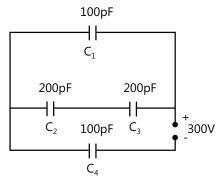
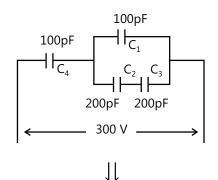
Solved Examples

JEE Main/Boards

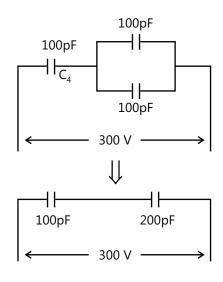
Example 1: Obtain the equivalent capacitance of the network in figure. For a 300V supply, determine the charge and voltage across each capacitor.



Sol: The circuit is made up of series and parallel combinations of the capacitors. The charge on the capacitor is given by q = CV.



The equivalent circuit is as shown below:



Potential difference across $\rm C_4$ and 200 PF is in the ratio 2:1 i.e. 200 V across $\rm C_4$

: Charge on $C_4 = C_4 V_{4:} = 100 \times 200 \times 10^{12} = 2 \times 10^{-8} C$

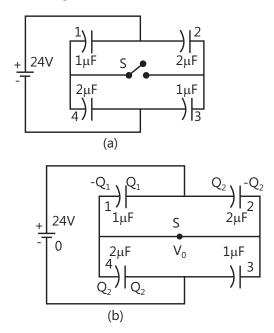
Potential difference across C₁=100V

Charge on $C_1 = C_1 \times V_1 = 100 \times 100 \times 10^{-12} = 1 \times 10^{-8} \text{ C}$

Potential difference across C₂ and C₃ is 50V each

:. Charge on C₂ or C₃ = C₂V₂ = $200 \times 50 \times 10^{12} = 10^{-8}$ C.

Example 2: The connection shown in figure are established with the switch S open. How much charge will flow through the switch if it is closed?



Sol: Find the initial charge on capacitors. After the switch is closed, 1 and 2 become parallel and 3 and 4 become parallel.

When the switch is open, capacitors (2) and (3) are in

series. Their equivalent capacitance is $\frac{2}{3}\mu$ F.

The charge appering on each of these capacitors is,

therefore,
$$24V \times \frac{2}{3}\mu F = 16\mu C$$

The equivalent capacitance of (1) and (4), which are also connected in series, is also $\frac{2}{3}\mu$ F and the charge on each on each of these capacitors is also 16 μ C. The total charge on the two plates of (1) and (4) connected to the switch is, therefore, zero.

The situation when the switch S is closed is shown in figure. Let the charges be distributed as shown in the figure. Q_1 and Q_2 are arbitrarily chosen for the positive plate of (1) and (2).

Take the potential at the negative terminal to the zero and at the switch to be V_0

Writing equations for the capacitors (i), (ii), (iii) and (iv).

 $Q_1 = (24V - V_0) \times 1\mu F$... (i)

 $Q_2 = (24V - V_0) \times 2\mu F$... (ii)

$$Q_1 = V_0 \times 1\mu F \qquad \dots (iii)$$

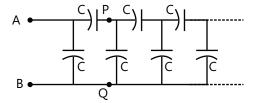
$$Q_2 = V_0 \times 2\mu F \qquad \dots (iv)$$

From (i) and (iii), $V_0 = 12V$, Thus, from (iii) and (iv),

$$Q_1 = 12\mu C$$
 and $Q_2 = 24\mu C$.

The charge on the two plates of (1) and (4) which are connected to the switch is, therefore $Q_2 - Q_1 = 12\mu C$. When the switch was open, this charge was zero. Thus, $12\mu C$ of charge has passed through the switch after it was closed.

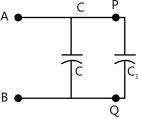
Example 3: Find the capacitance of the infinite ladder shown in figure.



Sol: Capacitance between points P and Q is same as that between A and B. The equivalent capacitance of the circuit is deduced by reducing it to simple network. The simplified circuit is a parallel combination of the capacitors whose capacitance is given by

$$\mathsf{C}_{\mathsf{eq}} = \mathsf{C} + \frac{\mathsf{C}\mathsf{C}_1}{\mathsf{C} + \mathsf{C}_1}.$$

As the ladder is infinitely long, the capacitance of the ladder to the right of the points P, Q is the same as that of the ladder to the right of the points A, B. If the equivalent capacitance of the ladder is C, the given ladder may be replaced by the connections shown in figure.



The equivalent capacitance between A being equivalent to the original ladder, the equivalent capacitance is also C

Thus,
$$C_1 = C + \frac{CC_1}{C + C_1}$$
 or $C_1C + C_1^2 = C^2 + 2CC_1$
Or $C_1^2 - CC_1 - C^2 = 0$,
Giving $C_1 = \frac{C + \sqrt{C^2 + 4C^2}}{2} = \frac{1 + \sqrt{5}}{2}C$

Negative value of C_1 is rejected.

