 10⁵ β -particles at t=36 s and 1.11 x 10⁵ β -particles at t = 108 s. Find T_{1/2} of this sample.

Q.16 A small quantity of solution containing ²⁴Na radionuclide (half-life 15 hours) of activity 1.0 microcurie is injected into the blood of a person. A sample of the blood of volume 1 cm³ taken after 5 hours shows an activity of 296 disintegrations per minute. Determine the total volume of blood in the body of the person. Assume that the radioactive solution mixes uniformly in the blood of the person. (1 Curie=3.7 x 10^{10} disintegrations per second)

Q.17 A mixture of ²³⁹Pu and ²⁴⁰Pu has a specific activity of 6×10^9 dis/s/g. The half lives of the isotopes are 2.44 x 10^4 y and 6.08 x 10^3 y respectively. Calculate the isotopic composition of this sample.

Q.18 Nuclei of a radioactive element A are being produced at a constant rate α . The element has a decay constant λ . At time t=0, there are N₀ nuclei of the element.

(a) Calculate the number N of nuclei of A at time t

(b) If $\alpha = 2N_0\lambda$, calculate the number of nuclei of A after one half-life of A & also the limiting value of N as t $\rightarrow \infty$

Q.19 In hydrogenation reaction at 25° C, it is observed that hydrogen gas pressure falls from 2 atm to 1.2 atm in 50 min. Calculate the rate of reaction in molarity per sec. R=0.0821 litre atm degree $^{-1}$ mol⁻¹

Q.20 $\frac{^{238}}{^{92}}$ U by successive radioactive decays changes

to $\frac{^{206}}{_{82}}$ Pb . A sample of uranium ore was analyzed and

found to contain 1.0g of U^{238} and 0.1g of PB^{206} . Assuming that all the PB^{206} had accumulated due to decay of U^{238} , find out the age of the ore.

(Halflife of $U^{238} = 4.5 \times 10^9$ years)

Q.21 $^{218}_{84}$ Po (t_{/12} = 3.05 min) decay to $^{214}_{82}$ Pb (t_{/12} = 3.05 min) by α -emission, while Pb²¹⁴ is a β – emitter . In an experiment starting with 1 gm atom of Pure Po²¹⁸, how much time would be required for the number of nuclei of $^{214}_{82}$ Pb to reach maximum?

Q.22 (a) On analysis a sample of uranium ore was found to contain 0.277g of ${}^{206}_{82}$ Pb and 1.667 g of ${}^{237}_{92}$ U. The half-life period of U²³⁸ is 4.51 x 10⁹ year. If all the lead were assumed to have come from decay of ${}^{238}_{92}$ U, what is the age of earth?

(b) An ore of $\frac{238}{92}$ U is found to contain $\frac{238}{92}$ U and $\frac{236}{92}$ U in the weight ratio of 1:0.1. The half-life period of $\frac{238}{92}$ U is 4.5 x 10⁹ year. Calculate the age of ore.

Q.23 An experiment requires minimum β -activity produced at the rate of 346 β -particles per minute. The half-life period of $\frac{99}{42}$ Mo which is a β -emitter is 66.6 hr. Find the minimum amount of $\frac{99}{42}$ Mo required to carry out the experiment in 6.909 hour.

Exercise 2

Nuclear Physics

Single Correct Choice Type

Q.1 The rest mass of the deuteron, ${}_{1}^{2}H$, is equivalent to an energy of 1876 MeV, the rest mass of a proton is equivalent to 939 MeV and that of a neutron to 940 MeV. A deuteron may disintegrate to a proton and a neutron if it :

(A) Emits a γ -ray photon of energy 2 MeV

- (B) Captures a γ -ray photon of energy 2 MeV
- (C) Emits a γ -ray photon of energy 3 MeV
- (D) Captures a γ -ray photon of energy 3 MeV

Q.2 A certain radioactive nuclide of mass number m_x disintegrates, with the emission of an electron and γ radiation only, to give second nuclide of mass number m_y . Which one of the following equation correctly relates m_x and m_v ?

(A) $m_y = m_x + 1$	(B) $m_y = m_x - 2$
(C) $m_y = m_x - 1$	(D) $m_y = m_x$

Q.3 The number of α and β -emitted during the radioactive decay chain starting from $^{226}_{88}$ Ra and ending at $^{206}_{82}$ Pb is

(A) 3α & 6β ⁻	(B) 4α & 5β ⁻
(C) 5α & 4β ⁻	(D) 6α & 6β ⁻

Q.4 In an α -decay the Kinetic energy of α particle is 48 MeV Q-value of the reaction is 50 MeV. The mass number of the mother nucleus is : (Assume that daughter nucleus is in ground state)

(C) 104 (D) None of these

Q.5 In the uranium radioactive series the initial nucleus is ${}^{238}_{92}$ U, and the final nucleus is ${}^{206}_{82}$ Pb. When the uranium nucleus decays to lead, the number of α -particles emitted is. And the number of β -particles emitted.

(A) 6, 8	(B) 8, 6
(C) 16, 6	(D) 32, 12

Q.6 Activity of a radioactive substance is \textbf{R}_1 at time \textbf{t}_1

and R_2 at time $t_2(t_2 > t_1)$. Then the $\frac{R_2}{R_1}$ is : (A) $\frac{t_2}{t_1}$ (B) $e^{-\lambda(t_1+t_2)}$ (C) $e\left(\frac{t_1-t_2}{\lambda}\right)$ (D) $e^{\lambda(t_1-t_2)}$

Q.7 A particular nucleus in a large population of identical radioactive nuclei did survive 5 half lives of

that isotope. Then the probability that this surviving nucleus will survive the next half-life :

(A)
$$\frac{1}{32}$$
 (B) $\frac{1}{5}$ (C) $\frac{1}{2}$ (D) $\frac{5}{2}$

Q.8 The activity of a sample reduces from A_0 to $A_0\sqrt{3}$ in one hour. The activity after 3 hours more will be

(A)
$$\frac{A_0}{3\sqrt{3}}$$
 (B) $\frac{A_0}{9}$ (C) $\frac{A_0}{9\sqrt{3}}$ (D) $\frac{A_0}{27}$

Q.9 The activity of a sample of radioactive material is A_1 at time t_1 and A_2 at time $t_2(t_2 > t_1)$. Its mean life is T.

(A)
$$A_1 t_1 = A_2 t_2$$
 (B) $\frac{A_1 - A_2}{t_2 - t_1}$ = constant

(C)
$$A_2 = A_1 e^{(t_1 - t_2)/T}$$
 (D) $A_2 = A_1 e^{(t_1 - Tt_2)}$

Q.10 A fraction f_1 of a radioactive sample decays in one mean life, and a fraction f_2 decays in one half-life.

(A) $f_1 > f_2$

(B) $f_1 < f_2$

(C) $f_1 = f_2$

(D) May be (A), (B) or (C) depending on the values of the mean life and half-life.

Q.11 A radioactive substance is being produced at a constant rate of 10 nuclei/s. The decay constant of the substance is $1/2 \sec^{-1}$. After what time the number of radioactive nuclei will become 10? Initially there are no nuclei present. Assume decay law holds for the sample.

(A) 2.45 sec (B) log (2) sec
(C) 1.386 sec (D)
$$\frac{1}{\log(2)}$$
sec

Q.12 The radioactivity of a sample is R_1 at time T_1 and T_2 . If the half-life of the specimen is T. Number of atoms that have disintegrated in the $(T_2 - T_1)$ is proportional to

(A)
$$(R_1T_1 - R_2T_2)$$
 (B) $(R_1 - R_2)T$
(C) $(R_1 - R_2) / T$ (D) $(R_1 - R_2)(T_1 - T_2)$

Q.13 The radioactive nucleus of an element X decays to a stable nucleus of element Y. A graph of rate of

formation of Y against time would look like



Q.14 A radioactive substance is dissolved in a liquid and the solution is heated. The activity of the solution

(A) Is smaller than that of element

(B) Is greater than that of element

(C) Is equal to that of element

(D) Will be smaller or greater depending upon whether the solution is weak or concentrated.

Q.15 In a certain nuclear reactor, a radioactive nucleus is being produced at a constant rate =1000/s. The mean life of radionuclide is 40 minutes. At steady state, the number of radionuclide will be

(A)
$$4 \times 10^4$$
 (B) 24×10^4 (C) 24×10^5 (D) 24×10^6

Q.16 In the above question, if there were 20×10^5 radionuclide at t=0, then the graph of N v/s t is



Q.17 A free neutron is decayed into a proton but a free proton is not decayed into a neutron. This is because-

(A) Neutron is a composite particle made of a proton and an electron whereas proton is a fundamental particle

(B) Neutron is an uncharged particle whereas proton is

a changed particle

(C) Neutron has larger rest mass than the proton

(D) Weak forces can be operated in a neutron but not in a proton

Multiple Correct Choice Type

Q.18 When a nucleus with atomic number Z and mass number A undergoes a radioactive decay process:

(A) Both Z and A will decrease, if the process is $\,\alpha\,$ decay

(B) Z will decrease but A will not change, if the process

is β^+ decay

(C) Z will decrease but A will not change, if the process

is β^- decay

(D) Z and A will remain unchanged, if the process is $\,\gamma\,$ decay.

Q.19 When the atomic number A of the nucleus increases

(A) Initially the neutron-proton ratio is constant=1

(B) Initially neutron-proton ratio increases and later decreases

(C) Initially binding energy per nucleon increases when the neutron-proton ratio increases.

(D) The binding energy per nucleon increases when the neutron –proton ratio increases.

Q.20 Let $\,\textbf{m}_{\!p}^{}\,$ be the mass of a proton, $\,\textbf{m}_{\!a}^{}\,$ the mass of

a neutron, $\rm M_1$ the mass of a $^{20}_{10}\rm Ne\,$ nucleus and $\rm M_2$ the

mass of a $^{40}_{20}$ Ca nucleus. Then

(A) $M_2 = 2M_1$	(B) $M_2 > 2M_1$
(C) M ₂ < 2M ₁	(D) $M_1 < 10(m_a + m_p)$

Q.21 The decay constant of a ratio active substance is $0.173 \text{ (years)}^{-1}$. Therefore :

(A) Nearly 63% of the radioactive substance will decay in (1/0.173) year.

(B) Half-life of the radioactive substance is (1/0.173) year.

(C) One-fourth of the radioactive substance will be left after nearly 8 years.

(D) All the above statements are true.

Q.22 The graph shown by the side shows the variation of potential energy ϕ of a proton with its distance 'r' form a fixed sodium nucleus, as it



approaches the nucleus, placed at origin O. Then the portion.

(A) AB indicates nuclear repulsion

(B) AB indicates electrostatic repulsion

(C) BC indicates nuclear attraction

(D) BC represents electrostatic interaction

Q.23 In β -decay, the Q-value of the process is E. Then

(A) K.E. of a β -particle cannot exceed E.

(B) K.E. of antineutrino emitted lies between Zero and E.

(C) N/X ratio of the nucleus is altered.

(D) Mass number (A) of the nucleus is altered.

Q.24 Consider the following nuclear reactions and select the correct statements from the option that follow.

Reaction I: $n \rightarrow p + e^- + v$

Reaction II: $p \rightarrow n + e^+ + v$

(A) Free neutron is unstable, therefore reaction I is possible

(B) Free proton is stable, therefore reaction II is not possible

(C) Inside a nucleus, both decays (reaction I and II) are possible

(D) Inside a nucleus, reaction I is not possible but reaction II is possible

Q.25 When the nucleus of an electrically neutral atom undergoes a radioactive decay process, it will remain neutral after the decay if the process is:

(A) α decay	(B) β -decay
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(C) γ decay (D) K-capture

 $\ensuremath{\textbf{Q.26}}$ The heavier nuclie tend to have larger N/Z ratio because-

(A) A neutron is heavier than a proton

(B) A neutron is an unstable particle

(C) A neutron does not exert electric repulsion

(D) Coulomb forces have longer range compared to the nuclear forces

Q.27 For nuclei with A>100

(A) The binding energy of the nucleus decreases on an average as A increases

(B) The binding energy per nucleon decreases on an average a A increases

(C) If the nucleus breaks into two roughly equal parts energy is released

(D) If two nuclei fuse to form a bigger nucleus energy is released

Q.28 A radioactive sample has initial concentration no. of nuclei-

(A) The number of undecayed nuclei present in the sample decays exponentially with time

(B) The activity (R) of the sample at any instant is directly proportional to the number of undecayed nuclei present in that sample at that time

(C) The no. of decayed nuclei grows exponentially with time

(D) The no. of decayed nuclei grow linearly with time

Q.29 A nuclide A undergoes α decay and another nuclide B undergoes β^- decay-

(A) All the $\,\alpha$ -particles emitted by A will have almost the same speed

(B) The α -particles emitted by A may have widely different speeds

(C) All the $\,\beta$ -particles emitted by B will have almost the same speed

(D) The $\,\beta$ -particles emitted by B may have widely different speeds.

Q.30 A nitrogen nucleus $\frac{14}{7}$ N absorbs a neutron and

can transform into lithium nucleus ${}_{3}\text{Li}^{7}$ under suitable conditions, after emitting :

(A) 4 protons and 3 neutrons

(B) 5 protons and 1 negative beta particle

(C) 1 alpha particle and 2 gamma particles

(D) 1 alpha particle, 4 protons and 2 negative beta particles

(E) 4 protons and 4 neutrons

Q.31 The instability of the nucleus can be due to various causes. An unstable nucleus emits radiations if possible to transform into less unstable state. Then the

cause and the result can be

(A) A nucleus of excess nucleons is α – active

- (B) An excited nucleus of excess protons is $\,\beta^-\,active$
- (C) An excited nucleus of excess protons is $\beta^{\scriptscriptstyle +}$ active
- (D) An nucleus of excess neutrons is $\,\beta^-\,active$

Assertion Reasoning Type

(A) Statement-I is true, statement-II is true and statement-II is correct explanation for statement-I.

(B) Statement-I is true, statement-II is true and statement-II is NOT the correct explanation for statement-I

(C) Statement-I is true, statement-II is false.

(D) Statement-I is false, statement-II is false.

Q.32 Half-life for certain radioactive element is 5 min. Four nuclei of that element are observed a certain instant of time. After five minutes

Statement-I: It can be definitely said that two nuclei will be left undecayed.

Statement-II: After half-life i.e. 5minutes, half of total nuclei will disintegrate. So only two nuclei will be left undecayed.

Q.33 Statement-I: Consider the following nuclear of

an unstable ${}^{14}C_6$ nucleus initially at rest. The decay ${}^{14}C_6 \rightarrow_7^{14} N + {}^0_{-1} e + \overline{v}$. In a nuclear reaction total energy

and momentum is conserved experiments show that the electrons are emitted with a continuous range of kinetic energies upto some maximum value.

Statement-II: Remaining energy is released as thermal energy.

Q.34 Statement-I: It is easy to remove a proton from

 $^{40}_{20}$ Ca nucleus as compared to a neutron

Statement-II: Inside nucleus neutrons are acted on only by attractive forces but protons are also acted on by repulsive forces.

Q.35 Statement-I: It is possible for a thermal neutron to be absorbed by a nucleus whereas a proton or an α -particle would need a much larger amount of energy for being absorbed by the same nucleus.

Statement-II: Neutron is electrically neutral but proton and α - particle are positively charged.

Comprehension Type

Paragraph 1: (Q.36) A town has a population of 1 million. The average electric power needed per person is 300 W. A reactor is to be designed to supply power to this town. The efficiency with which thermal power is converted into electric power is aimed at 25%.

Q.36 Assuming 200 MeV of thermal energy to come from each fission event on an average the number of events that should take place every day.

(A) 2.24×10 ²⁴	(B) 3.24×10^{24}
(C) 4.24×10 ²⁴	(D) 5.24×10^{24}

Paragraph 2: A nucleus at rest undergoes a decay emitting an α particle of de-Broglie wavelength $\lambda = 5.76 \times 10^{-15}$ m. The mass of the daughter nucleus is 223.40 amu and that of α particle is 4.002 amu.

Q.37 The linear momentum of α particle and that of daughter nucleus is-

(A) 1.15×10^{-19} N - s & 2.25×10^{-19} N - s

(B) 2.25×10^{-19} N - s & 1.15×10^{-19} N - s

- (C) Both 1.15×10^{-19} N s
- (D) Both $2.25 \times 10^{-19} \text{N} \text{s}$

Q.38 The kinetic energy of α particle is-

(A) 0.01 Mev	(B) 6.22 MeV
(C) 0.21 Mev	(D) 0.31 MeV

Q.39 The kinetic energy of daughter nucleus is-

(A) 3.16 Mev	(B) 4.16 MeV
(C) 5.16 MeV	(D) 0.11 MeV

Match the Columns

Q.40

	Column I		Column II
(A)	In reaction ${}_{1}^{2}H + {}_{1}^{2}H \rightarrow {}_{2}^{3}He + X$ The X is	(p)	²⁰⁶ Pb
(B)	If $\frac{^{238}}{_{92}}$ U decays by $8\alpha \& 6\beta$ the resulting nuclei is	(q)	¹ ₀ n

	Column I		Column II
(C)	Heavy water is		⁴ ₂ He
(D)	By emission of which particle the position in the periodic table is lowered by 2		¹⁴ ₇ N
(E)	When a deuterium is bombarded on $\frac{16}{8}$ O nucleus, an α particle is emitted, the product nucleus is	(t)	D ₂ O

Q.41

	Column I		Column II
(A)	Nuclear Fusion	(p)	Some matter converted into energy
(B)	Nuclear Fission	(q)	Generally occurs in nuclei having low atomic number
(C)	β – decay	(r)	Generally occurs in nuclei having higher atomic number.
(D)	α – decay	(s)	Essentially occurs due to weak nuclear force.