Example 4: A parallel-plate capacitor has plates of area 200 cm² and separation between the plates 1.00 mm. What potential difference will be developed if a charge of 1.00 nC (i.e., 1.00×10^{-9} C) is given to the capacitor? If the plate separation is now increased to 2.00 mm, what will be the new potential difference?

Sol: Capacitance is given by $C = \frac{\epsilon_0 A}{d}$ and the potential difference is given by $V = \frac{Q}{C}$

The capacitance of the capacitor is

$$C = \frac{\varepsilon_0 A}{d} = 8.85 \text{x} 10^{-12} \text{Fm}^{-1} \text{x} \frac{200 \text{x} 10^{-4} \text{m}^2}{1 \text{x} 10^{-3} \text{m}}$$

$$= 0.177 \times 10^{-9} F = 0.177 n F$$

The potential difference between the plates is

$$V = \frac{Q}{C} = \frac{1nC}{0.177nF} = 5.65$$
 Volts

If the separation is increased from 1.00 mm to 2.00 mm, the capacitance is decreased by a factor of 2. Thus, the new potential difference will be 5.65 volts \times 2 = 11.3 volts.

Example 5: An isolated sphere has a capacitance of 50pF.

(a) Calculate its radius.

(b) How much charge should be placed on it to raise its potential to 10^4 V?

Sol: For sphere, radius R is given by $C = 4\pi\epsilon_0 R$. To raise the potential to 10^4 V, the charge to be placed on sphere is given by Q = CV.

(a) The capacitance of an isolated sphere is

$$C = 4\pi\varepsilon_0 R. \text{ Thus, } 50 \times 10^{-12} \text{ F} = \frac{R}{9 \times 10^9 \text{ m} \text{ F}^{-1}}$$

$$Or R = 5000 X900 III = 450III.$$

(b)
$$Q = CV = 50X10^{-12}FX10^4 V = 0.5\mu C$$

Example 6: A parallel-plate capacitor of capacitance $100 \,\mu\text{F}$ if connected to a power supply of 200V. A dielectric slab of dielectric constant 5 is now inserted into the gap between the plates.

(a) Find the extra charge flown through the power supply and the work done by the supply.

(b) Find the charge in the electrostatic energy of the electric field in the capacitor.

Sol: After inserting the dielectric the capacitance is changed, thus the charge stored in the capacitor is given by Q = CV and work done by supply is $CV^2 = qV$.

The energy stored in the capacitor is given by
$$U = \frac{1}{2}CV^2$$

(a) The original capacitance was 100μ F. The charge on the capacitor before the insertion of the dielectric was, therefore, $Q_1 = 1000F \times 200V = 20mC$

After the dielectric slab is introduced, the capacitance is increased to 500μ F. The new charge on the capacitor is,

Therefore, $500\mu F x 200\nu = 100mC$.

The charge flown through the power supply is, therefore, 100 mC - 20 mC = 80 mC.

The work done by the power supply is $200V \times 80mC = 16J$.

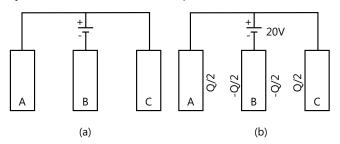
(b) the electrostatic field energy of the capacitor without the dielectric slab is

$$U_{1} = \frac{1}{2}CV^{2} = \frac{1}{2}(100\mu F)X(200V) = 2J$$

And that after the slab is inserted is

 $U_2 = \frac{1}{2} (500 \mu F) X (200 V)^2 = 10 J$ thus, the energy is increased by 8J.

Example 7: Each of the three plates shown in figure has an area of 200cm² on one side and the gap between the adjacent plates is 0.2mm. The emf of the battery is 20V. Find the distribution of charge on various surfaces of the plates. What is the equivalent capacitance of the system between the terminal points?



Sol: As the charge distribute symmetrically around the central plate. Due to this there is equal amount

of charge induced in other plates. The capacitance is

between any two surfaces is given by $C = \frac{A\epsilon_0}{d}$.

Suppose the negative terminal of the battery gives a charge – Q to the plate B. As the situation is symmetric on the two sides of B, the two faces of the plate B will share equal charge – Q/2 each. From Gauss's law, the facing surfaces will have charge Q/2 each. As the positive terminal of the battery has supplied just this much charge (+Q) to A and C, the outer surfaces of A and C will have no charge. The distribution will be as shown in figure. The capacitance between the plates A and B is

$$C = \frac{A\epsilon_0}{d} = 8.85 \times 10^{-12} \text{ F} / \text{m} \times \frac{200 \times 10^{-4} \text{ m}^{-2}}{2 \times 10^{-4} \text{ m}}$$
$$= 8.85 \times 10^{-10} \text{ F} = 0.885 \text{ nF}$$

Thus, Q = 8.85 nF x 20V = 17.7 nC

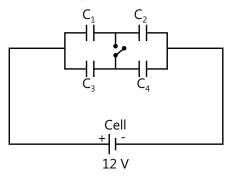
The distribution of charge on various surfaces may be written from figure.

The equivalent capacitance is $\frac{Q}{20V} = 1.77 nF$

Example 8: The emf of the cell in the circuit is 12 volts and the capacitors are: $C_1 = 1\mu$ F, $C_2 = 3\mu$ F, $C_3 = 2\mu$ F, $C_4 = 4\mu$ F

Calculate the charge on each capacitor and the total charge drawn from the cell when

- (a) The switch s is closed
- (b) The switch s is open.



Sol: When the switch is closed the equivalent capacitance is given by $C = \frac{(C_1 + C_3)(C_2 + C_4)}{(C_1 + C_3) + (C_2 + C_4)}$

and the charge stored in the circuit is given by Q=CV. When the switch is open the capacitance is given

by $C = \frac{C_1C_2}{C_1 + C_2} + \frac{C_3C_4}{C_3 + C_4}$. The charge stored in the

capacitor is given by

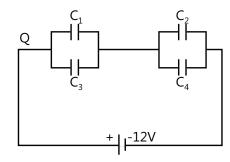
(a) Switch S is closed:

$$C = \frac{(C_1 + C_3)(C_2 + C_4)}{(C_1 + C_3) + (C_2 + C_4)}; \quad C = \frac{3 \times 7}{3 + 7} = 2.1 \mu F;$$

Total charge drawn from the cell is:

 $Q = CV = 2.1 \mu F \times 12 \text{ volts} = 25.2 \mu C$

 C_1 , C_3 are in parallel and C_2 , C_4 are in parallel.



Charge on C₁

$$Q_1 = \frac{C_1}{C_1 + C_3} Q = \frac{1}{1 + 2} \times 25.2 \mu C = 8.4 \mu C$$

Charge on C,

$$Q_3 = \frac{C_3}{C_1 + C_3}Q = \frac{2}{1 + 2} \times 25.2\mu C = 16.8\mu C$$

Charge on C,

$$Q_2 = \frac{C_2}{C_2 + C_4}Q = \frac{3}{3+4} \times 25.2\mu C = 10.8\mu C$$

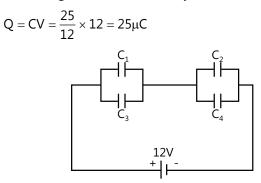
Charge on C

$$Q_4 = \frac{C_4}{C_2 + C_4}Q = \frac{4}{3+4} \times 25.2\mu C = 14.4\mu C$$

(c) switch S is open :

$$C = \frac{C_1 C_2}{C_1 + C_2} + \frac{C_3 C_4}{C_3 + C_4} C = \frac{1X3}{1+3} + \frac{2X4}{2+4} = \frac{25}{12} \mu F$$

Total charge drawn from battery is:



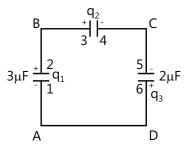
C₁ and C₂ are in series and the potential difference across combination is 12 volts charge on

$$C_{1} = \text{charge on } C_{2}$$
$$= \left(\frac{C_{3}C_{4}}{C_{3}+C_{4}}\right) V = \frac{8}{6} \times 12 = 16\mu C_{2}$$

 $C_3 \& C_4$ are in series and the potential difference across combination is 12 volts charge on

$$C_{3} = \text{charge on } C_{4}$$
$$= \left(\frac{C_{3}C_{4}}{C_{3} + C_{4}}\right) V = \frac{8}{6} \times 12 = 16 \mu C$$

Example 9: Two capacitors A and B with capacities 3 µF and $2 \mu F$ are changed to a potential difference of 100V and 180V respectively. The plates of the capacitors are connected as shown in the figure with one wire of each capacitor free. The upper plate of A is positive and that of B is negative. An uncharged $2\mu F$ capacitor C with lead wires falls on the free ends to complete the circuit. Calculate:



(i) The final charge on the three capacitors, and

(ii) The amount of electrostatic energy stored in the system before and after the completion of the circuit.

Sol: The charge stored in each capacitor when they are not connected to each other is given by q = CV. When the capacitors are connected to each other then the charge stored in each the capacitor is obtained by applying Kirchoff's 2nd law to the circuit. The energy

stored in the

capacitor is given by
$$U = \frac{1}{2}CV^2$$

(i) charge on capacitor A, before joining with an uncharged capacitor,

 $q_{\Delta} = CV = (100) + 3\mu c = 300\mu c$

Similarly charge on capacitor B,

 $q_{B} = 180 \times 2\mu c = 360\mu c$

Let q_1 , q_2 and q_3 be the charges on the three capacitors after joining them as shown.