Q.42

	Column I		Column II
(A)	1 Rutherford	(p)	1 dis/sec
(B)	1 Becquerel	(q)	3.7×10^{10} dis/sec
(C)	1 Curie	(r)	10 ⁶ dis/sec
(D)	Activity of 1g Ra ²²⁶	(s)	10 ¹⁰ dis/sec

Radioactivity

Single Correct Choice Type

Q.43 The analysis of a mineral of Uranium reveals that ratio of mole of ^{206}Pb and ^{238}U in sample is 0.2. If effective decay constant of process $^{238}\text{U} \rightarrow ^{206}\text{Pb}$ is λ then age of rock is

(A)
$$\frac{1}{\lambda} \ln \frac{5}{4}$$
 (B) $\frac{1}{\lambda} \ln \left(\frac{5}{1} \right)$ (C) $\frac{1}{\lambda} \ln \frac{4}{1}$ (D) $\frac{1}{\lambda} \ln \left(\frac{6}{5} \right)$

Q.44 The half-life of Tc^{99} is 6.0 hr. The delivery of a sample of Tc^{99} that must be shipped in order for the lab to receive 10.0 mg?

(A) 20.0 mg (B) 1	15.0 mg
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(C) 14.1 mg	(D) 12.5 mg
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Q.45 A sample contains 0.1 gram-atom of radioactive isotope ${}^{A}_{Z}X(t_{1/2} = 5 days)$. How many number of atoms will decay during eleventh day? [N_A = Avogadro's number]

(A)
$$0.1 \left(-e^{-\frac{0.693 \times 11}{5}} + e^{-\frac{0.693 \times 10}{5}} \right)$$

(B) $0.1 \left(-e^{-\frac{0.693 \times 11}{5}} + e^{-\frac{0.693 \times 10}{5}} \right)$
(C) $0.1 \left(-e^{-\frac{0.693 \times 11}{5}} + e^{-\frac{0.693 \times 10}{5}} \right) N_A$
(D) $0.1 \left(-e^{-\frac{0.693 \times 11}{5}} + e^{-\frac{0.693 \times 10}{5}} \right) N_A$

Multiple Correct Choice Type

Q.46 Which of the following statements are correct about half-life period?

(A) It is proportional to initial concentration for zero-th order.

(B) Average life=1.44 half-life for first order reaction

(C) time of 75% reaction is thrice of half –life period in second order reaction.

(D) 99.9% reaction takes place in 100 minutes for the case when rate constant is 0.0693 $\rm min^{-1}\,is$ 0.5

Q.47 C^{14} is a beta active nucleus. A sample of $C^{14}H_4$ gas kept in a closed vessel shows increase in pressure with time. This is due to

(A) The formation of N^{14} H₃ and H₂

(B) The formation of B^{11} H₃ and H₂

(C) The formation of C^{14} H₄ and H₂

(D) The formation of
$$C^{12} H_3$$
, $N^{14} H_2$ and H_2

Q.48 Select correct statement (s):

(A) The emission of gamma radiation involves transition between energy levels within the nucleus.

(B) 4_2 He is formed due to emission of beta particle from tritium 3_1 H.

(C) When positron $\binom{o}{+1}e$ is emitted, $\frac{n}{n}$ ratio increases.

Comprehension Type

Paragraph 1: Nuclei of a radioactive element 'A' are being produced at a constant rate, α . The element has a decay constant, λ . At time, t=0, there are N₀ nuclei of the element.

Q.49 The number of nuclei of A at time't' is

(A)
$$\frac{\alpha}{\lambda}$$
 (1-e^{- λ t}) (B) N₀. e ^{λ t}

(C)
$$\frac{1}{\lambda} [\alpha - (\alpha - \lambda N_0) e^{-\lambda t}]$$
 (D) $\frac{N_0 \cdot \alpha}{\lambda} \left[1 - \left(1 - \frac{\lambda}{\alpha} \right) e^{-\lambda t} \right]$

Q.50 If $\alpha = 2N_0\lambda$, the number of nuclei of A after one half-life of A becomes

(A) Zero (B) 2N₀ (C) 1.5N₀ (D) 0.5N₀

Paragraph 2: Mass defect in the nuclear reactions may be expressed in terms of the atomic masses of the parent and daughter nuclides in place of their nuclides in place of their nuclear masses.

Q.51 The mass defect of nuclear reaction:

 $_{a}Be^{10} \rightarrow _{5}B^{10} + e^{-is}$

(A) $\Delta m = At.$ mass of $\frac{10}{4}Be - At.$ mass of $\frac{10}{5}Be$

(B) $\Delta m = At. mass of {}^{10}_{4}Be - At. mass of {}^{10}_{5}B - mass of one electron$

(C) $\Delta m = At. mass of \frac{10}{4} Be - At. mass of \frac{10}{5} B + mass of one electron$

(D) $\Delta m = At. mass of \frac{10}{4}Be - At. mass of \frac{10}{5}B - mass of two electron$

Q.52 The mass defect of the nuclear reaction: ${}_{5}B^{8} \rightarrow {}_{4}Be^{8} + e^{+}$ is

(A) $\Delta m = At.$ mass of ${}_{5}^{8}B - At.$ mass of ${}_{4}^{8}Be$

(B) $\Delta m = At.$ mass of ${}_{5}^{8}B - At.$ mass of ${}_{4}^{8}Be$ -mass of one electron

(C) $\Delta m = At. mass of \frac{8}{5}B - At. mass of \frac{8}{4}Be + mass of one electron$

(D) $\Delta m = At. mass of \frac{8}{5}B - At. mass of \frac{8}{4}Be - mass of two electron$

Previous Years' Questions

Q.1 There is a stream of neutrons with a kinetic energy of 0.0327 eV. If the half-life of neutrons is 700 s, what fraction of neutrons will decay before they travel a distance of 10m? (1986)

Q.2 It is proposed to use the nuclear fusion reaction; ${}_{2}^{2}H + {}_{1}^{2}H \rightarrow {}_{2}^{4}He$

ln a nuclear reactor 200MW rating. If the energy from the above reaction is used with a 25 percent efficiency in the reactor, how many grams of deuterium fuel will

be needed per day? (The masses of ${}^{2}_{1}H$ and ${}^{4}_{2}He$ are

2.0141 atomic mass units and 4.0026 atomic mass units respectively.) (1990)

Q.3 A nucleus X, initially at rest, undergoes alpha-decay

according to the equation ${}^{A}_{92}X \rightarrow {}^{228}_{z}Y + \alpha$.

(a) Find the values of A and Z in the above process.

(b) The alpha particle produced in the above process is found to move in a circular track of radius 0.11m in a uniform magnetic field of 3T. Find the energy (in Mev) released during the process and the binding energy of the parent nucleus X.

Given that
$$m(Y) = 228.03u; m({}_0^1n) = 1.009u$$

 $m({}_2^4He) = 4.003u; m({}_1^1H) = 1.008u.$ (1991)

Q.4 A small quantity of solution containing Na^{24} radio nuclide (half-life=15h) of activity 1.0 microcurie is injected into the blood of a person. A sample of the blood of volume 1 cm³ taken after 5h shows an activity of 296 disintegrations per minute. Determine the total volume of the blood in the body of the person. Assume that the radioactive solution mixes uniformly in the blood of the person.

(1 curie = 3.7×10^{10} disintegrations per second) (1994)

Q.5 The element curium $^{248}_{96}\text{Cm}$ has a mean life of 10^{13}s .

Its primary decay modes are spontaneous fission and α -decay, the former with a probability of 8% and the latter with a probability of 92%, each fission releases 200 MeV of energy. The masses involved in decay are as follows: (1997)

 $^{248}_{96}Cm = 248.072220u$,

 $^{244}_{94}$ Pu = 244.064100u and $^{4}_{2}$ He = 4.002603u.

Calculate the power output from a sample of 10^{20} Cm atoms. (1u = 931MeV / c²)

Q.6 Nuclei of a radioactive element A are being produced at a constant rate α . The element has a decay constant λ . At time t = 0, there are N₀ nuclei of the element. (1998)

(a) Calculate the number N of nuclei of A at time t.

(b) If $\alpha = 2N_0\lambda$, calculate the number of nuclei of A after one hale-life of A and also the limiting value of N as $t \rightarrow \infty$.

Q.7 In a nuclear reactor ²³⁵U undergoes fission liberating 200 MeV of energy. The reactor has a 10% efficiency and produces 1000 MW power. If the reactor is to function for 10yr, find the total mass of uranium required. **(2001)**

Q.8 A radioactive nucleus X decays to a nucleus Y with a decay constant $\lambda_x = 0.1s^{-1}$, Y further decays to a stable nucleus Z with a decay constant $\lambda_y = 1/30s^{-1}$. Initially, there are only X nuclei and their number is $N_0 = 10^{20}$. Set up the rate equations for the populations of X, Y and z. The population of Y nucleus as a function of time is given by

$$N_{y}(t) = \left\{N_{0}\lambda_{x} / (\lambda_{x} - \lambda_{y})\right\} \left[\exp\left(-\lambda_{y} t\right) - \exp\left(-\lambda_{x} t\right)\right]$$

Find the time at which N_y is maximum and determine the populations X and Z at that instant. (2001)

Q.9 A rock is 1.5×10^9 yr old. The rock contains ²³⁸U which disintegrates to from ²⁰⁶Pb. Assume that there was no ²⁰⁶Pb in the rock initially and it is the only stable product formed by the decay. Calculate the ratio of number of nuclei of ²³⁸U to that of ²⁰⁶Pb in the rock. Half-life of ²³⁸U is 4.5×10^9 yr. $(2^{1/3} = 1.259)$ (2004)

Q.10 To determine the half-life of a radioactive element, a

student plots a graph of
$$ln \left| \frac{dN(t)}{dt} \right|$$
 versus t. Here $\frac{dN(t)}{dt}$

is the rate of radioactive decay at time t. If the number of radioactive nuclei of this element decreases by a factor of p after 4.16yr, the value of p is **(2010)**



Q.11 The activity of a freshly prepared radioactive sample is 10^{10} disintegrations per second, whose mean life is 10^{-9} s. The mass of an atom of this radioisotope is 10^{-25} kg. The mass (in mg) of the radioactive sample is (2011)

Q.12 Some laws and processes are given in column I. Match these with the physical phenomena given in column II. (2006)

	Column I		Column II
(A)	Nuclear Fusion	(p)	Converts some matter into energy
(B)	Nuclear Fusion	(q)	Generally possible for nuclei with low Atomic number
(C)	β – decay	(r)	Generally possible for nuclei with higher Atomic number.
(D)	Exothermic nuclear reaction	(s)	Essentially proceeds by weak nuclear forces

Q.13 In the core of nuclear fusion reactor, the gas becomes plasma because of (2009)

(A) Strong nuclear force acting between the deuterons

(B) Coulomb force acting between the deuterons

(C) Coulomb force acting between deuteron-electron pairs

(D) The high temperature maintained inside the reactor core

Q.14 Assume that two deuteron nuclei in the core of fusion reactor at temperature T are moving towards each other , each with kinetic energy 1.5kT, when the separation between them is large enough to neglect Coulomb potential energy. Also neglect any interaction from other particles in the core. The minimum temperature t required for them to reach a separation of 4×10^{-15} m is in the range (2009)

Q.15 Assume that the nuclear binding energy per nucleon (B/A) versus mass number (A) is as shown in the figure. Use this plot to choose the correct choice(s) given below. *(2008)*



(A) Fusion of two nuclei with mass numbers lying in the range of 1 < A < 50 will release energy

(B) Fusion of two nuclei with mass numbers lying in the range of 51 < A < 100 will release energy

(C) Fission of a nucleus lying in the mass range of 100 < A < 200 will release energy when broken into two equal fragments

(D) Fission of a nucleus lying in the mass range of 200 < A < 260 will release energy when broken into two equal fragments

Q.16 Results of calculations for four different designs of a fusion reactor using D-D reaction are given below.

Which of these is most promising based on Lawson criterion? (2009)

(A) Deuteron density = 2.0×10^{12} cm⁻³, confinement time = 5.0×10^{-3} s

(B) Deuteron density = 8.0×10^{14} cm⁻³, confinement time = 9.0×10^{-1} s

(C) Deuteron density = 4.0×10^{23} cm⁻³, confinement time = 1.0×10^{-11} s

(D) Deuteron density = 1.0×10^{24} cm⁻³, confinement time = 4.0×10^{-12} s

Q.17 A freshly prepared sample of a radioisotope of half-life 1386s has activity 10³ disintegrations per second.

Given that $\ln 2 = 0.693$, the fraction of the initial number of nuclei (expressed in nearest integer percentage) that will decay in the first 80 s after preparation of the sample is (2013)

(A) 4% (B) 5% (C) 5.5% (D) 3%

Q.18 A nuclear power plant supplying electrical power to a village uses a radioactive material of half life T years as the fuel. The amount of fuel at the beginning is such that the total power requirement of the village is 12.5 % of the electrical power available form the plant at that time. If the plant is able to meet the total power needs of the village for a maximum period of nT years, then the value of n is **(2014)**

(A) 2 (B) 5 (C) 3 (D) 4

Q.19 Match the nuclear processes given in column I with the appropriate option(s) in column II (2015)

	Column I		Column II
(A)	Nuclear fusion	(p)	Absorption of thermal neutrons by $\frac{235}{92}$ U
(B)	Fission in a nuclear reactor	(q)	⁶⁰ ₂₇ Co nucleus
(C)	β -decay	(r)	Energy production in stars via hydrogen conversion to helium
(D)	γ -ray emission	(s)	Heavy water
		(t)	Neutrino emission

Q.20 The isotope ${}_{5}^{12}$ B having a mass 12.014 u undergoes β decay to ${}_{6}^{12}C \cdot {}_{6}^{12}C$ has an excited state of the nucleus (${}_{6}^{12}C^*$) at 4.041 MeV above its ground state. If ${}_{5}^{12}$ B decays to ${}_{6}^{12}C^*$, the (1 u = 931.5 MeV/c²), where c is the speed of light in vacuum) **(2016)**

Q.21 A radioactive sample S1 having an activity 5μ Ci has twice the number of nuclei as another sample S2 which has an activity of 10 μ Ci. The half lives of S1 and S2 can be (2008)

(A) 20 years and 5 years, respectively

- (B) 20 years and 10 years, respectively
- (C) 10 years each
- (D) 5 years each

Q.22 The electric field at r = R is

(A) Independent of a

(B) Directly proportional to a

(C) Directly proportional to a²

(D) Inversely proportional to a

Q.23 For a = 0, the value of d (maximum value of ρ as shown in the figure) is (2008)

(A)
$$\frac{3Ze}{4\pi R^3}$$
 (B) $\frac{3Ze}{\pi R^3}$ (C) $\frac{4Ze}{3\pi R^3}$ (D) $\frac{Ze}{3\pi R^3}$

Q.24 The electric field within the nucleus is generally observed to be linearly dependent on r. This implies. (2008)

(A)
$$a = 0$$
 (B) $a = \frac{R}{2}$ (C) $a = R$ (D) $a = \frac{2R}{3}$

Q.25 To determine the half-life of a radioactive element,

a student plots a graph of log $\left|\frac{dN(t)}{dt}\right|$ versus t. Here $\frac{dN(t)}{dt}$ is the rate of radioactive decay at time t. If the number of radioactive nuclei of this element decreases by a factor of p after 4.16 years, the value of p is **(2009)**



Q.26 What is the maximum energy of the anti-neutrino? (2012)

(A) Zero

(2008)

(B) Much less than $0.8 \times 10^6 \text{ eV}$

(C) Nearly $0.8 \times 10^6 \text{ eV}$

(D) Much larger than $0.8 \times 10^6 \text{ eV}$

Q.27 If the anti-neutrino had a mass of $3eV/c^2$ (where c is the speed of light) instead of zero mass, what should be the range of the kinetic energy, K, of the electron? *(2012)*

(A) $0 \le K \le 0.8 \times 10^{6} \text{ eV}$ (B) $3.0 \text{ eV} \le K \le 0.8 \times 10^{6} \text{ eV}$ (C) $3.0 \text{ eV} \le K < 0.8 \times 10^{6} \text{ eV}$ (D) $0 \le K < 0.8 \times 10^{6} \text{ eV}$

Q.28 The radius of the orbit of an electron in a Hydrogen-like atom is 4.5 a_0 where a_0 is the Bohr radius. Its orbital angular momentum is $\frac{3h}{2\pi}$. It is given that h is Planck's constant and R is Rydberg constant. The

possible wavelength(s), when the atom de-excites, is (are) (2013)

(A)
$$\frac{9}{32R}$$
 (B) $\frac{9}{16R}$ (C) $\frac{9}{5R}$ (D) $\frac{4}{3R}$

Direction: The mass of nucleus ${}^{A}_{Z}X$ is less than the sum of the masses of (A-Z) number of neutrons and Z number of protons in the nucleus. The energy equivalent to the corresponding mass difference is known as the binding energy of the nucleus. A heavy nucleus of mass M can break into two light nuclei of mass m₁ and m₂ only if (m₁ + m₂) < M. Also two light nuclei of masses m3 and m4 can undergo complete fusion and form a heavy nucleus of mass M' only if (m₁ + m₄) > M'. The masses of some neutral atoms are given in the table below:

¹ ₁ H	1.007825 u	² ₁ H	2.014102 u	
⁶ ₃ Li	6.015123 u	⁷ ₃ Li	7.016004 u	
¹⁵² ₆₄ Gd	151.919803 u	²⁰⁶ ₈₂ Pb	205.974455 u	
³ ₁ H	3.016050 u	⁴ ₁ He	4.002603 u	
⁷⁰ ₃₀ Zn	69.925325 u	⁸² ₃₄ Se	81.916709 u	
²⁰⁹ 83Bi	208.980388 u	²¹⁰ ₈₄ Po	209.982876 u	

Q.29 The correct statement is

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(2013)
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(A) The nucleus $\frac{6}{3}$ Li can emit an alpha particle

(B) The nucleus $\frac{210}{84}$ Po can emit a proton.

(C) Deuteron and alpha particle can undergo complete fusion.

(D) The nuclei $\frac{70}{30}$ Zn and $\frac{82}{34}$ Se can undergo complete fusion.