From conservation of charge,

Net charge on plates 2 and 3 before joining

= Net charge after joining

$$\therefore 300 = q_1 + q_2$$
 (i)

Similarly, net charge on plates 4 and 5 before

Joining = Net charge after joining

 $-360 = -q_2 - q_3$; $360 = q_2 + q_3$ (ii)

Applying Kirchoff's 2nd law in loop ABCDA,

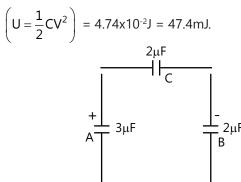
$$\frac{q_1}{3} - \frac{q_2}{2} + \frac{q_3}{2} = 0$$

2q₁ - 3q₂ + 3q₃ = 0 (iii)

From equations (i), (ii) and (iii),

$$q_1 = 90\mu C, q_2 = 90\mu C$$
 and $q_3 = 150\mu C$

(iii) (a) Electrostatic energy stored before completing the circuit,



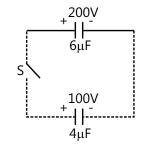
(b) Electrostatic energy stored after completing the circuit,

$$U_{f} = \frac{1}{2} (90 \times 10^{-6})^{2} \frac{1}{3 \times 10^{-6}}$$
$$+ \frac{1}{2} (90 \times 10^{-6})^{2} \frac{1}{2 \times 10^{-6}}$$
$$+ \frac{1}{2} (150 \times 10^{-6})^{2} \frac{1}{2 \times 10^{-6}}; \quad \left(U = \frac{1}{2} \frac{q}{c^{2}} \right)$$
$$= 90 \times 10^{-4} \text{ J} = 90 \text{ mJ}$$

Example 10: A capacitor of capacitance $4 \mu F$ is charged to a potential difference of 100V and another of capacitance $6 \mu F$ is charged to a potential of 200V. These capacitances are now joined with plates of like charges connected together. Calculate:

- (a) The total potential across each after joining
- (b) The total electrical energy stored before joining

(c) The total electrical energy stored after joining



How do you account for the difference in energies in (b) and (c) ?

Sol: When the capacitors are connected to each other then the total charge stored in the circuit is given by $Q = Q_1 + Q_2 = C_1V_1 + C_2V_2$. The energy stored in each capacitor is given by $U = \frac{1}{2}CV^2$.

$$V_1 = 100V, C_1 = 4\mu F, Q_1 = C_1V_1 = 4 \times 10^{-6} \times 100$$

= 4 × 10⁻⁴ C; V₂ = 200V, C₂ = 6\mu F
Q₂ = C₂V₂ = 6X10⁻⁶ × 200 = 12 × 10⁻⁴ C

When the plates with like charges are connected together, both capacitors have the same potential after redistribution of charge.

(a) Total charge = $Q = Q_1 + Q_2$

$$= (4+12) \times 10^{-4} 1.6 \times 10^{-3} C$$

Capacitance of the combination in parallel

$$= C = C_1 + C_2 = (4+6)\mu F = 10\mu F$$

Potential across each capacitor after joining

$$= V = \frac{q}{C} = \frac{1.6 \times 10^{-3}}{10 \times 10^{-6}} = 160V$$

(b) Electrical energies U_1 and U_2 before joining are given as :

$$U_{1} = \frac{1}{2}C_{1}V_{1}^{2} = \frac{1}{2} \times (4X10^{-6}) \times (100)^{2} = 2X10^{-2} J$$
$$U_{2} = \frac{1}{2}C_{2}V_{2}^{2} = \frac{1}{2} \times (6X10^{-6}) \times (200)^{2} = 12X10^{-2} J$$

Energy before joining

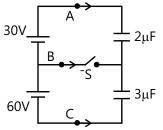
$$= U_i = U_1 + U_2; = (12 + 2) \times 10^{-2} = 0.14 J$$

(c) Electrical energy after joining of capacitors

$$= U_{f} = \frac{1}{2} \times 10 \times 0^{-6} \times (160)^{2} = 0.128 J$$

The stored electrical energy after joining is less by (0.14-0.128) J i.e. 0.012J. the energy is dissipated as heat energy through the connecting wires as current flows.

Example 11: What charges will flow thorugh A, B and C in the directions shown in Fig. 19.69 when switch S is closed?

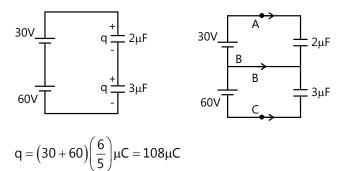


Sol: The charges stored in capacitor is given by Q = CV. The equivalent capacitance is $C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$. To find the charges flowing in each capacitor we use the Kirchoff's 2nd law.

Let us draw two figures as shown in figure and find the charge on both the capacitors before closing the switch and after closing the switch. Refer figure (a) when switch is open: both capacitors are in series. Hence, their equivalent capacitance is,

$$C_{eq} = \frac{C_1 C_2}{C_1 + C_2} = \frac{(2)(3)}{2+3} = \frac{6}{5} \mu F$$

Therefore, charge on both capacitors will be same. Hence, using q = CV, we get



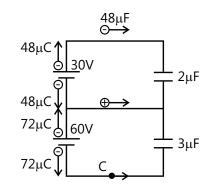
Refer figure (b), when switch is closed: let q_1 and q_2 be the charges (in μ C) on two capacitors. Then applying Kirchoff's 2nd law in upper and lower loop, we have

$$30 - \frac{q_1}{2} = 0$$
 Or $q_1 = 60\mu$ C;
 $60 - \frac{q_2}{3} = 0$ Or $q_2 = 180\mu$ C

Charges q_1 and q_2 can be calculated alternatively by seeing that upper plate of $2 \mu F$ capacitor is connected with positive terminal of 30V battery. Therefore, they are at the same potential. Similarly, the lower plate of this capacitor is at the same potential as that of the negative terminal of 30V battery. So, we can say that P.D. across $2 \mu F$ capacitor is also 30V. $q_1 = (C)(P.D) = (2)(30)\mu C$

Similarly, P.D. across 3μ F capacitor is same as that between 60V battery. Hence, $q_2 = (3)(60) = 180\mu$ C. Now let q_A charge goes to the upper plate of 2μ F capacitor. Initially it had a charge +q and finally charge on it is + q_1 . Hence, $q_1 = q + q_A$ or $q_A = q_1 - q = 60 - 180$

 $= -48 \mu C$



Similary, charge q_B goes to the upper plate of $3 \mu F$ capacitor and lower plate of $2 \mu F$ capacitor. Initially both the plates had a charge +q, -q or zero. And finally they have a charge $(q_2 - q_1)$.

Hence,
$$q_2 - q_1 = q_B + 0$$

$$\therefore q_{\rm B} = q_2 - q_1$$
$$= 180 - 60$$

= 120μ C Initially it had a charge-q and finally $-q_2$.

Hence, $qc = q - q_2 = 108 - 180 = -72\mu C$

Example 12: If 100 volts of potential difference is applied between a and b in the circuit of figure, find the potential difference between c & d.

Sol: The charge stored in each capacitor is given by Q = CV. To find the potential difference at point's c and d we apply Kirchoff's law to the circuit.

The charge distribution on different plates is shown in figure. Suppose charge $Q_1 + Q_2$ is given by the positive terminal of the battery, out of which Q_1 resides on the positive plate of capacitor (1) and Q_2 on that of (2). The remaining plates will have charges as shown in the figure. Take the potential at the point b to be zero. The potential at a will be 100V. Let the potentials at points c and d be V_c and V_d respectively. Writing the equation Q=CV for the four capacitors, we get,

$$Q_1 = 6\mu F \times 100V = 600\mu C$$
(i)

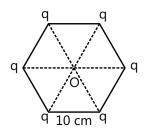
- $Q_2 = 6\mu F \times (100V V_c)$ (ii)
- $Q_2 = 6\mu F \times V_{d-} \qquad \qquad \dots (iv)$

From (ii) and (iii)
$$100V - V_c = V_c - V_d$$

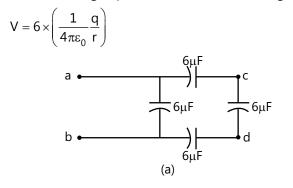
or $2V_c - V_d = 100V$ (v)
And from (iii) and (iv) $V_c - V_d = V_d$
or $V_c = 2V_{d-}$ (vi)
From (v) and (vi)
From (v) and (vi) $V_d = \frac{100}{3}V$ and $V_c = \frac{200}{3}V$

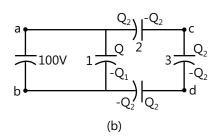
So that $V_c - V_d = \frac{100}{3}V$

Example.13 A regular hexagon of side 10 cm has a charge $5 \mu C$ at each of its vertices. Calculate the potential at the center of the hexagon.



Sol: The potential at the center of the hexagon is due to 6 charges placed at its vertices. It is given by



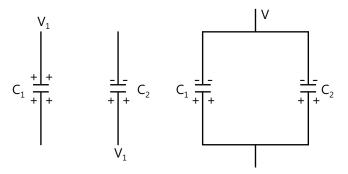


Total potential at O is given by,

$$V = 6 \times \left(\frac{1}{4\pi\epsilon_0} \frac{q}{r}\right) = 6 \times (9 \times 10^9) \times \frac{5 \times 10^{-6}}{0.1} = 2.7 \times 10^6 \text{ volt.}$$

JEE Advanced/Boards

Example 1: Two capacitors $C_1 = 1\mu F$ and $C_2 = 4\mu F$ are charged to a potential difference of 100 volts and 200 volts respectively. The charged capacitors are now connected to each other with terminals of opposite sign connected together. What is the



- (a) Final charge on each capacitor in steady state?
- (b) Decrease in the energy of the system?