Q.30 The kinetic energy (in keV) of the alpha particle, when the nucleus $\frac{210}{84}$ Po at rest undergoes alpha decay, is (2013)

(A) 5319 (B) 5422 (C) 5707 (D) 5818

Q.31 Match List I of the nuclear processes with List II containing parent nucleus and one of the end products of each process and then select the correct answer using the codes given below the lists: (2013)

	List I		List II
(i)	Alpha decay	(p)	${}^{15}_{8}O \rightarrow {}^{15}_{7}N +$
(ii)	$\beta^{\scriptscriptstyle +}$ decay	(q)	$^{258}_{92}U \rightarrow^{234}_{90}$ Th+
(iii)	Fission	(r)	$^{185}_{83}\text{Bi} \rightarrow ^{184}_{82}\text{Pb} +$
(iv)	Proton emission	(s)	$^{239}_{94}$ Pu \rightarrow^{140}_{57} La +

Codes:

	р	q	r	S
(A)	(iv)	(ii)	(i)	(iii)
(B)	(i)	(iii)	(ii)	(iv)
(C)	(ii)	(i)	(iv)	(iii)
(D)	(iv)	(iii)	(ii)	(i)

Q.32 If λ_{cu} is the wavelength of K_a X-ray line of copper (atomic number 29) and λ_{Mo} is the wavelength of the K_a X-ray line of molybdenum (atomic number 42), then the ratio $\lambda_{cu} / \lambda_{Mo}$ is close to **(2014)** (A) 1.99 (B) 2.14 (C) 0.50 (D) 0.48

Q.33 An electron in an excited state of Li^{2+} ion has angular momentum $3h/2\pi$. The de Broglie wavelength of the electron in this state is $p\pi a_0$ (where a_0 is the Bohr radius). The value of p is (2015)

(A) πa_0 (B) $2\pi a_0$ (C) $4\pi a_0$ (D) $3\pi a_0$

Q.34 For a radioactive material, its activity A and rate of change of its activity R are defined as $A = -\frac{dN}{dt}$ and $R = dA - \frac{dA}{dt}$, where N(t) is the number of nuclei at time t. Two radioactive sources P (mean life τ) and Q(mean life 2τ) have the same activity at t = 0. Their rates of change of activities at t = 2τ are R_p and R_Q respectively. If $\frac{R_p}{R_Q} = \frac{n}{e}$, then the value of n is (2015)

(A)
$$\frac{1}{2e}$$
 (B) $\frac{2}{e}$ (C) $\frac{3}{e}$ (D) $\frac{2}{3e}$

Q.35 A fission reaction is given by $^{236}_{92}U \rightarrow^{140}_{54} Xe + ^{94}_{38} Sr + x + y$, where x and y are two particles. Considering ${}^{236}_{92}$ U to be at rest, the kinetic energies of the products are denoted by K_{Xe'}, K_{sr'} K_x(2MeV) and K_y(2MeV), respectively. Let the binding energies per nucleon of ${}^{236}_{92}$ U, ${}^{140}_{54}$ Xe and ${}^{94}_{38}$ Sr be 7.5

MeV, 8.5 MeV and 8.5 MeV respectively. Considering different conservation laws, the correct option(s) is(are) (2015)

(A) $x = n, y = n, K_{sr} = 129 \text{MeV}, K_{xe} = 86 \text{ MeV}$ (B) $x = p, y = e^{-}, K_{sr} = 129 \text{ MeV}, K_{xe} = 86 \text{ MeV}$ (C) $x = p, y = n, K_{sr} = 129 \text{ MeV}, K_{xe} = 86 \text{ MeV}$ (D) $x = n, y = n, K_{sr} = 86 \text{ MeV}, K_{xe} = 129 \text{ MeV}$

Q.36 The electrostatic energy of Z protons uniformly distributed throughout a spherical nucleus of radius R

is given by $E = \frac{3}{5} \frac{Z(Z-1)e^2}{4\pi\epsilon_0 R}$ The measured masses of the neutron, ¹₁H, ¹⁵₇N and ¹⁵₈O are 1.008665 u, 1.007825 u, 15.000109 u and 15.003065 u, respectively. Given that the radii of both the $^{15}_{7}$ N and $^{15}_{8}$ O nuclei are same, 1 u = 931.5 MeV/c² (c is the speed of light) and e²/(4 π ε₀) = 1.44 MeV fm. Assuming that the difference between the binding energies of $^{15}_{7}$ N and $^{15}_{8}$ O is purely due to the electrostatic energy, the radius of either of the nuclei is (1 fm = 10⁻¹⁵ m) **(2016)**

(A) 2.85 fm	(B) 3.03 fm
(C) 3.42 fm	(D) 3.80 fm

Q.37 An accident in a nuclear laboratory resulted in deposition of a certain amount of radioactive material of half-life 18 days inside the laboratory. Tests revealed that the radiation was 64 times more than the permissible level required for safe operation of the laboratory. What is the minimum number of days after which the laboratory can be considered safe for use? (2016)

(A) 64 (B) 90 (C) 108 (D) 120

PlancEssential Questions

JEE Main/Boards

Exercise 1 Q.5 Q.13 Q.28

Q.31	Q.34	Q.40

Exercise 2

Q.6	Q.11	Q.23
Q.24	Q.26	Q.27
Q.29		

JEE Advanced/Boards

Exercise 1					
Q. 7	Q.8	Q.13	Q.14		
Q.15	Q.17	Q.19	Q.23		
Exercise	Exercise 2				
Q.1	Q.12	Q.13	Q.22		
Q.27	Q.37	Q.38	Q.39		
Q.43	Q.44	Q.40	Q.49		
Q.50					

Previous Years' Question

Q.1	Q.7	Q.10	Q.12
Q.14			

Answer Key

JEE Main/E	Boards				
Exercise 1					
Nuclear Physics					
Q.1 56.45 days		Q.2 449.94 year		Q.3 7s	
Q.4 $\frac{\alpha}{\lambda}$		Q.5 4.57×10^{21} day	s ⁻¹	Q.6 384.5g	
Radioactivity					
Q.26 beta emitter:	⁴⁹ Ca, ³⁰ Al, ⁹⁴ Kr, pos	itron emitter : ¹⁹⁵ He	g, ⁸ B, ¹⁵⁰ Ho		
Q.27 ¹¹⁴ ₄₉ In, odd nu	umber of neutrons		Q.28 (a) ¹ ₁ H, (b) ¹ ₀ r	$(c)_{3}^{6}Li, (d)_{+1}^{0}e, (e)$	$e_{-1}^{0}e_{,-1}(f)^{-1}p_{,-1}(f)$
Q.29 $\lambda = 2.078 hr^{-1}$	1		Q.30 5.05×10 ⁶ ator	ns	, - (, +1
Q.31 6.25%	Q.31 6.25% Q.32 2.67×10 ⁵ sec ⁻¹				
Q.33 33.67 years			Q.34 (i) ${}^{40}_{19}$ K $\rightarrow {}^{40}_{18}$ A	$r + {}^{0}_{1} e + v$ (ii) 2.8×1	_0 ⁹ years
Q.35 (i) t _{means} = 14	1.43s (ii) 40 sec		Q.36 ∆E = 14.25 M	ev	
Q.37 (a) No.of α -	particles=8, No.ofβ	-particles=6; (b)	Pb		
Q.38 6.13×10 ⁻⁷ g		02	Q.39 (i) 31.25 cm ³	,27.104 cm ³ (ii) 4.5	×10 ⁹ year
Q.40 6.30×10 ⁻⁴ yr	-1 , 3.087 $\times 10^{-2}$ yr ⁻¹				
Exercise 2					
Nuclear Physics					
Single Correct Ch	oice Type				
Q.1 C	Q.2 B	Q.3 B	Q.4 A	Q.5 B	Q.6 A
Q.7 B	Q.8 B	Q.9 A	Q.10 A		
Radioactivity					
Single Correct Ch	oice Type				
Q.11 B	Q.12 C	Q.13 A	Q.14 B	Q.15 B	Q.16 B
Q.17 C	Q.18 A	Q.19 D	Q.20 A	Q.21 A	Q.22 C
Q.23 A	Q.24 C	Q.25 A	Q.26 C	Q.27 C	Q.28 B
Q.29 A	Q.30 B	Q.31 D			

Previous Years' Question

Q.1 . B	Q.2 C	Q.3 C	Q.5 C	Q.6 B	Q.7 A
Q.8 A	Q.9 125decays/sec	Q.10 Alpha=8, bet	ta=6	Q.11 24 Mev	Q.12 D
Q.13 B	Q.14 A	Q.15 D	Q.16 C	Q.17 B	Q.18 B
Q.19 B	Q.20 B	Q.21 D	Q.22 A	Q.23 A	Q.24 C

JEE Advanced/Boards

Exercise 1

Nuclear Physics

Q.2 (i) ${}^{40}_{19}$ K $\rightarrow {}^{40}_{18}$ Ar $+{}^{0}_{1}$ e + v (ii) 4.2×10^{9} years Q.1 23.6 Mev **Q.3** $t = \left(\frac{\ln 5}{\ln 2}\right)\tau$ **Q.4** 2.73×10¹⁸sec **Q.8** 1.7×10¹⁰ years **Q.9** 5196 yrs Q.10 28 Mev **Q.11** 9.00×10⁶ eV **Q.13** $\Delta T = \frac{0.2E_0 \left[\alpha t - \frac{\alpha}{\lambda} \left(1 - e^{-\lambda t} \right) \right]}{ms}$ **Q.12** v=-uλt Radioactivity **Q.14** t = 4.89×10^9 years **Q.15** $(T_{1/2} = 10.8 \text{ sec})$ **Q.17**²³⁹Pu=44.7%, ²⁴⁰Pu=55.3% **Q.16** 6 litre **Q.18** (a) $N = \frac{1}{\lambda} \left[\alpha \left(1 - e^{-\lambda t} \right) + \lambda N_0 e^{-\lambda t} \right]$ (b) $\frac{3N_0}{2}, 2N_0$ **Q.19** 0.833×10⁻⁵mol/lit sec **Q.20** t = 7.1×10^8 years **Q.21** 4.125 min **Q.22** (a) 1.143×10^9 year, (b) 7.097×10^8 year **0.23** 3.43×10⁻¹⁸ mol

Exercise 2

Nuclear Physics

Single Correct Choice Type					
Q.1 D	Q.2 D	Q.3 C	Q.4 B	Q.5 B	Q.6 D
Q.7 C	Q.8 B	Q.9 C	Q.10 A	Q.11 C	Q.12 B
Q.13 E	Q.14 C	Q.15 C	Q.16 B	Q.17 C	

Multiple Correct	Choice Type					
Q.18 A, B, D	Q.19 A, C	Q.20 C, D	Q.21 A, C	Q.22 B, C	Q.23 A, B, C	
Q.24 A, B, C	Q.25 C, D	Q.26 C, D	Q.27 B, C	Q.28 A, B, C	Q.29 A, D	
Q.30 D, E	Q.31 A, C, D					
Assertion Reasor	ning Type					
Q.32 D	Q.33 C	Q.34 A	Q.35 A			
Comprehension ⁻	Туре					
Q.36 B	Q.37 C	Q.38 B	Q.39 D			
Matric Match Ty	ре					
Q.40 A→q; B→p; 0	C→t; D→r; E→s					
Q.41 A→p, q; B→p	o, r; C→p, s; D→r, s					
Q.42 A→r; B→p; C	C→q; D→q					
Radioactivity						
Single Correct Ch	noice Type					
Q.43 D	Q.44 C	Q.45 C				
Multiple Correct Choice Type						
Q.46 A, B, C, D	Q.47 B, C, D	Q.48 C, D				
Comprehension ⁻	Туре					
Q.49 C	Q.50 C	Q.51 A	Q.52 D			

Previous Years' Questions

Q.1 3.96×10 ⁻⁶	Q.2 120.26 g	Q.3 1823.2 MeV	Q.4 V=5.95 L	Q.5 3.32×10^{-5} W
Q.7 $3.847 \times 10^4 \text{kg}$	Q.9 3.861	Q.10 8	Q.11 1	
Q.12 A \rightarrow p, q; B \rightarrow	\rightarrow p, r; C \rightarrow p, s; D \rightarrow	o, q, r	Q.13 D	Q.14 T = 1.4 × 10 ⁹ K
Q.15 B, D	Q.16 B	Q.17 A	Q.18 C	
Q.19 A \rightarrow r, t; B \rightarrow p	p, s; C \rightarrow p, q, r, t; D –	→ p, q, r, t	Q.20 9 MeV	Q.21 A
Q.22 A	Q.23 B	Q.24 C	Q.25 8	Q.26 C
Q.27 D	Q.28 A, C	Q.29 C	Q.30 A	Q.31 C
Q.32 B	Q.33 B	Q.34 B	Q.35 A	Q.36 C

Q.37 C

Solutions

JEE Main/Boards

Exercise 1

Sol 1:
$$t_{1/2} = \frac{\ln 2}{\lambda} = 10$$

 $\Rightarrow \lambda = \frac{\ln 2}{10} (days)^{-1}$
Now, $\frac{N}{N_0} = \frac{1}{50}$ and $N = N_0 e^{-\lambda t}$
 $\Rightarrow e^{-\lambda t} = \frac{1}{50} \Rightarrow \ln 50 = \lambda t$
 $\Rightarrow t = \frac{10 \times \ln 50}{\ln 2} = 56.44 \text{ days}$
Sol 2: $\lambda_1 = \frac{1}{1620}$ years⁻¹ and $\lambda_2 = \frac{1}{405}$ years⁻¹
Now, $\frac{dN}{dt} = -(\lambda_1 t + \lambda_2 t) \Rightarrow \frac{dN}{dt} = -(\lambda_1 + \lambda_2) t$
 $\Rightarrow N = N_0 \cdot e^{-\lambda} tot^{-t}$
So, $2t_{1/2} = \frac{2 \cdot \ln 2}{\lambda_{tot}} = \frac{2 \cdot \ln 2}{\frac{1}{1620} + \frac{1}{405}}$
 $= \frac{810 \cdot \ln 2}{1 + \frac{1}{4}} = \frac{4 \times 810 \cdot \ln 2}{5} = 449 \text{ years}$
Sol 3: $N = N_0 \cdot e^{-\lambda t}$
So in 1st 2 sec,
 $\Delta N_1 = N_0 \cdot - N_0 \cdot e^{-\lambda 2} = N_0 \cdot (1 - e^{-2\lambda})$
in other 2 sec,
 $\Delta N_2 = N_0 \cdot e^{-2\lambda} - N_0 \cdot e^{-4\lambda} = N_0 \cdot e^{-2\lambda} (1 - e^{-2\lambda})$
Now, $\frac{N_0 \cdot (1 - e^{-2\lambda})}{N_0 \cdot e^{-2\lambda} \cdot (1 - e^{-2\lambda})} = \frac{n}{0.75n} = \frac{4}{3}$
 $\Rightarrow \frac{3}{4} = e^{-2\lambda}$
 $\Rightarrow e^{2\lambda} = \frac{4}{3}$

 $\Rightarrow 2\lambda = 2\ln 2 - \ln 3$ $\Rightarrow \lambda = (\ln 2 - (\ln 3)/2) \sec^{-1}$ Now mean life

$$= \frac{1}{\lambda} = \left[\frac{1}{\ln 2 - \frac{(\ln 3)}{2}}\right] \operatorname{sec}$$
$$= \left[\frac{1}{0.6931 - \frac{(1.0986)}{2}}\right] = 6.9 \approx 7 \operatorname{sec}$$

Sol 4: (a)
$$\frac{dN}{dt} = \alpha - \lambda N \Rightarrow \frac{dN}{dt} + IN = a$$

 $\Rightarrow \int d \left[N.e^{\lambda t} \right] = \int \left[\alpha.e^{\lambda t} \right] \cdot dt$
 $\Rightarrow \left[N.e^{\lambda t} \right]_{0}^{t} = \left[\alpha.e^{\lambda t} \right]_{0}^{t} / \lambda$
 $\Rightarrow N \cdot e^{\lambda t} - N_{0} = (\alpha \cdot e^{\lambda t} - \alpha) / \lambda$
 $\Rightarrow N = N_{0} \cdot e^{-\lambda t} + \frac{\alpha}{\lambda} (1 - e^{-\lambda t})$
(B) $\alpha = 2N_{0}I$
After one half life, $\left[t_{1/2} = \frac{In2}{2} \right]$

After one name,
$$\frac{t_{1/2} - \frac{1}{\lambda}}{\sum_{\lambda}}$$

So, t = $\frac{\ln 2}{\lambda}$
N = N₀. e^{-ln2} + $\frac{\alpha}{\lambda}$. (1 - e^{-ln2})
= $\frac{N_0}{2} + \frac{\alpha}{\lambda}$. (1 - 1/2)
 $\boxed{N = \frac{N_0}{2} + \frac{\alpha}{2\lambda} = \left(N_0 + \frac{\alpha}{\lambda}\right) \times \frac{1}{2}}$
Now, as t $\rightarrow \infty$,

$$N = N_0(0) + \frac{\alpha}{\lambda}(1-0) \Rightarrow \boxed{N = \frac{\alpha}{\lambda}}$$

Sol 5:
$$_{84}Po^{210} \longrightarrow _{2}\alpha^{4} + _{82}Pb^{206}$$

So, $t_{1/2} = \frac{\ln 2}{\lambda} = 138.6$ days

$$\Rightarrow \lambda = \frac{\ln 2}{138.6} \text{ (days)}^{-1}$$
Now, Mass defect
= 209.98264 - (205.97440 + 4.00260)
= 0.00564 amu
= 5.251 MeV.
1.6 × 10⁻¹⁹ J = 1 eV
So, Mass defect = 1.6 × 10⁻¹⁹ × 10⁶ × 5.251
= 8.4 × 10⁻¹³ J
So to produce 1.2 × 10⁷ J energy (at 0.1 efficiency)
Number of reactions

 $8.4 \times 10^{-13} \pi \left(\frac{dN}{dt}\right) \times 0.1 = 1.2 \times 10^{7}$ $\Rightarrow \left(\frac{dN}{dt}\right) = \frac{1.2}{8.4} \times 10^{21} = \frac{1}{7} \times 10^{21}$ Now, $\frac{dN}{dt} = \lambda N = \frac{1}{7} \times 10^{21}$ $\Rightarrow \lambda N_{0} e^{-\lambda t} = \frac{1}{7} \times 10^{21}$ $\Rightarrow N_{0} = \frac{1}{7} \times 10^{21} \times e^{\lambda t} \cdot \frac{1}{\lambda}$ $= \frac{1}{7} \times 10^{21} \times \left(e^{\frac{\ln 2}{138.6} \times 693}\right) \times \frac{1}{\ln 2} \times 138.6$ $= 28.56 \times 32 \times 10^{21}$ $N_{0} = 9.13 \times 10^{23}$

Now, number of moles = $\frac{N_o}{6 \times 10^{23}}$ = 1.52

So mass = $1.52 \times 210 \text{ gm} = 319.2 \text{ gm}$ Initial activity = λN_0

$$= \frac{\ln 2}{138.6} \times 9.13 \times 10^{23} = 4.6 \times 10^{21} \, \text{days}^{-1}$$

Sol 6: Energy per fission = 200 MeV

- $= 200 \times 10^{6} \, \text{eV}$
- $= 200 \times 10^{6} \, \text{eV}$

$$= 200 \times 10^6 \times 1.6 \times 10^{-19} \text{ J}$$

Now, number of fissions required / time

$$= \frac{1 \times 10^6}{3.2 \times 10^{-11}} = \frac{10}{3.2} \times 10^{18}$$

= 3.125×10^{16} fissions Number of fissions in 1 year = $3.125 \times 10^{16} \times 365 \times 24 \times 60 \times 60$ = 9.855×10^{23} Moles of uranium required = 1.637 moles Mass of Uranium = 384.5 g

Now higher the BE/nucleon higher the stability.