Sol: The capacitors are connected parallel to each other. Thus the equivalent capacitance is given by $C = C_1 + C_2$. The charges stored in capacitor is given by Q = CV. The

energy stored in each capacitor is given by $U = \frac{1}{2}CV^2$.

initial charge on $C_1 = C_1 V_1 = 100 \mu F$;

Initial charge on $C_2 = C_2 V_2 = 800 \mu F$; $C_1 V_1 < C_2 V_2$

When the terminals of opposite polarity are connected together, the magnitude of net charge finally is equal to the difference of magnitude of charges before connection.

(Charge on C_2)_i (charge on C_1)_i

= (charge on C_2)_f - (charge on C_1)_f

Let V be the final common potential difference across each.

The charges will be redistributed and the system attains a steady state when potential difference across each capacitor becomes same.

$$C_2V_2 - C_1V_1 = C_2V + C_1V_1$$

$$V = \frac{C_1 V_2 - C_1 V_2}{C_2 + C_1} = \frac{800 - 100}{5} = 140 \text{ volts}$$

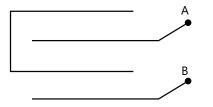
Note that because $C_1V_1 < C_2V_2$, the final charge polarities are same as that of C_2 before connection.

Final charge on $C_1 = C_1 V = 140 \mu C$ Final charge on $C_2 = C_2 V = 560 \mu C$ Loss of energy= $U_i - U_f$ Loss of energy

$$= \frac{1}{2}C_{1}V_{1}^{2} + \frac{1}{2}C_{2}V_{2}^{2} - \frac{1}{2}C_{1}V^{2} - \frac{1}{2}C_{2}V^{2}$$
$$= \frac{1}{2}1(100)^{2} + \frac{1}{2}4(200)^{2} - \frac{1}{2}(1+4)(140)^{2}$$
$$= 36000\mu J = 0.036 J$$

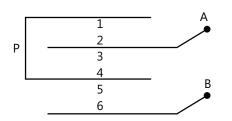
Note: the energy is lost as heat in the connected wires due to the temporary currents that flow while the charge is being redistributed.

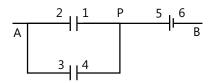
Example 2: Four identical metal plates are located in the air at equal separation d as shown. The area of each plate is a. Calculate the effective capacitance of the arrangement across A and B.



Sol: The plates are connected in parallel combination with each other. The equivalent capacitance is given by $C = C_1 + C_2 + C_3$. The capacitance between A and B is

given by $C_{AB} = \frac{2C}{3}$

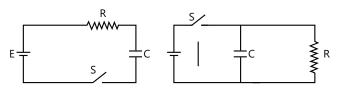




Let us call the isolated plate as P.A capacitor is formed by a pair of parallel plates facing each other. Hence we have three capacitor formed by the pairs (1,2), (3,4) and (5,6). The surface 2 and 3 are at same potential as that of A. The arrangement can be redrawn as a network of three capacitors.

$$C_{AB} = \frac{2C}{3} = \frac{2\varepsilon}{3} \frac{A0}{d}$$

Example 3: A 10 μ F condenser C is charged through resistance R of 0.1 M Ω from a battery of 1.5V. Find the time required for the capacitor to get charged upto 0.75V for the circuits shown below.



Sol: For RC circuit, the charge stored in the capacitor is given by $q = q_0 \left[1 - e^{-t/RC} \right]$. Taking log on both sides we can get the value of time t.

(a) In the case of charging of a capacitor C through the resistance R,

$$q = q_0 \left[1 - e^{-t/RC} \right]; \quad e^{-t/RC} = 1 - \frac{q}{q_0}$$

For a capacitor, $q = CV \frac{q}{q_0} = \frac{V}{V_0} = \frac{0.75}{1.5} = \frac{1}{2}$

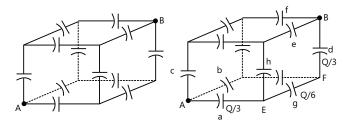
 $t = RClog_e 2 = (0.1 \times 10^6) \times (10 \times 10^{-6}) \log_e 2$

 $t = RClog_e 2 = 0.693$ second.

(b) In the case of the capacitor C being connected directly to the battery initially, it acts like short circuit. The capacitor will get charged instantaneously at t = 0 secs.

Hence, time cannot be calculated as per the requirement of the question.

Example 4: Twelve capacitors, each having a capacitance C, are connected to form a cube. Find the equivalent capacitance between the diagonally opposite corners such as A and B.