So light nuclei try to get high $\frac{BE}{Nucleon}$ ratio by going through nuclear fusion and hence increasing their atomic number.

Sol 8: Now number of particles decaying is directly proportional to the number of particles present in the reaction.

i.e.
$$\frac{dN}{dt} \propto N$$

 \Rightarrow This is equated by a constant known as decaying constant.

$$\frac{dN}{dt} = \lambda N$$

(i) X-rays and gamma rays both electromagnetic.

(ii) γ-rays

(iii) γ-rays

(iv) β -rays (Both (–) ve)

Sol 9: Mass defect $m\binom{6}{3}Li + m\binom{1}{0}n - \left[m\binom{4}{2}H + m\binom{3}{1}H\right]$ $\Rightarrow (6.015126 + 1.008665)$

- (4.002604 + 3.016049)

= 0.010697 amu = 9.96 MeV

Sol 10: n/p ratio decreases due to beta decay.

i.e.
$$_{_6}C^{_{14}} \longrightarrow _{_7}N^{_{14}} + \beta^{_{-1}} + \overline{\nu}$$

$$\Rightarrow \frac{n}{p} = \frac{8}{6} = \frac{4}{3}, |\frac{n}{p} = \frac{7}{7} = 1$$

Sol 11: Decay constant refer ans. 8

Half-life period: the time taken by a disintegration reaction to half the total number of particles in a sample.

Sol 12: Mass defect = 2.0141 + 6.0155 - 2x (4.0026)

= 0.0244 m

So energy transferred to KE

= (0.0244) × 931 MeV

= 22.7164 MeV

So energy for each particle

$$= \frac{22.7164}{2} = 11.36 \text{ MeV}$$
$$= 11.36 \times 1.6 \times 10^{-19} \times 10^{6}$$

 $= 18.176 \times 10^{-13} = 1.8176 \times 10^{-12} \text{ J}$

Sol 13: Number of moles =
$$\frac{2.2 \times 10^{-3}}{11}$$

= 0.2 × 10⁻³ = 0.2 × 10⁻⁴ moles
(i) Number of moles × A₀ = Number of particles
= 6.0022 × 10²³ × 2 × 10⁻⁴
= 12.044 × 10¹⁹
(ii) Activity = $\lambda N = \frac{dN}{dt}$
So = $\frac{\lambda}{1224} \times \frac{5 \times 10^{-6}}{11} \times 6 \times 10^{23} = 1.54 \times 10^{14}$

Sol 14: Half-life period: sec

Decay constant
$$\Rightarrow$$
 sec⁻¹ - $\frac{dN}{dt} = 4 N \times \lambda$
 $\Rightarrow N = N_0 \cdot e^{-\lambda t}$
Now, $N = N_0 / 2$
 $\Rightarrow e^{\lambda t_{1/2}} = 2$
 $\Rightarrow \lambda t_{1/2} = \ln 2$
 $\Rightarrow t_{1/2} = \frac{\ln 2}{\lambda}$

Sol 15: (i)
$${}_{3}^{6}\text{Li} + {}_{0}^{1}\text{n} \rightarrow {}_{2}^{4}\alpha + \text{triton}$$

(ii) Mass defect

= mass before reaction – mass after reaction
=[(6.015126) + (1.0086554)] – [4.0026044 + 3.0100000]
= 0.011177 m
So energy released = 0.011177 × 931 MeV
= 10.405 MeV

Sol 16: Activity = rate of change of number of particles in a disintegration reaction.

SI unit
$$\Rightarrow \frac{dN}{dt}$$

 \Rightarrow SI Unit = sec⁻¹





(ii) For $r > r_0$ Attraction

(iii) For $r < r_0$ Repulsion

Sol 18: Refer Q.7

Mass defect = $20 \times \text{mass}$ of proton + $20 \times \text{mass}$ of neutron – [mass of $\frac{40}{20}$ Ca]

= 20×[1.0007825 + 1.008665] - 39.962589

So, energy = (Δmc^2)

$$= 0.226361 \times \frac{931}{c^2} \text{MeV} \times c^2$$

Sol 19: (a) Nuclear forces are short-ranged. They are most effective only up to a distance of the order of a femtometre or less.

(b) Nuclear forces are much stronger than electromagnetic forces.

(c) Nuclear forces are independent of charge.

Sol 20: Mass defect = - [mass of $\frac{234}{90}$ Th

+ mass of
$${}^{4}_{2}$$
He] + mass of ${}^{238}_{92}$ U

= 0.00456 u

So energy released = 0.00456×931.5 MeV = 4.25 MeV

Sol 21: Radius =
$$R_0[A]^{1/3}$$

So, $\frac{R_1}{R_2} = \frac{[A_1]^{1/3}}{[A_2]^{1/3}} \Rightarrow \frac{R_1}{R_2} = \left[\frac{1}{8}\right]^{1/3}$
 $\boxed{\frac{R_1}{R_2} = \frac{1}{2}}$

Sol 22: (a) It is because of the fact that the binding energy of the particle has to be (+) ve. [i.e. every system tries to minimise its energy] some of its mass is converted into energy.

Sol 23: For stability, binding energy/nucleon should be high. Since it is highest at some intermediate atomic number, the elements with large atomic number try to increase the binding energy/nucleon by fission. Similarly elements with small atomic number tries to increase B.E./nucleon using fusion.

Sol 24: Refer Q.16



Sol 25: For A > 30, the stability of the nucleus increases as more and more nucleons are introduced because of minimization of potential energy. Because of this, initially the B.E./nucleon increases.

But at high mass number, the size of the nucleus starts to increase and because of this, as the nucleons are weaker for larger distance, the electrostatic repulsion between the protons starts to dominate over them and thus on further increase in the mass number (the nucleus starts to become unstable).

Radioactivity

Sol 26: For same atomic No.

If mass No. of an isotope > mass no. of most stable isotope

Then isotope is a beta emitter \rightarrow n/p ratio increases otherwise positron emitter \rightarrow n/p ratio decreases

 $^{49}_{20}$ Ca; $^{30}_{13}$ Al; $^{94}_{36}$ Cr \rightarrow beta emitter

Sol 27: Odd no. of neutrons

Sol 28: (a)
$${}_{7}^{14}N + {}_{2}^{4}He \rightarrow {}_{8}^{17}O + {}_{1}^{1}H$$

(b) ${}_{2}^{4}Be + {}_{2}^{4}He \rightarrow {}_{6}^{12}C + {}_{0}^{1}n$
(c) ${}_{9}^{9}Be (p, \alpha) \rightarrow {}_{3}^{6}L_{i} + {}_{2}^{4}He + {}_{1}^{0}P$
(d) ${}_{15}^{30}P \rightarrow {}_{14}^{30}S + {}_{+1}^{0}e$
(e) ${}_{1}^{3}H \rightarrow {}_{2}^{3}He + {}_{-1}^{0}e$
(f) ${}_{20}^{43}Ca + {}_{2}^{4}He \rightarrow {}_{21}^{46}Sc + {}_{1}^{1}P$
Sol 29: ${}_{1/2} = {}_{2}\times 3600 s$
 $t_{1/2} = 1200 sec$
 $t_{1/2} = {}_{1}1200 sec$
 $t_{1/2} = {}_{1}1200 sec^{-1}$
 $\lambda = 5.775 \times 10^{-4} sec^{-1}$
 $\lambda = 2.079 hr^{-1}$

Sol 30: n =
$$\frac{40}{12.3}$$
 = 3.252

No. of atoms =
$$\frac{\frac{10}{1} \times N_A \times 8 \times 10^{-18}}{2^{3.252}}$$

 $= 5.05 \times 10^{6}$ atoms.

Sol 31: % of radiation = $100 \times \frac{1}{2^4}$ % =6.25%

Sol 32: $k = \frac{0.693}{t_{\frac{1}{2}}}$ $t_{\underline{1}} = 30 \text{ days}$ $k = \frac{0.693}{30 \times 24 \times 60 \times 60} \text{ sec}^{-1}$ As N = 10^{11} atoms $-\frac{dN}{dt} = kN$ $-\frac{dN}{dt} = \frac{0.693 \times 10^{11}}{30 \times 24 \times 60 \times 60} \text{ sec}^{-1}$ $= 2.67 \times 10^{5} \text{ sec}^{-1}$ **Sol 33:** $\frac{1}{2^{\frac{t}{1/2}}} = \frac{15}{100}$ $\Rightarrow 2^{\frac{t}{t_{1/2}}} = \frac{100}{15}$ $\frac{t}{t} = \frac{\ln\left(\frac{100}{15}\right)}{\ln 2}$ $t = \frac{t_{1/2} \times \ln\left(\frac{100}{15}\right)}{\ln 2}$ t = 33.66 yrs **Sol 34:** $t_{1/2} = 1.4 \times 10^9$ Nuclear reaction: -

(i) ${}^{40}_{10}K \rightarrow {}^{40}_{18}Ar + {}^{0}_{1}e + v$ (ii) Age = $2t_{1/2} = 2.8 \times 10^{18}$ years **Sol 35:** t_{1/2} = 10 sec

(i) $t_{mean} = 1.443 \times t_{1/2} = 14.43 \text{ sec}$ (ii) $2^n = \frac{100}{6.25}$ $2^n = 16$ n = 4 $t = 4 t_{1/2} = 40 sec$

Sol 36: ${}^{2}_{1}H + {}^{2}_{1}H \rightarrow {}^{3}_{2}He + {}^{1}_{0}n$ $\Delta m = 2 \times 2.020 - (3.0160 + 1.0087)$ ∆m = 0.0153 amu $\Delta m = \frac{0.0153 \times 10^{-3}}{6.022 \times 10^{23}} = 2.54 \times 10^{-29} \text{ kg}$ $E = \Delta m \times c^2 = 2.28 \times 10^{-12} J$ $\mathsf{E} = \frac{2.28 \times 10^{-12}}{1.6 \times 10^{-19}}$ E = 14.25 MeV **Sol 37:** (a) $_{_{92}}U^{_{238}} \rightarrow _{_{82}}Pb^{_{206}} + 8 {}^4_{_2}He + 6 {}^0_{_{-1}}e$ α -Particles = 8 β -Particles = 6 (b) $_{90}Th^{234} \rightarrow {}^{206}_{82}Pb + 7 {}^{4}_{2}He + 6 {}^{0}_{-1}e$ **Sol 38:** Remains of $Sr^{40} = 1 \times 10^{-6} \times 2^{\frac{20}{28.1}}$ = 0.613 mg**Sol 39:** (i) ${}_{84}Po^{210} \rightarrow {}_{82}Pb^{206} + {}_{2}^{4}He$ Moles of helium produced = $\left(1 - \frac{1}{2}\right) \times \frac{1}{210}$ $V = \frac{nRT}{P} = \frac{\left(1 - \frac{1}{\sqrt{2}}\right) \times \frac{1}{210} \times 8.314 \times 273}{1.01325 \times 10^5} = 31.25 \text{ cm}^3$ (ii) V' = $\frac{V \times m_{PoO_2}}{m_{Po}}$ = 27.104 cm³ (iii) $U^{238} t_{1/2} = 4.5 \times 10^9 \text{ yrs}$ -0.1 mole U²³⁸ 0.1 mole Pb²⁰⁶ Age of ore = $t_{1/2} = 4.5 \times 10^9$ yr. **Sol 40:** $\lambda = \lambda_1 + \lambda_2$; $\lambda_1 + \lambda_2 = \frac{\ln 2}{t_{1/2}}$

$$\lambda_{1} + \lambda_{2} = \frac{\ln 2}{22}; \lambda_{1} = \frac{1}{49}\lambda_{2}$$
$$\lambda_{1} = \frac{\ln 2}{22 \times 50} = 6.301 \times 10^{-4} \text{ year}^{-1}$$
$$\lambda_{2} = \frac{49 \times \ln 2}{22 \times 50} = 3.087 \times 10^{-2} \text{ year}^{-1}$$

$$\lambda_2 = \frac{1}{22 \times 50}$$

Exercise 2

Single Correct Choice Type

Sol 1: (C) Carbon-12 is taken as standard

Sol 2: (B) $R = R_0 \cdot A^{1/3}$

Sol 3: (B) 0

Energy released

= (8.2 × 90 + 8.2 × 110 - 7.4 × 200) MeV = (0.8 × 200) MeV = 160 MeV

Sol 4: (A) Energy = (7.5 × 13 – 12 × 7.68) MeV = 5.34 MeV

Sol 5: (B) $2X \rightarrow Y + Q$

Binding energy is the (-) ve energy

From energy conservation

 $-2E_1 = -E_2 + Q \Longrightarrow Q = E_2 - 2E_1$

Sol 6: (A) We know that half life is given as

 $T = \frac{0.693}{\lambda}$ Given that $\lambda' = 1:2$ $\therefore \frac{T}{T'} = \frac{\lambda'}{\lambda} = \frac{2}{1}$

Thus, for probabilities of getting α and β particles at the same time t = 0, the ratio will be the same 2 : 1

Sol 7: (B) Half-life = 5 years, time given = 10 years = 2 half-lives

$$\frac{N}{N_0} = \left(\frac{1}{2}\right)^n$$
Or N = $\left(\frac{1}{2}\right)^2 N_0$

Or N =
$$\frac{1}{4}$$
 N₀ = 0.25 N₀

 \therefore 25% substance left hence probability of decay

= 100 - 25 = 75%

Sol 8: (B)
$$\lambda = \frac{\ln 2}{t_{1/2}} = \frac{\ln 2}{1620}$$
 (years)⁻¹

$$= \frac{\ln 2}{1620 \times 365 \times 24}$$
 (hours)⁻¹
Now, N = N₀.e^{- λ t}
where N₀ = $\frac{5}{223} \times 6.022 \times 10^{23}$
So N = N₀.e^{- λ ×5}
So decayed particles
= N₀ - N = N₀(1 - e^{- λ 5})
= $\frac{5}{223} \times 6.022 \times 10^{23} \left[1 - e^{-\frac{5\ln 2}{1620 \times 365 \times 24}} \right]$
= 3.29 × 10¹⁵

Sol 9: (A) The end product of radioactive series is stable and hence the decay constant is zero.

Sol 10: (A) (A) (A) (
$$\lambda_2$$
)
Now, $\frac{dN}{dt} = -(\lambda_1 N + \lambda_2 N)$
 $\Rightarrow \frac{dN}{dt} = -(\lambda_1 + \lambda_2)N.$

Radioactivity

Single Correct Choice Type

Sol 11: (B)
$$^{29}_{13}$$
Al $\rightarrow ^{27}_{13}$ Al $+ 2^{1}_{1}$ n $+ 2^{0}_{-1}$ B

Sol 12: (C)
$${}^{1}_{0}n \rightarrow {}^{1}_{1}p + {}^{0}_{-1}\beta$$

Sol 13: (A)
$$\frac{N_1}{N_2} = \frac{A_1}{A_2} = \frac{e^{-10\lambda_0 t}}{e^{-\lambda_0 t}} = \frac{e^{-10/9}}{e^{-1/9}} = e^{-1}$$

Sol 14: (B) m =
$$\frac{256}{2^6}$$
 g = 4g

$$\frac{k_1 e^{-k_1 t}}{(k_2 - k_1)} = \frac{k_2 e^{-k_2 t}}{(k_2 - k_1)} \ ; \frac{k_1}{k_2} = e^{(k_1 - k_2)t}$$

$$t_{max.} = \frac{\ln\left(\frac{k_1}{k_2}\right)}{(k_1 - k_2)} = \frac{\ln(k_2 / k_1)}{(k_2 - k_1)}$$

Sol 15: (B) Reaction need not be exothermic.