Sol: Applying the Kirchoff's second law across diagonal points A and B to find the charge distribution across the branch of the circuit, and find the equivalent capacitance.

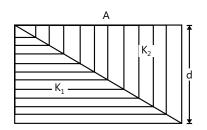
Suppose the points A and B are connected to a battey. The charges appearing on some of the capacitors are shown in figure suppose the positive terminal of the battery supplies a charge +Q through the point A. This charge is divided on the three plates connected to A. Looking from A, the three sides of the cube have identical properties and hence, the charge will be equally distributed on the three plates. Each of the capacitors a, b and c will receive a charge Q/3. The negative terminal of the battey supplies a charge -Q through the point B. This is again divided equally on the three plates connected to B. Each of the capacitors d, e and f gets equal charge Q/3.

Now consider the capacitors g and h. As the three plates connected to the point E form an isolated system, their total charge must be zero. The negative plate of the capacitor has a charge -Q/3. The two plates of g and h connected to E should have a total charge Q/3. By symmetry, these two plates should have equal charges and hence each of these has a charge Q/6. The capacitors a, g and d have charges Q/3, Q/6 and Q/3 respectively.

We have,
$$V_A - V_B = (V_A - V_E) + (V_E - V_F) + (V_F - V_B)$$

= $\frac{Q/3}{C} + \frac{Q/6}{C} + \frac{Q/3}{C} = \frac{5Q}{6C}$
 $C_{eq} = \frac{Q}{V_A - V_B} = \frac{6}{5}C.$

Example 5: The Capacitance of a parallel plate capacitor with plate area A and separation d is C. The space between the plates is filled with two wedges of dielectric constants K_1 and K_2 respectively (figure). Find the capacitance of the resulting capacitor.



Sol: As represented in the figure the dielectric material are connected in series with each other across diagonal.

Consider one thin strip of the capacitor. The equivalent

capacitance is given by $\frac{1}{dC} = \frac{1}{dC_1} + \frac{1}{dC_2}$.

These strips are connected to each other parallely such that the equivalent capacitance of the capacitor is given by

$$C = \int_{x=0}^{x=L} dC$$

Let length and breadth of the capacitor be I and b respectively and d be the distance between the plates as shown in figure then consider a strip at a distance x of width dx.

Now QR=x tan
$$\theta$$

And PQ = d-x tan θ ; where

tan
$$\theta = d/l$$
,Capacitance of PQ
 $\leftarrow L$
 A
 b

$$dC_{1} = \frac{k_{1}\epsilon_{0}(b \, dx)}{d - x \tan \theta} = \frac{k_{1}\epsilon_{0}(b \, dx)}{d - \frac{xd}{l}}$$
$$dC_{1} = \frac{k_{1}\epsilon_{0}b / dx}{d(l - x)} = \frac{k_{1}\epsilon_{0}A}{d(l - x)}$$
And
$$dC_{2} = \text{capacitance of QR} \quad dC_{2} = \frac{k_{2}\epsilon_{0}b(dx)}{d \tan \theta}$$
$$dC_{2} = \frac{k_{2}\epsilon_{0}A(dx)}{Xd} \quad \dots \left\{ \therefore \tan \theta = \frac{d}{l} \right\}$$

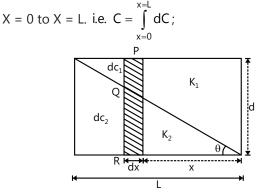
Now dC_1 and dC_2 are in series. Therefore, their resultant capacity dC will be given by

;

$$\frac{1}{dc} = \frac{1}{dC_1} + \frac{1}{dC_2}, \quad \text{then } \frac{1}{dC} = \frac{d(l-x)}{K_1 \varepsilon_0 A(dx)} + \frac{X.d}{K_1 \varepsilon_0 A(dx)}$$
$$\frac{1}{dc} = \frac{d}{\varepsilon_0 A(dx)} \left(\frac{l-x}{K_1} + \frac{X}{K_2} \right) = \frac{d\left[K_2(l-x) + K_1 X\right]}{\varepsilon_0 A K_1 K_2(dx)}$$
$$dC = \frac{\varepsilon_0 A K_1 K_2}{d\left[K_2(l-x) + K_1 X\right]} dx, dC = \frac{\varepsilon_0 A K_1 K_2}{d\left[K_2 l + (K_1 - K_1) X\right]} dx$$

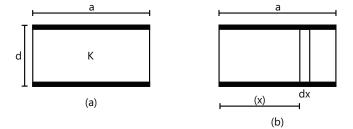
All such elemental capacitor representing DC are connected in parallel.