Sol 16: (B) ${}^{238}_{92}M \rightarrow {}^{x}_{y}N + 2 {}^{4}_{2}He; {}^{x}_{y}N \rightarrow {}^{A}_{B}L + 2{}^{0}_{1}\beta^{+}$ X = 230 A = 230 Y = 88 B = 86 Neutrons = 230 - 86 = 144

Sol 17: (C) m = $\frac{200}{2^6} = \frac{200}{64} = 3.125$ g

- **Sol 18: (A)** 4 ${}^{4}_{2}$ He $\rightarrow {}^{16}_{8}$ O
- $\Delta m = 4 \times 4.0026 15.834$
- = 16.0104 15.834 = 0.1764 amu
- B.E. per nucleon
- $=\frac{1}{16} \times 0.1764 \times 931 \text{MeV} = 10.24 \text{ MeV}$
- Sol 19: (D) $\frac{1}{2n} \le \frac{1}{10}$ $2^{t/30} \ge 10$ $\Rightarrow t/30 \ge \log_2 10$ $\Rightarrow t \ge \frac{30 \ln 10}{\ln 2}$ $\Rightarrow t \ge 99.65 \approx 100$

Sol 20: (A) ${}^{a}_{b}X \rightarrow {}^{a-1}_{b}X + {}^{1}_{0}n$

Sol 21: (A) (i) $t_{1/2x} = \frac{t_{1/2y}}{\ln 2}$ $t_{1/2x} > t_{1/2y}$ \therefore Y Decays faster. (ii) True (iii) $4t_{1/2} = 400 \ \mu s$ (iv) $v \propto m$ (v) No. of disintegrated nucleus = $\frac{3}{4} N_0$ Probability = $\frac{3}{4}$

Sol 22: (C)
$$R = \frac{dN}{dt} = -\lambda N$$

 $I = \frac{ln2}{t_{1/2}}; \frac{\lambda_1}{\lambda_2} = \frac{t_{1/2}}{t_{1/2_1}} = 2$
 $\frac{N_1}{N_2} = \frac{N/2}{N/\sqrt{2}}$
 $\frac{R_1}{R_2} = \frac{\lambda_1 N_1}{\lambda_2 N_2} = 2 \times \frac{1}{\sqrt{2}} = \sqrt{2}$

Sol 23: (A)
$$\frac{m}{t_{1/2}} \times N = \frac{1}{60}$$

 $\frac{\ln 2}{t_{1/2}} \times 6.022 \times 10^{23} \times 1.3 \times 10^{-12} = 3$
 $t_{1/2} = \frac{6.022 \times 1.3 \times \ln 2}{3} \times 10^{-11}$
 $= 1.808 \times 10^{11} = 0.18 \times 10^{-12} \text{ sec}$

Sol 24: (C) In a γ decay energy of atom is reduced, atomic mass and atomic number remains the same.

Sol 25: (A) 1 fm << radius of atom \therefore Repulsive forces dominate. $F_{pp} > F_{pn} = F_{nn}$ F_{pn} and F_{nn} would be negligible compared to repulsive forces of protons. **Sol 26:** (C) A $\xrightarrow{\lambda_1}$ B $\lambda_1 = 1.8 \times 10^{-2} \text{ sec}^{-1}$ $2A \xrightarrow{\lambda_2}$ C $\lambda_2 = 10^{-3} \text{ sec}^{-1}$ $\lambda = \lambda_1 + 2\lambda_2 = 18 \times 10^{-3} + 2 \times 10^{-3}$ $= 2 \times 10^{-2}$ $t_{mean} = \frac{1}{\lambda} = \frac{1}{2 \times 10^{-2}} = 50 \text{ sec}$

Sol 27: (C) Initially, N_B = 8N_A Finally, N'_A = 2N'_B $\frac{N_A}{N'_A} = 2^{t/50} \frac{N_B}{N'_B} = 2^{t/10}$ $\frac{8N_A}{N'_A} = \frac{N_B}{2N'_B}$ $16 \times 2^{t/50} = 2^{t/10}$

$$2^{\frac{t}{50}+4} = 2^{\frac{t}{10}} \Rightarrow \frac{t}{50} - \frac{t}{10} = -4$$

$$\frac{4t}{50} = 40 \Rightarrow t = 50 \text{ min}$$

Sol 28: (B) A = $10^4 \times \frac{60 \times 10^3}{10}$
= $6 \times 10^7 \text{ dis/min} = 10^6 \text{ dps}$
Activity = $\frac{10^6}{3.7 \times 10^{10}}$ Curie = 27 µCi

Sol 29: (A) Age = t_{1/2}

Sol 30: (B) $t_{1/2} = 69.3$ min. $\lambda = \frac{0.693}{69.3} = \min^{-1} = \frac{1}{100} \min^{-1}$

 $\lambda N = 10; N = 10/\lambda = 1000$ atoms

Sol 31: (D)
$$R_1 = \lambda N_1$$

Atoms disintegrated = $(N_1 - N_2)$

 $= \left(\frac{\mathsf{R}_1 - \mathsf{R}_2}{\lambda}\right) = \left(\frac{\mathsf{R}_1 - \mathsf{R}_2}{\ln 2}\right) \mathsf{T}$

Previous Years' Questions

Sol 1: (B) Using $N = N_0 e^{-\lambda t}$

where
$$\lambda = \frac{\ln 2}{t_{1/2}} = \frac{\ln(2)}{3.8} \therefore \frac{N_0}{20} = N_0 e^{-\frac{\ln(2)}{3.8}t}$$

Solving this equation with the help of given data we find: t = 16.5 days

Sol 2: (C) Beta particles are fast moving electrons which are emitted by the nucleus.

Sol 3: (C) During fusion process two or more lighter nuclei combine to form a heavy nucleus.

Sol 4: Following nuclear reaction takes place

 $_{0}n^{1} \rightarrow _{1}H^{1} + _{-1}e^{0} + \overline{\nu}$ $\overline{\nu}$ is antineutrino

Sol 5: (C) The given reaction are :

 $_{1}H^{2} + _{1}H^{2} \rightarrow _{1}H^{3} + p$

 $_{1}H^{2} + _{1}H^{3} \rightarrow _{2}He^{4} + n$ $3_{1}H^{2} \rightarrow _{2}He^{4} + n + p$ Mass defect $\Delta m = (3 \times 2.014 - 4.001 - 1.007 - 1.008)$ amu = 0.026 amu Energy released $= 0.026 \times 931$ MeV $= 0.026 \times 931 \times 1.6 \times 10^{-13}$ J $= 3.87 \times 10^{-12}$ J

This is the energy produced by the consumption of three deuteron atoms.

 \therefore Total energy released by 10⁴⁰ deuterons

$$= \frac{10^{40}}{3} \times 3.87 \times 10^{-12} \text{ J}$$
$$= 1.29 \times 10^{28} \text{ J}$$

The average power radiated is $P = 10^{16}$ W or 10^{16} J/s

Therefore, total time to exhaust all deuterons of the star will be

$$t = \frac{1.29 \times 10^{28}}{10^{16}} = 1.29 \times 10^{12} \text{ s} \approx 10^{12} \text{ s}$$

Sol 6: (B) Heavy water is used as moderators in nuclear reactors to slow down the neutrons.

Sol 7: (A) Penetrating power is maximum for γ -rays, then of β -particles and then α -particles because basically it depends on the velocity. However, ionization power is in reverse order.

Sol 8: (A) Activity of
$$S_1 = \frac{1}{2}$$
 (activity of S_2)
or $\lambda_1 N_1 = \frac{1}{2} (\lambda_2 N_2)$ or $\frac{\lambda_1}{\lambda_2} = \frac{N_2}{2N_1}$
or $\frac{T_1}{T_2} = \frac{2N_1}{N_2}$ (T = half-life= $\frac{\ln 2}{\lambda}$)
Given $N_1 = 2N_2 \therefore \frac{T_1}{T_2} = 4$
 \therefore Correct option is (A).

Sol 9:
$$R = R_0 \left(\frac{1}{2}\right)^n$$

Here R_0 = initial activity =1000 disintegration/s and n = number of half-lives.

$$\therefore R = 10^{3} \left(\frac{1}{2}\right) = 500 \text{ disintegration/s}$$

At t = 3s, n = 3
$$R = 10^{3} \left(\frac{1}{2}\right)^{3} = 125 \text{ disintegration/s}$$

Sol 10: Number of α -particles emitted

$$n_1 = \frac{238 - 206}{4} = 8$$

and number of β -particles emitted are say n₂, then 92 - 8 × 2 + n₂ = 82

$$\therefore$$
 n₂ = 6

Sol 11: Q = (Δ m in atomic mass unit) × 931.4 MeV = (2 × mass of $_1$ H² – mass of $_2$ He⁴) × 931.4 MeV

= (2 × 2.0141 – 4.0024) × 931.4 MeV

 $Q\approx 24~MeV$

Sol 12: (D) Binding energy per nucleon increases for lighter nuclei and decreases for heavy nuclei.

Sol 13: (B) $\frac{k}{r} = \frac{mv^2}{r}$

 $mv^2 = k$ (independent or r)

 $n\left(\frac{h}{2\pi}\right) = mvr \Rightarrow r \propto n$ and $T = \frac{1}{2}mv^2$ is independent of n.

Sol 14: (A) 1^{st} reaction is fusion and 4^{th} reaction is fission.

Sol 15: (D) IR corresponds to least value of $\left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right)$

i.e. from Paschen, Bracket and Pfund series. Thus the transition corresponds to $5 \rightarrow 3$.

Sol 16: (C) After decay, the daughter nuclei will be more stable hence binding energy per nucleon will be more than that of their parent nucleus.

Sol 17: (B) Conserving the momentum $0 = \frac{M}{2}V_1 - \frac{M}{2}V_2$

$$V_1 = V_2 \qquad \qquad \dots (i)$$

$$\Delta mc^{2} = \frac{1}{2} \cdot \frac{M}{2} V_{1}^{2} + \frac{1}{2} \cdot \frac{M}{2} \cdot V_{2}^{2} \qquad \dots (ii)$$

$$\Delta mc^{2} = \frac{M}{2}V_{1}^{2}$$
$$\frac{2\Delta mc^{2}}{M} = V_{1}^{2}$$
$$V_{1} = c\sqrt{\frac{2\Delta m}{M}}$$

Sol 18: (B) In positive beta decay a proton is transformed into a neutron and a positron is emitted.

$$p^+ \rightarrow n^0 + e^+$$

no. of neutrons initially was A - Z

no. of neutrons after decay $(A - Z) - 3 \times 2$ (due to alpha particles) + 2 x 1 (due to positive beta decay)

The no. of proton will reduce by 8. [as 3×2 (due to alpha particles) + 2(due to positive beta decay)]

Hence atomic number reduces by 8.

Sol 19: (B)
$$E_n = -13.6 \frac{Z^2}{n^2}$$

 $E_{Li^{++}} = -13.6 \times \frac{9}{1} = -122.4 \text{eV}$
 $E_{Li^{+++}} = -13.6 \times \frac{9}{9} = -13.6 \text{eV}$
 $\Delta E = -13.6 - (-122.4)$
= 108.8 eV

Sol 20: (B)
$$t_{\frac{1}{2}} = 20 \text{ minutes}$$

 $N = N_0 e^{-\lambda t_2} \lambda t_1 = \ln 3$
 $\frac{2}{3} N_0 = N_0 e^{-\lambda t_2} t_1 = \frac{1}{\lambda} \ln 3$
 $\frac{2}{3} N_0 = N_0 e^{-\lambda t_2}$
 $t_2 = \frac{1}{\lambda} \ln \frac{3}{2}$
 $t_2 - t_1 = \frac{1}{\lambda} \left[\ln \frac{3}{2} - \ln 3 \right] = \frac{1}{\lambda} \ln \left[\frac{1}{2} \right] = \frac{0.693}{\lambda} = 20 \text{ min}$

Sol 21: (D) Number of spectral lines from a state n to ground state is $=\frac{n(n-1)}{2}=6$

Sol 22: (A)
$$\Delta m(m_p + m_e) - m_n = 9 \times 10^{-31} \text{ kg}$$

Energy released = $(9 \times 10^{-31} \text{ kg})c^2$ joules

$$= \frac{9 \times 10^{-31} \times (3 \times 10^8)^2}{1.6 \times 10^{-13}} \text{MeV} = 0.73 \text{ MeV.}$$

Sol 23: (A) KE $\propto \left(\frac{Z}{n}\right)^2$ as n decreases KE increases and TE, PE decreases

Sol 24: (C)

А

 $T_{A} = 20 \text{ min}$ $T_{B} = 40 \text{ min}$

В

$$\frac{\left(1-\frac{N}{N_0}\right)_A}{\left(1-\frac{N}{N_0}\right)_B} = \frac{1-\frac{1}{2^{t/t_{1/2}}}}{1-\frac{1}{2^{t/t_{1/2}}}} = \frac{1-\frac{1}{2\frac{80}{20}}}{1-\frac{1}{2\frac{80}{40}}} = \frac{1-\frac{1}{16}}{1-\frac{1}{4}} = \frac{\frac{15}{16}}{\frac{3}{4}} = \frac{5}{4}$$

JEE Advanced/Boards

Exercise 1

Sol 1:
$$_{1}H^{2} + _{1}H^{2} \longrightarrow _{2}He^{4}$$

Binding energy of deuteron = (1. 1) × 2 MeV = 2.2 MeV

Binding energy of helium

 $= {}_{2}\text{He}^{4} = 7 \times 4$

= 28 MeV

So total energy released

= 28 - 2.2 × 2 = 28 - 4.4

= 23.6 MeV

Sol 2: (i) ${}^{40}_{19}K \rightarrow {}^{40}_{18}Ar + {}^{0}_{+1}e + v$ (ii) 4.2×10^9 years

Sol 3: $\frac{dN}{dt} = R - \lambda N$ $\frac{dN}{dt} + \lambda N = R$ $\Rightarrow \int_{0,0}^{N,t} d(N.e^{\lambda t}) = \int_{0}^{t} R.e^{\lambda t}.dt$ N. $e^{\lambda t} = \frac{R}{\lambda} \cdot [e^{\lambda t} - 1]$ $\Rightarrow N = \frac{R}{\lambda} [1 - e^{-\lambda t}]$ d So for eq. as $t \to \infty$, $N \to R/\lambda$, So for N = 0.8 R/I $0.8 \frac{R}{\lambda} = \frac{R}{\lambda} [1 - e^{-\lambda t}]$ $\Rightarrow \frac{4}{5} = 1 - e^{-\lambda t} \Rightarrow \frac{1}{5} = e^{-\lambda t}$ $\Rightarrow \lambda t = \ln 5$ $\Rightarrow \frac{\ln 5}{\lambda}$ and give, $\lambda = \frac{\ln 2}{\tau} \Rightarrow t = \frac{\ln 5}{\ln 2} \times \tau$

Sol 4: 4 hydrogen atom produces 26 MeV energy. \Rightarrow 4g (4 moles) hydrogen atom produces \Rightarrow [26 × 6.022×10²³] MeV(energy) $= 26 \times 6.022 \times 10^{23} \times 1.6 \times 10^{-19} \times 10^{6}$ Joule $= 26 \times 6.022 \times 1.6 \times 10^{10}$ Joule = 250.51 × 10¹⁰ Joules \Rightarrow 1.7 × 10³⁰ kg = 1.7 × 10³³ g H produces $= \frac{250.51 \times 10^{10}}{4} \times 1.7 \times 10^{33}$ $=\frac{250.51\times1.7}{4}\times10^{43}$ Joules $= 1.065 \times 10^{45}$ Joules Now power × time = total energy \Rightarrow time = $\frac{1.065 \times 10^{45}}{3.9 \times 10^{26}}$ = 2.73 × 10¹⁸ sec **Sol 5:** We have, $N = N_0 \cdot e^{-\lambda t}$ So, $N_{U_{225}} = N_0 \cdot e^{-\lambda_1 t}$ $N_{U_{238}} = N_0 \cdot e^{-\lambda_2 t}$ $\frac{N_{U_{238}}}{N_{U_{235}}} = e^{(\lambda_1 - \lambda_2)t}$ Given $\frac{140}{1} = e^{(\lambda_1 - \lambda_2)t}$ $\Rightarrow \ln 140 = (\lambda_1 - \lambda_2) \times t$

$$\Rightarrow t = \frac{\ln 140}{\lambda_1 - \lambda_2}$$

Now, $\lambda_1 = \frac{\ln 2}{7.13 \times 10^8}$, $\lambda_2 = \frac{\ln 2}{4.5 \times 10^9}$
So $t = \frac{\ln 140}{\ln 2 \left[\frac{1}{7.3 \times 10^8} - \frac{1}{4.5 \times 10^9}\right]}$ years

$$= \frac{\ln 140}{\ln 2 \left[\frac{10}{7.3} - \frac{1}{4.5} \right]} \times 10^9 \text{ years} = 6.21 \times 10^9 \text{ years}$$

Sol 6: Now, as the momentum of the nucleus and α -particle are same (momentum conservation)

Energy = $\frac{P^2}{2m}$, is divided in the inverse ratio of their

respective masses.

So, let the energy of nucleus after disintegration be K, then

$$\frac{4.78}{K} = \frac{222}{4} = \frac{111}{2}$$
$$\Rightarrow K = \frac{2 \times 4.78}{111} = 0.086 \text{ MeV}$$

Total Energy = (4.78+0.086) MeV = 4.87 MeV

Sol 7: We have,
$$\frac{dN}{dt} = \lambda N = \lambda . N_0 . e^{-\lambda t}$$

Sol 8: We have Number of particles

$$= \frac{2.5 \times 10^{-3}}{230} \times 6.022 \times 10^{23}$$

So $\left| \frac{dN}{dt} \right| = (-\lambda N) \Rightarrow \lambda N = 8.4 \text{ sec}^{-1}$
 $\Rightarrow \frac{1}{\lambda} = \frac{N}{8.4} \text{ sec}$
 $\Rightarrow \frac{\ln 2}{\lambda} = t_{1/2} = \frac{\ln 2 \times N}{8.4} \text{ sec}$
 $= \frac{\ln 2 \times 2.5 \times 10^{-3} \times 6.022 \times 10^{23}}{230 \times 8.4 \times 365 \times 24 \times 60 \times 60} \text{ years} = 1.7 \times 10^{10} \text{ years}$

Sol 9: Activity / gm = 320/50 = 68.4 min⁻¹

$$\lambda = \frac{\ln 2}{t_{1/2}} = \frac{\ln 2}{5730} \text{ (years)}^{-1}$$

Now, initial activity = $\lambda . N_0$ Activity at some t = $\lambda . N_0 . e^{-\lambda t}$ So, 6.4 = $\lambda . N_0 . e^{-\lambda t}$ and 12 = λN_0 $\Rightarrow e^{-\lambda t} = 6.4/12$ $\Rightarrow \lambda t = \ln (12/6.4)$ $\Rightarrow t = \frac{5730 \times \ln(12/6.4)}{\ln 2} = 5196$ years

Sol 10: ${}_{1}^{2}H + {}_{1}^{2}H \rightarrow {}_{2}^{4}H + 23.6 \text{ MeV}$

Now we have, B.E. of He > B.E. of deuterium for the reaction to happen.

 \Rightarrow B.E. of helium = B.E. of Deuterium + 23.6 MeV

Sol 11:
$$\pi^+_{(\substack{\text{meson}\\150\text{ MeV}})} \rightarrow \mu^+_{(\substack{\text{neutrino}\\100\text{ MeV}})} \rightarrow P$$

Now assume momentum of $\overline{\nu} = P$
Now 150 = 100 + KE_{µ+} + KE _{$\overline{\nu}$} (energy conservation)
 $\Rightarrow 50 = \text{KE}_{\mu^+} + \text{KE}_{\overline{\nu}}$

Also using momentum conservation

$$\sqrt{2m_{\mu^{+}}KE_{\mu^{+}}} = P \text{ and } KE_{\overline{v}} = Pc$$

$$\Rightarrow KE_{\overline{v}} = c. \sqrt{2m_{\mu^{+}}KE_{\mu^{+}}}$$

$$\Rightarrow 50 = KE_{\mu^{+}} + \sqrt{2m_{\mu^{+}}c^{2}KE_{\mu^{+}}}$$

$$\Rightarrow 50 = KE_{\mu^{+}} + \sqrt{200KE_{\mu^{+}}}$$

$$\Rightarrow 50 = KE_{\mu^{+}} + 10\sqrt{2KE_{\mu^{+}}}$$

$$\Rightarrow (50 - x)^{2} = 200 x \quad (x = KE)$$

$$\Rightarrow x^{2} - 100x - 200 x + 2500 = 0$$

$$\Rightarrow x^{2} - 300x - 2500 = 0$$

$$x = \frac{300 \pm \sqrt{90000 - 10000}}{2}$$

$$= \frac{300 \pm 200\sqrt{2}}{2} = (150 \pm 100\sqrt{2}) \text{ MeV}$$

$$= (150 - 100\sqrt{2}) \text{ MeV}$$

$$= (150 - 141) \text{ MeV} = 9 \text{ MeV}$$
Sol 12: (m) v v (m-dm) (m-dm) (v+dv)

 $(v+dv-\mu)$

Momentum conservation

mv = (m - dm) (v + dv) + dm(v + dv - u)mv = mv + mdv - dmv + dmv - u.dm $\Rightarrow mdv = u.dm$ $\Rightarrow \int_{0}^{v} dv = u \int_{m_{0}}^{m} \frac{dm}{m}$

 $\Rightarrow v = u . \ln m/m_0$ Now, m = m_0.e^{- λt} \Rightarrow m/m₀ = e^{- λt} \Rightarrow v = u. (- λt) = - u λt

So v is opposite to u.



From the conservation of momentum the above diagram can be deduced

Now, Q = K.E. after collision – K.E. before collision

$$= \frac{P_{y}^{2}}{2m_{0}} + \frac{(P_{x}^{2} + P_{y}^{2})}{2m_{p}} - \frac{P_{x}^{2}}{2m_{I}}$$

$$= \frac{P_{y}^{2}}{2m_{0}} + \frac{P_{x}^{2}}{2m_{0}} - \frac{P_{x}^{2}}{2m_{0}} + \frac{(P_{x}^{2} + P_{y}^{2})}{2m_{p}} - \frac{P_{x}^{2}}{2m_{I}}$$

$$= \left[\frac{P_{x}^{2} + P_{y}^{2}}{2m_{p}}\right] \cdot \left[1 + \frac{m_{p}}{m_{0}}\right] - \frac{P_{x}^{2}}{2m_{0}} - \frac{P_{x}^{2}}{2m_{I}}$$

$$= K_{p} \cdot \left[1 + \frac{m_{p}}{m_{0}}\right] - \frac{P_{x}^{2}}{2m_{I}} \left(1 + \frac{m_{I}}{m_{0}}\right)$$

$$Q = K_{p} \cdot \left[1 + \frac{m_{p}}{m_{0}}\right] - K_{I} \cdot \left(1 + \frac{m_{I}}{m_{0}}\right)$$

Radioactivity

Sol 14:
$$_{90}Th^{232} \rightarrow {}_{82}Pb^{208} + 6 {}_{2}He^{4} + 4 {}_{+}^{0}\beta$$

 $n_{He} = \frac{1.01325 \times 10^{5} \times 8 \times 10^{-5} \times 10^{-6}}{8.314 \times 273}$
 $n_{He} = 3.571 \times 10^{-9}$
 $n_{Th} = 2.155 \times 10^{-9}$
 $n_{Th_{0}} = 2.75 \times 10^{-9}$
 $\frac{n_{Th}}{n_{Th_{0}}} = 0.783 = 2^{\frac{-t}{T_{1/2}}}$

$$\begin{split} & \Gamma_{1/2} \times \frac{\ln 0.783}{\ln 2} = -t \\ t &= \frac{1.39 \times 10^{10} \times 0.244}{0.693} \\ t &= 4.906 \times 10^9 \text{ yrs} \\ & \textbf{Sol 15: } N_0 \left(1 - e^{-36\lambda}\right) = 10^5 \\ & N_0 \left(1 - e^{-108\lambda}\right) = 1.11 \times 5^5 \\ & \frac{1 - e^{-36\lambda}}{1 - e^{-108\lambda}} = \frac{100}{111} \\ & \text{Let } e^{-36\lambda} = t e^{-108\lambda} = t^3 \\ & \frac{1 - t}{1 - t^3} = \frac{100}{111} \\ & \text{111} - 111 t = 100 - 100 t^3 \\ & 100 t^3 - 111 t + 11 = 0 \\ & (t - 1) \left(100 t^2 + 100 t - 11\right) = 0 \\ & t \neq 1 t = -1/2 + 3/5 \\ & t = 1/10 \\ & e^{-36\lambda} = \frac{1}{10} \Rightarrow -36\lambda = -\ln 10 \\ & \lambda = \frac{\ln 10}{36} \\ & \Gamma_{1/2} = \frac{\ln 2}{\ln 10} \times 36 \\ & \Gamma_{1/2} = 10.8 \sec \\ & \textbf{Sol 16: } \frac{A}{A_0} = \frac{1}{2^{1/3}} \\ & \frac{296}{60} \\ & \frac{296}{3.7 \times 10^4 \times \frac{1}{V}} = \frac{1}{2^{1/3}} \\ & V = \frac{3.7 \times 10^4 \times 60}{296 \times 2^{1/3}} \Rightarrow V = 5952.753 \text{ cm}^3 \\ & V = 5.592 \text{ m}^3 \\ & \textbf{Sol 17: } \lambda_1 = \frac{0.693}{2.44 \times 10^4} = 2.84 \times 10^{-5} \text{ yr}^1 \\ & \lambda_2 = \frac{0.693}{6.08 \times 10^3} = 1.139 \times 10^{-4} \text{ yr}^1 \\ & \lambda_1 = 9 \times 10^{-13} ; \lambda_2 = 3.61 \times 10^{-12} \\ \end{split}$$

$$A = \lambda_{1} N_{1} + \lambda_{2} N_{2}$$

$$6 \times 10^{9} = 6.02 \times 10^{23}$$

$$\left(\frac{9 \times 10^{-13} \times x}{239} + \frac{3.61 \times 10^{-12} (1-x)}{240}\right)$$

$$1 = \frac{90x}{239} + \frac{361(1-x)}{240}$$

$$1 = \frac{-64679x + 86279}{239 \times 240}$$

$$x = 0.447$$

$$\%^{230}Pu = 44.7\%$$

$$\%^{240}Pu = 55.3\%$$
Sol 18: (a) $\frac{dN}{dt} = \alpha - \lambda N$

$$\frac{dn}{\alpha - \lambda N} = dt$$

$$\ln \left(\frac{\alpha - \lambda N}{\alpha - \lambda N_{0}}\right) = -\lambda t$$

$$\frac{\alpha - \lambda N}{\alpha - \lambda N_{0}} = e^{-\lambda t}$$

$$N = \frac{1}{\lambda} \left[\alpha - (\alpha - \lambda N_{0}) e^{-\lambda t}\right]$$
(b) $t = t_{1/2}$

$$N = \frac{1}{\lambda} \left(\frac{\alpha}{2} + \frac{\lambda N_{0}}{2}\right) = \frac{1}{\lambda} (1.5 \lambda N_{0})$$

$$N = 1.5 N_{0}$$

$$\lim_{t \to \infty} N = \frac{\alpha}{\lambda} = 2N_{0}$$
Sol 19: $\frac{dP_{H}}{dt} = -kP_{H}$

$$\frac{1.2}{2} = 2^{\frac{50}{11/2}}$$

$$\ln \left(\frac{2}{1.2}\right) = \frac{50}{t_{1/2}} \ln 2$$

$$t_{1/2} = \frac{50 \ln 2}{\ln(2/1.2)} = 67.84 \min$$

$$k = \frac{\ln 2}{t_{1/2}} = 0.0102$$

$$\begin{split} \frac{dm}{dt} &= \frac{d(n/v)}{dt} = \frac{1}{RT} \frac{dP_{H}}{dt} \\ &= \frac{1}{RT} \times -0.0102 \times 1.2 \\ &= -\frac{0.0102 \times 1.2}{0.0821 \times 298} \text{ molarity/min} \\ &= 0.833 \times 10^{-5} \text{ molarity/sec.} \\ \text{Sol 20: } n_{U} &= \frac{1}{238}, n_{Pb} = \frac{0.1}{206} \\ 2^{\frac{t}{1/2}} &= \frac{n_{0}}{n} \\ \frac{t}{t_{1/2}} &= \frac{\ln(n_{0}/n)}{\ln 2} \\ t_{1} &= \frac{t_{1/2} \times \ln(n_{0}/n)}{1 \ln 2} \\ \ell \ln \left(\frac{n_{0}}{n}\right) &= \ln \left(\frac{1/238}{1/238 - 0.1/206}\right) = 0.119 \\ t &= \frac{4.5 \times 10^{9} \times 0.1227}{\ln 2} \\ t &= 7.75 \times 10^{8} \text{ years} \\ \text{Sol 21: } \frac{218}{84} \text{Po} \xrightarrow{\lambda_{1}} \frac{214}{N2} \text{Pb} \xrightarrow{\lambda_{2}} \frac{214}{N3} \text{Pb} + \frac{0}{1}\beta \\ \frac{dN}{dt} &= \lambda_{1}N_{1} - \lambda_{2}N \\ \frac{dN}{dt} &= \lambda_{1}N_{0}e^{-\lambda_{1}t} - \lambda_{2}N \\ N &= \frac{\lambda_{1}N_{0}\left(e^{-\lambda_{1}t} - e^{-\lambda_{2}t}\right)}{(\lambda_{2} - \lambda_{1})} \\ \frac{dN}{dt} &= 0 \\ \Rightarrow \lambda_{1}N_{0} e^{-\lambda_{1}t} &= \lambda_{2} e^{-\lambda_{1}t} - \lambda_{2} e^{-\lambda_{2}t} \\ (\lambda_{1}) e^{-\lambda_{1}t} &= \lambda_{2} e^{-\lambda_{1}t} - \lambda_{2} e^{-\lambda_{2}t} \\ (\lambda_{1}) e^{-\lambda_{1}t} &= \lambda_{2} e^{-\lambda_{1}t} - \lambda_{2} e^{-\lambda_{2}t} \\ (\lambda_{1}) e^{-\lambda_{1}t} &= \lambda_{2} e^{-\lambda_{1}t} - \lambda_{2} e^{-\lambda_{2}t} \\ (\lambda_{1}) e^{-\lambda_{1}t} &= \lambda_{2} e^{-\lambda_{1}t} - \lambda_{2} e^{-\lambda_{2}t} \\ (\lambda_{1}) e^{-\lambda_{1}t} &= \lambda_{2} e^{-\lambda_{2}t} \\ e^{(\lambda_{1} - \lambda_{2})t} &= \frac{\lambda_{1}}{\lambda_{2}} \\ t &= \frac{\ln((\lambda_{1}/\lambda_{2})}{(\lambda_{1} - \lambda_{2})} \end{split}$$

$$t = \frac{\ln(2.68 / 3.05)}{\ln 2 \left(\frac{1}{3.05} - \frac{1}{2.68}\right)} = 4.12 \text{ min}$$

Sol 22: (a) Given at time t; ${}^{238}_{92}$ U = 1.667g = $\left(\frac{1.667}{238}\right)$ mole

$$^{206}_{83}$$
Pb = 0.277g = $\left(\frac{0.277}{206}\right)$ mole

Since all lead has been formed from $\mathsf{U}^{\scriptscriptstyle 238}$ and therefore

moles of U decayed = Moles of Pb formed = $\left(\frac{0.277}{206}\right)$

 \therefore Total moles of U before decay (N_0) = moles of U at time t (N)

$$= \frac{1.667}{238} \times \frac{0.277}{206} \quad \because \quad t = \frac{2.303}{\lambda} \log \frac{N_0}{N}$$
$$= \frac{2.303 \times 4.51 \times 10^9}{0.693} \log \frac{\left(\frac{1.667}{238}\right) + \left(\frac{0.277}{206}\right)}{\left(\frac{1.667}{238}\right)}$$

(a) t = 1.143×10^9 year

(b) 7.097×10^8 year

Sol 23: Minimum β -activity required = 346 min⁻¹

Number of β -activity required to carry out the experiment for 6.909 h = (346 min⁻¹) (6.909 × 60 min) = 143431

Amount of β -activity required

$$= \frac{143431}{6.022 \times 10^{23} \text{ mol}^{-1}} = 2.3818 \times 10^{-19} \text{ mol}$$

Now, the rate constant of radioactive decay is

$$\lambda = \frac{0.693}{t_{\frac{1}{2}}} = \frac{0.693}{66.6 \text{ h}} = 0.010404 \text{ h}^{-1}$$

Now using the integrated rate expression

$$\log \frac{n_0 - n_{\text{consumed}}}{n_0} = -\frac{\lambda t}{2.303},$$

We get $\log \frac{n_0 - 2.3818 \times 10^{-19} \text{ mol}}{n_0}$
$$= -\frac{(0.010404 \text{ h}^{-1}) (6.909 \text{ h})}{2.303} = -0.03121$$
$$\frac{n_0 - 2.3818 \times 10^{-19} \text{ mol}}{n_0} = 0.9306$$

or

Solving for n₀, we get

$$n_0 = \frac{2.3818 \times 10^{-19} \text{ mol}}{1 - 0.9306} = 3.43 \times 10^{-18} \text{ mol}$$

Exercise 2

Single Correct Choice Type

Sol 1: (D)
$${}_{1}H^{2} \rightarrow {}_{1}P^{1} + {}_{0}n^{1} + Energy$$

 ${}_{1876MeV} \rightarrow {}_{939MeV} + {}_{940MeV} + Energy$

So energy conservation gives

 \Rightarrow 1876 = 939 + 940 + E

 \Rightarrow E = -3MeV

So a γ ray has to be absorbed

Sol 2: (C) Mass number is constant as no nucleoid is emitted.

Sol 3: (D) Mass of 20 is released and charge of 6 is released from nucleus 20 mass \Rightarrow 5 α .

Sol 4: (B) Given that k.E_a = 48 Mev, Q = 50 Mev

We know that $\mathbf{k}.\mathbf{E}_{\alpha} = \mathbf{Q}\left(\frac{\mathbf{A}-\mathbf{4}}{\mathbf{A}}\right)$

Here, A is the mass number of mother nucleus Putting the values, we get

$$\Rightarrow 48 = 50 \left(\frac{A-4}{A}\right) \Rightarrow 48 A = 50 A - 200$$
$$\Rightarrow A = 100$$

Sol 5: (B) In the uranium radioactive series the initial nucleus is 8 alpha and 6 beta particles are released as it is a 4n + 2 series.

Sol 6: (D) Activity =
$$\frac{dN}{dt}$$
 = N × I
So $\lambda \cdot N_0 \cdot e^{-\lambda t}$ = activity (R)
 $\frac{R_2}{R_1} = \frac{\lambda \cdot N_0 \cdot e^{-\lambda t_2}}{\lambda \cdot N_0 \cdot e^{-\lambda t_1}} = e^{\lambda (t_1 - t_2)}$

Sol 7: (C) Just like tossing of a coin, S heads won't change probability of next outcome, after any half-life,

there is $\frac{1}{2}$ probability of any atom surviving.

Sol 8: (B)
$$\frac{A_0}{\sqrt{3}} = A_0 \cdot e^{-\lambda t} = A_0 \cdot e^{-1}$$

 $\Rightarrow \lambda = \frac{1}{2}\lambda n3$
Activity $= \lambda N = \lambda N_0 \cdot e^{-4\lambda} = A_0 \cdot e^{-4\lambda} = A_0/9$

Sol 9: (C) So act. $(t_1) = \lambda N_1 = \lambda . N_0 . e^{-\lambda t_1} = A_1$

So act. (t₂) = $\lambda N_2 = \lambda N_0 e^{-\lambda t_2} = A_2$

So
$$\frac{A_1}{A_2} = e^{\lambda(t_2-t_1)} \Rightarrow A_2 = A_1 \cdot e^{(t_2-t_1)/T}$$

Sol 10: (A) $f_1 > f_2 \Rightarrow 63^\circ$ decays in mean life

Sol 11: (C)
$$\frac{dN}{dt} = R - \lambda N$$

 $\Rightarrow \lambda N + \frac{dN}{dt} = R$
 $\Rightarrow \int_{0,0}^{N,t} d\left[N.e^{\lambda t}\right] = \int_{0}^{t} R.e^{\lambda t}.dt$
 $N.e^{\lambda t} = \frac{R}{\lambda} \cdot \left[e^{\lambda t} - 1\right]$
 $\Rightarrow N = \frac{R}{\lambda} \cdot \left[1 - e^{-\lambda t}\right]$
So, N = 10, R = 10
 $\Rightarrow 10 = \frac{10}{1/2} \left[1 - e^{-t/2}\right]$
 $\Rightarrow e^{-t/2} = 1/2$
 $\Rightarrow t = 2ln2 = 0.693$

Sol 12: (B) $R_1 = \lambda . N_0 . e^{-\lambda T_1}$ and $R_2 = \lambda . N_0 . e^{-\lambda T_2}$

$$t_{1/2} = T = \frac{ln2}{\lambda} \Rightarrow \boxed{\lambda = \frac{ln2}{T}}$$

Number of atoms disintegrated = $N_1 - N_2$

<u>а</u>т

$$= N_{0} \cdot e^{-\lambda T_{1}} - N_{0} \cdot e^{-\lambda T_{2}}$$
$$= \frac{R_{1} - R_{2}}{R_{1} - R_{2}} = \frac{T(R_{1} - R_{2})}{R_{1} - R_{2}}$$

$$\frac{1}{\lambda} = \frac{1}{\ln 2}$$

Sol 13: (E) Rate =
$$\frac{dN}{dt} = \lambda N(t) = \lambda N_0 e^{-\lambda t} \Longrightarrow (E)$$

Sol 14: (C) depends on the number of elements and activities inside nucleus.

Sol 15: (C) Mean life = $1/\lambda$ $\Rightarrow \lambda = 1/40 \text{ (min}^{-1}) = \frac{1}{2400} \text{ sec}^{-1}$ $So \frac{dN}{dt} = -\lambda N + R$ $\Rightarrow N = \frac{R}{\lambda} \cdot \left[1 - e^{-\lambda t}\right]$ At steady state, $t \rightarrow \infty$, \Rightarrow N = $\frac{R}{\lambda} = \frac{10^3}{1/2400} = 24 \times 10^5$

Sol 16: (B) at t = 0, N and at t $\rightarrow \infty$, N = const.

Sol 17: (C) Because neutron has larger rest mass than proton.

Multiple Correct Choice Type

Sol 18: (A, B, D) × nuclear attraction is there, (no rep.)

(B) \checkmark as r \uparrow the energy $\downarrow \Rightarrow$ it is electrostatic (C) ✓ Nuclear attraction

(D) \times

Sol 19: (A, C) Refer theory.

Sol 20: (C, D) Due to mass defect (which is finally responsible for the binding energy of the nucleus), mass of a nucleus is always less than the sum of masses of its constituent particles.

²⁰₁₀Ne is made up of 10 protons plus 10 neutrons. Therefore, mass of ${}^{20}_{10}$ Ne nucleus, M₁ < 10 (m_o + m_n) Also, heavier the nucleus, more is the mass defect. Thus, $20(m_n + m_n) - M_2 > 10(m_n + m_n) - M_1$ Or $10(m_p + m_n) > M_2 - M_1$ Or $M_2 < M_1 + 10(m_p + m_n)$ Now since $M_1 < 10(m_p + m_n)$ $M_{2} < 2M_{1}$

Sol 21: (A, C) $T = \frac{0.693}{\lambda} = 2$

 \therefore Decay time = n × Half life.

$$\therefore \quad n = \frac{8}{4} = 2$$
$$\therefore \quad \frac{N}{N_0} = \left(\frac{1}{2}\right)^n = \frac{1}{4}$$

Sol 22: (B, C) A, B, negative slope, +F;

B, C, positive slope, -F

Sol 23: (A, B, C) (A) √true (cons. of energy)

(B) \checkmark True (cons. of energy). [energy can't be generated from anywhere alse]

(C) \checkmark as either N \downarrow (β^{-}) and P \uparrow or N \uparrow or P \downarrow (β^{+})

(D) \times mass number is const. so (ABC)

Sol 24: (A, B, C) (A) ✓ free neutron is unstable

- (B) √ free proton is stable
- (C) \checkmark B⁻and B⁺ decay
- (D) \times both are possible ABC

Sol 25: (C, D) (A) \times as ${}^{4}_{2}$ He²⁺ has charge in it

(B) \times as (+) 1 charge is there in neutron

(C) $\checkmark \gamma$ decay (no charge transfer)

(D) \checkmark inside the atom, no change in charge.

(C, D)

Sol 26: (C, D)

(C) √

(D) √

Because there is comparatively more distance between protons inside the nucleus, electric repulsion is more because nuclear forces are small as compared to electrostatic when distance is high.

Sol 27: (B, C)

(B) √

(C) ✓ At high A, BE /nucleon is more

Sol 28: (A, B, C) (A)
$$\checkmark$$
 N = N₀.e^{- λ t}

 $(B) \checkmark \frac{dN}{dt} = -\lambda N$

 $(C) \checkmark N = N_0(1 - e^{-\lambda t})$

(D) \times

Sol 29: (A, D) ${}^{A}_{Z}A \longrightarrow {}^{A-4}_{Z-2}A + {}^{4}_{2}He^{2+}$ ${}^{A}_{Z}B \longrightarrow {}^{A}_{Z+1}B + \beta + \overline{\nu}$

(A) \checkmark Now as the α -particle is alone, the energy could transfer to the α -particle only and from momentum cons., the particles will have same v.

(C) \times

(D) \checkmark Now during β -decay, the anti-neutrino is also emitted with the β -particle and thus energy can be distributed between them.

Sol 30: (**D**, **E**) ${}^{14}_{7}$ N + ${}^{1}_{0}$ n $\longrightarrow {}_{3}$ Li⁷ + 'some more '

elements

Now mass number should be same

$$14 + 1 = 7 + x \Longrightarrow x = 8$$

(So the products should have mass number = 8) (D) \checkmark and (E) \checkmark

Now charge also has to balance in D and E.

 $1\alpha \Longrightarrow 2 + 4 - 2 = 4$

Similarly, (E) is also correct and 4P° + 2B

So (D), (E)

Sol 31: (A, C, D) (A) more nucleons \Rightarrow release of nucleons as α particles

(B) Protons in excess \Rightarrow B⁺ release \Rightarrow (C) is \checkmark

(D) β^- is reduced then protons are increased and neutrons are decreased in a nucleus.

 \Rightarrow (A), (C), (D)

Assertion Reasoning Type

Sol 32: (D) Because the statement is valid for large number of nuclei

Sol 33: (C) Remaining energy is given to the antineutrino particles

Sol 34: (A) True exp.

Sol 35: (A) True exp.

Comprehension Type

Paragraph 1

Sol 36: (B) 1 million = 10,00,000 = 10⁶ person Electric power = $300 \times 10^6 = 3 \times 10^8$ watts Thermal power = $\frac{3 \times 10^8}{0.25}$ = 12×10^8 watts t = $24 \times 60 \times 60$ So N × 200 × $10^6 \times 1.6 \times 10^{-19}$ J = $12 \times 10^8 \times t$ \Rightarrow N = $\frac{12 \times 10^8 \times 24 \times 60 \times 60}{200 \times 1.6 \times 10^{-13}}$ = $\frac{12 \times 24 \times 60 \times 60}{2 \times 1.6} \times 10^{21} = 3.24 \times 10^{24}$

Paragraph 2

Sol 37: (C) Now,
$$\frac{h}{p} = 5.76 \times 10^{-15} \text{ m}$$

$$\Rightarrow P = \frac{6.6 \times 10^{-34}}{5.76 \times 10^{-15}} = 1.15 \times 10^{-19} \text{ N-s}$$

As from cons. of momentum, their mom should be same

Sol 38: (B)
$$P = mv = \frac{P^2}{2m} = KE$$

$$\Rightarrow KE = \frac{(1.15 \times 10^{-19})^2}{2 \times 4 \times 1.6 \times 10^{-27}} J$$

$$= \frac{(1.15)^2 \times 10^{-38}}{8 \times 1.6 \times 10^{-27}} J = \frac{(1.15)^2 \times 10^{-11}}{8 \times 1.6 \times 1.6 \times 10^{-19}} eV$$

$$= \frac{(1.15)^2}{8 \times 1.6 \times 1.6} \times 10^8 eV = 6.22 \times 10^6$$
Sol 39: (D) $KE = \frac{P^2}{2m}$

$$= \frac{(1.15 \times 10^{-19})^2}{2 \times 223.4 \times 1.6 \times 10^{-27}} J$$

$$= \frac{(1.15)^2 \times 10^{-11}}{2 \times 223.4 \times 1.6 \times 1.6 \times 10^{-19}} eV$$

$$= \frac{(1.15)^2}{2 \times 223.4 \times (1.6)^2} \times 10^8 eV$$

$$= 0.11 MeV$$

Match the Columns

Sol 40: (A) \rightarrow q charge balance (B) \rightarrow p (238 – 32) = 206 \triangleright (B) (C) \rightarrow t (Theory) (D) \rightarrow r (Z_{new} = Z – 2) (E) \rightarrow s 16 + 2 – 4 = 14 (mass no.)

Sol 41: (A) \rightarrow p and q Matter into energy (mass defect is observed) Materials combine (low atomic no.) (B) \rightarrow (p) mass defect (r) big nucleus disintegrates into smaller ones (C) \rightarrow (p) mass defect (r) weak nuclear forces are Responsible (D) \rightarrow (r) (s)

Sol 42: (A) \rightarrow r (from def.) (B) \rightarrow p (from def.) (C) \rightarrow q (from def.) (D) \rightarrow q (from def.)

Radioactivity

Single Correct Choice Type

Sol 43: (D)
$$\frac{1}{2^{t_{1/2}}} = \frac{5}{6} \Rightarrow 2^{\frac{1}{t_{1/2}}} = \frac{6}{5}$$

 $\frac{t}{t_{1/2}} = \frac{\ln 6/5}{\ln 2}$
 $t = \frac{t_{1/2} \ln 6/5}{\ln 2} = \frac{1}{\lambda} \ln 6/5$

Sol 44: (C) For Tc⁹⁹ = t_{1/2} t_{1/2} = 6.0 hr Let the minimum amount be x Concentration after 3 hr = $\frac{x}{\sqrt{2}}$ $\frac{x}{\sqrt{2}} \ge 10.0 \text{ mg} \Rightarrow x \ge 10.0 \times \sqrt{2} \text{ mg}$ $x \ge 14.1 \text{ mg}$ Sol 45: (C) $N_{11} = 0.1 e^{-\lambda \times 11}$ $N_{10} = 0.1 e^{-\lambda \times 10}$ Atoms decaying during 11th day $= N_{10} - N_{11} = 0.1 (e^{-10\lambda} - e^{-11\lambda})$ $= 0.1 \left(-e^{\frac{-\ln 2 \times 11}{5}} + e^{\frac{-\ln 2 \times 10}{5}} \right)$

Multiple Correct Choice Type

Sol 46: (**A**, **B**, **C**, **D**) (A) $t_{1/2} \propto C^{1-n}$ where n is the order of the reaction. (B) $t_{avg} = \frac{1}{\lambda} = \frac{t_{1/2}}{\ln 2}$ (C) $\frac{dN}{dt} = -\lambda N^2$ $\frac{dN}{N^2} = -\lambda dt;$ $\frac{1}{N} = \lambda t;$ $N = \frac{1}{\lambda t}$ (D) $t_{1/2} = \frac{0.693}{0.0693} = 10$ min % Reactant = $\frac{100}{2^{10}} = \frac{100}{1024} = 0.098$ Reaction completions = 99.92%

Sol 47: (B, C, D)
$${}^{14}_{6}C \rightarrow {}^{14}_{7}N + {}^{0}_{-1}\beta$$

 ${}_{2}C^{14}H_{4} \rightarrow 2N^{14}H_{3} + H_{2}$

(A)

Sol 48: (C, D) (A) Within the atom not nucleus (B) ${}_{1}^{3}H \rightarrow {}_{2}^{3}He + {}_{-1}^{0}\beta$ (C) ${}_{1}^{1}P \rightarrow {}_{+1}^{0}\beta + {}_{0}^{1}n$ \therefore n/p ratio increases (D) True

Comprehension Type

Paragraph 1

Sol 49: (C)
$$\frac{dN}{dt} = \alpha - \lambda N;$$

 $\frac{dN}{\alpha - \lambda N} = dt$
 $\frac{-1}{\lambda} \ln\left(\frac{\alpha - \lambda N}{\alpha - \lambda N_0}\right) = t \Rightarrow \frac{\alpha - \lambda N}{\alpha - \lambda N_0} = e^{-\lambda t}$

$$\begin{aligned} \alpha - \lambda N &= (\alpha - \lambda N_0) e^{-\lambda t} \implies \lambda N = \alpha - (\alpha - \lambda N_0) e^{-\lambda t} \\ \implies N &= \frac{1}{\lambda} \left[\alpha - (\alpha - \lambda N_0) e^{-\lambda t} \right] \end{aligned}$$
Sol 50: (C) $t_{1/2} = \frac{\ln 2}{\lambda}$

$$N &= \frac{1}{\lambda} \left(\alpha - (\alpha - \lambda N_0) e^{-\lambda \frac{\ln 2}{\lambda}} \right) = \frac{1}{\lambda} \left(\alpha - \left(\frac{\alpha - \lambda N_0}{2} \right) \right) \end{aligned}$$

$$= \frac{1}{\lambda} \left(\frac{\alpha}{2} + \frac{\lambda N_0}{2} \right) = \frac{1}{\lambda} \left(\frac{2N_0\lambda}{2} + \frac{\lambda N_0}{2} \right)$$

$$N = 1.5 N_0$$

Paragraph 2

Sol 51: (A) ${}^{10}_{4}\text{Be} \rightarrow {}^{10}_{5}\text{Be} + e^{-}$ $\Delta m = (4m_p + 6m_n) - (5m_p + 5m_n) - m_e$ $+4m_e - 5m_e + m_e$ = At. mass of ${}_{4}\text{Be}{}^{10}$ - At mass of ${}_{5}\text{B}{}^{10}$

Sol 52: (D) ${}_{5}^{8}Be \rightarrow {}_{4}^{8}Be + e^{+}$ $\Delta m = (5m_{p} + 3m_{n}) - (4m_{p} + 4m_{n}) - m_{e}$ $+5m_{e} - 4m_{e} - m_{e}$ $\Delta m = At. mass of {}_{5}B^{8} - At mass of {}_{4}Be^{8}$ - mass of two electrons

Previous Years' Questions

Sol 1: Speed of neutrons

$$= \sqrt{\frac{2K}{m}} \left(\text{from } K = \frac{1}{2}mv^2 \right)$$

or $v = \sqrt{\frac{2 \times 0.0327 \times 1.6 \times 10^{-19}}{1.675 \times 10^{-27}}} \approx 2.5 \times 10^3 \text{m/s}$

Time taken by the neutrons to travel a distance of 10 m:

$$t = \frac{d}{v} = \frac{10}{2.5 \times 10^3} = 4.0 \times 10^{-3}$$

Number of neutrons decayed after time

$$t: N = N_0(1 - e^{-\lambda t})$$

 \therefore Fraction of neutrons that will decay in this time interval

$$= \frac{N}{N_0} = (1 - e^{-\lambda t}) = 1 - e^{-\frac{\ln(2)}{700} \times 4.0 \times 10^{-3}} = 3.96 \times 10^{-6}$$

Sol 2: Mass defect in the given nuclear reaction:

$$\Delta m = 2(mass of deuterium) - (mass of helium)$$

= 2(2.0141) - (4.0026) = 0.0256

Therefore, energy released

 $\Delta E = (\Delta m)(931.48)MeV = 23.85 MeV$

 $= 23.85 \times 1.6 \times 10^{-13} \text{ J} = 3.82 \times 10^{-12} \text{ J}$

Efficiency is only 25%, therefore,

25% of
$$\Delta E = \left(\frac{25}{100}\right) (3.82 \times 10^{-12}) \text{ J}$$

= 9.55 × 10⁻¹³ J

i.e., by the fusion of two deuterium nuclei, 9.55 \times 10⁻¹³ J energy is available to the nuclear reactor.

Total energy required in one day to run the reactor with a given power of 200 MW:

 $E_{total} = 200 \times 10^6 \times 24 \times 3600 = 1.728 \times 10^{13} J$

 \therefore Total number of deuterium nuclei required for this purpose

n =
$$\frac{E_{total}}{\Delta E/2} = \frac{2 \times 1.728 \times 10^{13}}{9.55 \times 10^{-13}} = 0.362 \times 10^{26}$$

... Mass of deuterium required

= (Number of g-moles of deuterium required)

× 2 g
=
$$\left(\frac{0.362 \times 10^{26}}{6.02 \times 10^{23}}\right)$$
 × 2 = 120.26 g.

Sol 3: (a) A – 4 = 228

∴ A = 232

92 - 2 = Z or Z = 90

(b) From the relation,

$$r = \frac{\sqrt{2Km}}{Bq}$$

$$K_{\alpha} = \frac{r^{2}B^{2}q^{2}}{2m} = \frac{(0.11)^{2}(3)^{2}(2 \times 1.6 \times 10^{-19})^{2}}{2 \times 4.003 \times 1.67 \times 10^{-27} \times 1.6 \times 10^{-13}}$$

From the conservation of momentum,

or
$$p_{\gamma} = p_{\alpha}$$
 or $\sqrt{2K_{\gamma}m_{\gamma}} = \sqrt{2K_{\alpha}m_{\alpha}}$
 $\therefore K_{\gamma} = \left(\frac{m_{\alpha}}{m_{\gamma}}\right)K_{\alpha} = \frac{4.003}{228.03} \times 5.21 = 0.09 \text{ MeV}$

$$\therefore$$
 Total energy released = $K_{\alpha} + K_{\gamma} = 5.3 \text{ MeV}$

Total binding energy of daughter products

- = [92× (mass of proton) + (232 92) (mass of neutron) – (m_{γ}) – (m_{α})] ×931.48 MeV
- $= [(92 \times 1.008) + (140)(1.009) 228.03 4.003]$

×931.48 MeV

- = 1828.5 MeV
- : Binding energy of parent nucleus
- = binding energy of daughter products –

energy released

= (1828.5 - 5.3) MeV = 1823.2 MeV

Sol 4: λ = Disintegration constant

 $\frac{0.693}{t_{1/2}} = \frac{0.693}{15} h^{-1} = 0.0462 h^{-1}$

Let R_0 = initial activity = 1 microcurie

= 3.7×10^4 disintegration per second.

 $r = Activity in 1 cm^3 of blood at t = 5 h$

 $=\frac{296}{60}$ disintegration per second

= 4.93 disintegration per second, and

R = Activity of whole blood at time t = 5 h

Total volume of blood should be

$$V = \frac{R}{r} = \frac{R_0 e^{-\lambda t}}{r}$$

Substituting the values, we have

$$V = \left(\frac{3.7 \times 10^4}{4.93}\right) e^{-(0.0462)(5)} \text{ cm}^3$$
$$V = 5.95 \times 10^3 \text{ cm}^3$$
or V = 5.95 L

Sol 5: The reaction involved in α -decay is

Means life is given as $t_{mean} = 10^{13} s = \frac{1}{\lambda}$

: Disintegration constant $\lambda = 10^{-13} \text{ s}^{-1}$

Rate of decay at the moment when number of nuclei are $10^{20} = \lambda N = (10^{-13})(10^{20})$

= 10⁷ disintegration per second

Of these disintegrations. 8% are in fission and 92% are in $\alpha\text{-decay}$

Therefore, energy released per second

- = $(0.08 \times 10^7 \times 200 + 0.92 \times 10^7 \times 5.136)$ MeV
- = 2.074 × 10⁸ MeV
- ... Power output (in watt)
- = energy released per second (J/s)
- $= (2.074 \times 10^8) (1.6 \times 10^{-13})$
- \therefore Power output = 3.32 × 10⁻⁵ W

Sol 6: (a) Let at time t, number of radioactive nuclei are N. Net rate of formation of nuclei of A

$$\frac{dN}{dt} = \alpha - \lambda N$$

or $\frac{dN}{\alpha - \lambda N} = dt$ or $\int_{N_0}^{N} \frac{dN}{\alpha - \lambda N} = \int_{0}^{t} dt$

solving this equation, we get

$$N = \frac{1}{\lambda} \left[\alpha - (\alpha - \lambda N_0) e^{-\lambda t} \right] \qquad ... (i)$$

(b) (i) Substituting α = $2\lambda N_{_0}$ and t = $t_{_{1/2}} \, \frac{ln(2)}{\lambda}$ in equation (i) we get,

$$N = \frac{3}{2}N_0$$

(ii) Substituting α = $2\lambda N_{_0}$ and t $\rightarrow \infty$ in Equation (i), we get

$$N = \frac{\alpha}{\lambda} = 2N_0 \text{ or } N = 2N_0$$

Sol 7: The reactor produces 1000 MW power or 10^9 J/s. The reactor is to function for 10 yr. Therefore, total energy which the reactor will supply in 10 yr is

E = (power)(time) = $(10^9 \text{ J/s})(10 \times 365 \times 24 \times 3600 \text{ s})$ = $3.1536 \times 10^{17} \text{ J}$

But since the efficiency of the reactor is only 10%, therefore actual energy needed is 10 times of it or 3.1536 \times 10¹⁸ J. One uranium atom liberates 200 MeV of energy

or 200 $\times 1.6 \times 10^{-13}$ J or 3.2 $\times 10^{-11}$ J of energy. So, number of uranium atoms needed are

$$\frac{3.1536 \times 10^{18}}{3.2 \times 10^{-11}} = 0.9855 \times 10^{29}$$

Or number of kg-moles of uranium needed are

$$n = \frac{0.9855 \times 10^{29}}{6.02 \times 10^{26}} = 163.7$$

Hence, total mass of uranium required is

$$m = (n)M = (163.7)(235) kg$$

or m \approx 38470 kg or m = 3.847 \times 10⁴ kg

Sol 8: (a) Let at time t = t, number of nuclei of Y and Z are N_y and N_z . Then

Rate equations of the populations of X, Y and Z are

$$\left(\frac{dN_x}{dt}\right) = -\lambda_x N_x \qquad \dots (i)$$

$$\left(\frac{dN_{Y}}{dt}\right) = \lambda_{X}N_{X} - \lambda_{Y}N_{Y} \qquad ... (ii)$$

and
$$\left(\frac{dN_z}{dt}\right) = \lambda_y N_y$$
 ... (iii)

(b) Given N_v(t) =
$$\frac{N_0 \lambda_X}{\lambda_X - \lambda_Y} [e^{-\lambda_Y t} - e^{-\lambda_X t}]$$

For N_v to be maximum

$$\frac{dN_{Y}(t)}{dt} = 0$$

i.e., $\lambda_{X}N_{X} = \lambda_{Y}N_{Y}$... (iv)

[from Equation (ii)]

or
$$\lambda_{x}(N_{0}e^{-\lambda}x^{t}) = \lambda_{y} \frac{N_{0}\lambda_{x}}{\lambda_{x} - \lambda_{y}} [e^{-\lambda_{y}t} - e^{-\lambda_{x}t}]$$

or $\frac{\lambda_{x} - \lambda_{y}}{\lambda_{y}} = \frac{e^{-\lambda_{y}t}}{e^{-\lambda_{x}t}} - 1; \frac{\lambda_{x}}{\lambda_{y}} = e^{(\lambda_{x} - \lambda_{y})t}$
or $(\lambda_{x} - \lambda_{y})t \lambda n(e) = \ln\left(\frac{\lambda_{x}}{\lambda_{y}}\right)$
or $t = \frac{1}{\lambda_{x} - \lambda_{y}} \ln\left(\frac{\lambda_{x}}{\lambda_{y}}\right)$

NI A

Substituting the values of λ_x and λ_y we have

t =
$$\frac{1}{(0.1-1/30)} \ln\left(\frac{0.1}{1/30}\right)$$
 = 15 ln (3)

or t = 16.48 s.

(c) The population of X at this moment,

$$\begin{split} N_{X} &= N_{0} e^{-\lambda_{X}t} = (10^{20}) e^{-(0.1)(16.48)} \\ N_{X} &= 1.92 \times 10^{19} \\ N_{Y} &= \frac{N_{X}\lambda_{X}}{\lambda_{Y}} [\text{From Equation (iv)}] \\ &= (1.92 \times 10^{19}) \frac{(0.1)}{(1/30)} = 5.76 \times 10^{19} \\ N_{Z} &= N_{0} - N_{X} - N_{Y} = 10^{20} - 1.92 \times 10^{19} - 5.76 \times 10^{19} \\ \text{or } N_{z} &= 2.32 \times 10^{19} \end{split}$$

Sol 9: Let N_0 be the initial number of nuclei of ²³⁸U.

After time t, $N_{U} = N_{0} \left(\frac{1}{2}\right)^{n}$

Here n = number of half-lives

$$= \frac{t}{t_{1/2}} = \frac{1.5 \times 10^9}{4.5 \times 10^9} = \frac{1}{3}$$

$$N_{U} = N_0 \left(\frac{1}{2}\right)^{1/3}$$
and $N_{Pb} = N_0 - N_U = N_0 \left[1 - \left(\frac{1}{2}\right)^{1/3}\right]$

$$\therefore \frac{N_U}{N_{Pb}} = \frac{\left(\frac{1}{2}\right)^{1/3}}{1 - \left(\frac{1}{2}\right)^3} = 3.861$$

Sol 10: $\left| \frac{dN}{dt} \right| = |Activity of radioactive substance|$ = $\lambda N = \lambda N_0 e^{-\lambda t}$

Taking log both sides

$$\ln \left| \frac{dN}{dt} \right| = \ln(\lambda N_0) - \lambda t$$

Hence, $\ln \left| \frac{dN}{dt} \right|$ versus t graph is a straight line with slope – λ . From the graph we can see that,

$$\lambda = \frac{1}{2} = 0.5 \text{ yr}^{-1}$$

Now applying the equation,

$$N = N_0 e^{-\lambda t} = N_0 e^{-0.5 \times 4.16}$$
$$= N_0 e^{-2.08} = 0.125 N_0 = \frac{N_0}{8}$$

i.e., nuclei decreases by a factor of 8. Hence, the answer is 8.

Sol 11: Activity
$$\left(-\frac{dN}{dt}\right) = \lambda N = \left(\frac{1}{t_{mean}}\right) \times N$$

 $\therefore N = \left(-\frac{dN}{dt}\right) \times t_{mean} = \text{Total number of atoms}$ Mass of one atom is 10⁻²⁵ kg = m(say)

... Total mass of radioactive substance

= (number of atoms) × (mass of one atom)

$$=\left(-\frac{\mathrm{dN}}{\mathrm{dt}}\right)(\mathrm{t}_{\mathrm{mean}})(\mathrm{m})$$

Substituting the values, we get

Total mass of radioactive substance = 1 mg

: Answer is 1.

Sol 12: $A \rightarrow p$, q; $B \rightarrow p$, r; $C \rightarrow p$, s; $D \rightarrow p$, q, r

Sol 13: (D) It is only due to collision between high energy thermal deuterons which get fully ionized and release energy which increases the temperature inside the reactor

Sol 14: From conservation of mechanical energy, we have

$$U_{i} + K_{i} = U_{f} + K_{f}$$

$$0 + 2(1.5 \text{ KT}) = \frac{1}{4\pi\varepsilon_{0}} \cdot \frac{(e)(e)}{d} + 0$$
Substituting the values, we get

 $T = 1.4 \times 10^9 \text{ K}$

Sol 15: (B, D) If $(BE)_{final} - (BE)_{initial} > 0$ Energy will be released.

Sol 16: (B) $nt_0 > 5 \times 10_{14}$ (as given)

Sol 17: (D)
$$f = (1 - e^{-\lambda t}) = 1 - e^{-\lambda t} \approx (1 - \lambda t) = \lambda t$$

f = 0.04

Hence % decay ≈ 4%

Sol 18: (C)
$$\frac{A}{A_0} = \left(\frac{1}{2}\right)^{\frac{1}{2}}$$

Where, A_0 is the initial activity of the radioactive material and A is the activity at t.

So,
$$\frac{12.5}{100} = \left(\frac{1}{2}\right)^{\frac{t}{T}}$$
 $\therefore t = 3T$

Sol 19: (C)

 $(\mathsf{A}) \rightarrow (\mathsf{r},\,\mathsf{t})\;;\,(\mathsf{B}) \rightarrow (\mathsf{p},\,\mathsf{s})\;;\,(\mathsf{C}) \rightarrow (\mathsf{p},\,\mathsf{q},\,\mathsf{r},\,\mathsf{t});\,(\mathsf{D}) \rightarrow (\mathsf{p},\,\mathsf{q},\,\mathsf{r},\,\mathsf{t})$

Sol 20: (9) ${}_{5}^{12}B \rightarrow {}_{6}^{12}C^{*}+e^{-}+v$

We take the mass of ${}^{12}_{6}C$ as 12 amu

Rest energy of ${}_{6}^{12}$ C * = 12 × 931.5 MeV + 4.041 MeV

Energy of ${}_{5}^{12}$ B = 12 × 931.5 MeV + 0.014 × 931.5

 \therefore Value of the reaction = 13.041 MeV – 4.041 MeV = 9 MeV

Maximum e^{-} energy = 9 MeV

Sol 21: (A) $5\mu Ci = \frac{ln2}{T_1}(2N_0)$ $10\mu Ci = \frac{ln2}{T_2}(N_0)$

Dividing we get $T_1 = 4T_2$

Sol 22: (A) The electric field at r = R

$$\mathsf{E} = \frac{\mathsf{K}\mathsf{Q}}{\mathsf{R}^2}$$

Q = Total charge within then nucleus = Ze

So,
$$E = \frac{KZe}{R^2}$$

So electric field is independent of a.

Sol 23: (B)
$$q = \int_{0}^{R} \frac{d}{R}(R - x) 4\pi x^{2} dx = Ze$$

 $d = \frac{3Ze}{\pi R^{3}}$

Sol 24: (C) If within a sphere $\,\rho\,$ is constant E $\,\propto\,$ r

Sol 25: (8) N = N₀e<sup>-
$$\lambda$$
t</sup>
In | dN/dt | = In(N₀ λ) - λ t
From graph, $\lambda = \frac{1}{2}$ per year
 $t_{1/2} = \frac{0.693}{1/2} = 1.386$ year
4.16 yrs = 3 $t_{1/2}$
∴ p = 8

Sol 26: (C) KE_{max} of β^{-} $Q = 0.8 \times 10^{6} \text{ eV}$ $KE_{p} + KE_{\beta^{-}} + KE_{\overline{v}} = Q$ KE_{p} is almost zero When $KE_{\beta^{-}} = 0$ Then $KE_{\overline{v}} = Q - KE_{p} \cong Q$

Sol 27: (D)
$$0 \le KE_{\beta^{-}} \le Q - KE_{p} - KE_{\overline{v}}$$

 $0 \le KE_{\beta^{-}} < Q$

Sol 28: (A, C) Given data

$$4.5a_0 = a_0 \frac{n^2}{Z} \qquad ... (i)$$

So possible wavelength are

$$\frac{1}{\lambda_1} = RZ^2 \left[\frac{1}{1^2} - \frac{1}{3^2} \right] \Rightarrow \lambda_1 = \frac{9}{32R}$$
$$\frac{1}{\lambda_2} = RZ^2 \left[\frac{1}{1^2} - \frac{1}{2^2} \right] \Rightarrow \lambda_2 = \frac{1}{3R}$$
$$\frac{1}{\lambda_3} = RZ^2 \left[\frac{1}{2^2} - \frac{1}{3^2} \right] \Rightarrow \lambda_3 = \frac{9}{5R}$$

Sol 29: (C)
$${}_{3}^{6}$$
Li $\rightarrow {}_{2}^{4}$ He $+{}_{1}^{2}$ H
 $\frac{Q}{C^{2}} = 6.015123 - 4.002603 - 2.014102$
 $0 = -0.001582 < 0$
So no α -decay is possible
 ${}_{1}^{2}$ H $+{}_{2}^{4}$ He $\rightarrow {}_{3}^{6}$ Li
 $\frac{Q}{C^{2}} = 2.014102 + 4.002603 - 6.015123 = 0.001582 > 0$
So, this reaction is possible
 ${}_{30}^{70}$ Zn $+{}_{34}^{82}$ Se $\rightarrow {}_{64}^{152}$ Gd
 $\frac{Q}{C^{2}} = 69.925325 + 81.916709 - 151.919803 = -0.077769 < 0$
So this reaction is not possible

Sol 30: (A) $^{210}_{84}$ Po \rightarrow^{4}_{2} He $+^{206}_{82}$ Pb Q = (209.982876 - 4.002603 - 205.97455)C² = 5.422 MeV from conservation of momentum

$$\begin{split} \sqrt{2K_1(4)} &= \sqrt{2K_2(206)} \\ 4K_1 &= 206K_2 \\ \therefore K_1 &= \frac{103}{2}K_2 \\ K_1 + K_2 &= 5.422 \\ K_1 + \frac{2}{103}K_1 &= 5.422 \\ \Rightarrow \frac{105}{103}K_1 &= 5.422 \\ \therefore K_1 &= 5.319 \text{ MeV} &= 5319 \text{ KeV} \\ \hline \text{Sol 31: (C) } P \rightarrow (ii); Q \rightarrow (i); R \rightarrow (iv); S \rightarrow (iii) \\ \frac{15}{8}O \rightarrow_7^{15} N +_1^0 \beta \text{ (Beta decay)} \\ \frac{238}{92}U \rightarrow_{90}^{234} \text{ Th} +_2^4 \text{ He (Alpha decay)} \\ \frac{185}{83}\text{Bi} \rightarrow_{82}^{184} \text{ Pb} +_1^1 \text{H} \text{ (Proton emission)} \\ \frac{239}{94}Ph \rightarrow_{57}^{140} \text{ La} +_{97}^{99} \text{ Rb (fission)} \end{split}$$

Sol 32: (B) $\frac{\lambda_{Cu}}{\lambda_{Mo}} = \left(\frac{Z_{Mo} - 1}{Z_{Cu} - 1}\right)^2$

Sol 33: (B) mvr
$$=\frac{nh}{2\pi}=\frac{3h}{2\pi}$$

de-Broglie Wavelength

$$\lambda = \frac{h}{mv} = \frac{2\pi r}{3} = \frac{2\pi}{3} \frac{a_0(3)^2}{z_{Li}} = 2\pi a_0$$

Sol 34: (B) $\lambda_P = \frac{1}{\tau}$; $\lambda_Q = \frac{1}{2\tau}$
$$\frac{R_P}{R_Q} = \frac{(A_0 \lambda_P) e^{-\lambda_P t}}{A_0 \lambda_Q e^{-\lambda_Q t}}$$

At $t = 2\tau$; $\frac{R_P}{R_Q} = \frac{2}{e}$

Sol 35: (A) Q value of reaction = (140 + 94) × 8.5 –236 × 7.5 = 219 Mev So, total kinetic energy of Xe and Sr = 219 –2 –2 = 215Mev

So, by conservation of momentum, energy, mass and charge, only option (A) is correct

Sol 36: (C)
$$(BE)_{\frac{15}{7}N} = 7 m_p + 8 m_n - m_{\frac{15}{7}N}$$

 $(BE)_{\frac{15}{8}O} = 8 m_p + 7 m_n - m_{\frac{15}{8}N}$
 $\Rightarrow \Delta(BE) = (m_n + m_p) + \left(m_{\frac{15}{8}O} - m_{\frac{15}{7}N}\right)$
 $= 0.00084 + 0.002956 = 0.003796 u$
 $\Rightarrow \frac{3}{5} \times \frac{14 \times 1.44 \text{ MeV f}_m}{0.003796 \times 931.5 \text{ MeV}} = R$
 $\Rightarrow R = 3.42 f_m$

Sol 37: (C) Activity A \propto N (Number of atoms)

$$N = N_0 \left(\frac{1}{2}\right)^n$$

where n \rightarrow Number of half lives

If N =
$$\frac{N_0}{64}$$

N₀ $\left(\frac{1}{2}\right)^n = \frac{N_0}{64}$
 $\left(\frac{1}{2}\right)^n = \frac{1}{64} = \left(\frac{1}{2}\right)^6$
n = 6
time = n × T_{1/2}
time = 6 × 18 days = 108 days