Now the capacitance of the given parallel plate capacitor is obtained by adding such infinitesimal capacitors parallel from



$$= \int_{0}^{L} \frac{\epsilon_0 A K_1 K_2}{d \left[K_2 I + \left(K_1 - K_2 \right) X \right]} dx \ ; \ C = \frac{K_1 K_2 \epsilon_0 A}{\left(K_1 - K_2 \right) d} In \frac{K_2}{K_1}$$

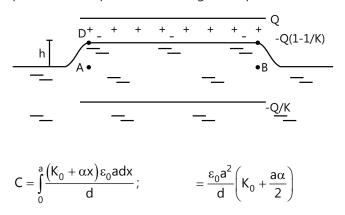
Example 6: Figure (a) shows a parallel-plate capacitor having square plates of edge a and plate-separtion d. The gap between the plates is filled with a dielectric medium of dielectric constant K which varies parallel to an edge as $K = K_0 + ax$



Where K and α are constants and x is the distance from the left end. Calculate the capacitance.

Sol: As the medium varies, consider a small strip of the dielectric medium such that its capacitance is $dC = \frac{(K_0 + \alpha x)\varepsilon_0 adx}{d}$. These strips are connected in parallel so the equivalent capacitance is given by $C = \int_0^a dC$ where a is the length of plates. Consider a small strip of width dx at a separation x from the left end. This strip forms a small capacitor of plate area adx. Its capacitance is $dC = \frac{(K_0 + \alpha x)\varepsilon_0 adx}{d}$

d The given capacitor may be divided into such strips with x varying from 0 to A. All these strips are connected in parallel. The capacitance of the given capacitor is,



Example 7: A parallel-plate capacitor is placed in such a way that its plates are horizontal and the lower plate is dipped into a liquid of dielectric constant K and density ρ . Each plate has an area A. the plates are now

connected to a battery which supplies a positive charge of magnitude Q to the upper plate. Find the rise in the level of the liquid in the space between the plates.

Sol: The dielectric liquid experiences a electric force due to which it rises to the height h. This force is balanced by weight of liquid.

The situation is shown in figure. A charge
$$-Q\left(1-\frac{1}{K}\right)$$
 is
induced on the upper surface of the liquid and $Q\left(1-\frac{1}{K}\right)$
at the surface in contact with the lower plate. The net
charge on the lower plate is $-Q + Q\left(1-\frac{1}{K}\right) = -\frac{Q}{K}$.

Consider the equilibrium of the liquid in the volume

ABCD. The forces on this liquid are

- (a) The force due to the electric field at CD,
- (b) The weight of the liquid,
- (c) The force due to atmospheric pressure and
- (d) The force due to the pressure of the liquid below AB.

As AB is in the same horizontal level as the outside surface, the pressure here is the same as the atmospheric pressure. The forces in (c) and (d), therefore, balance each other. Hence, for equilibrium, the forces in (a) and (b) should balance each other.

The electric field at CD due to the charge Q is $E_1 = \frac{Q}{2A\varepsilon_0}$

In the downward direction.

The field at CD due to the charge –Q/K is $E_2 = \frac{Q}{2A\epsilon_0 K}$

Also in the downward direction.

The net field at CD is $E_1 + E_2 = \frac{(K+1)Q}{2A\epsilon_0 K}$.

The force on the charge $-Q\left(1-\frac{1}{K}\right)$ at CD is

$$\mathsf{F} = \mathsf{Q}\left(1 - \frac{1}{\mathsf{K}}\right) \frac{(\mathsf{K} + 1)\mathsf{Q}}{2\mathsf{A}\varepsilon_0\mathsf{K}}; \quad = \frac{\left(\mathsf{K}^2 - 1\right)\mathsf{Q}^2}{2\mathsf{A}\varepsilon_0\mathsf{K}^2}$$

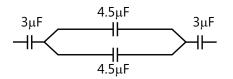
In the upward direction. The weight of the liquid considered is $hA\rho g$.

thus,
$$hA\rho g = \frac{(K^2 - 1)Q^2}{2A\epsilon_0 K^2}$$
; or $h = \frac{(K^2 - 1)Q^2}{2A^2 K^2 \epsilon_0 \rho g}$

JEE Main/Boards

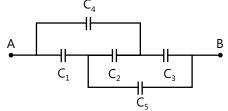
Exercise 1

Q.1 Calculate the equivalent capacitance in the following circuit

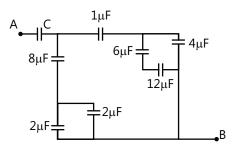


Q.2 Find the potential of a sphere having charge of $5 \,\mu C$ and capacitance of 1nF.

Q. 3 Find the equivalent capacitance between A and B in the given figure. Take $C_2 = 10\mu F$ and B in the given figure. Take $C_2 = 10\mu F$ and C_1, C_3, C_4, C_5 each equal to $4\mu F$



Q.4 Find the value of C if the equivalent capacitance between the points A and B in the given figure is 1μ F

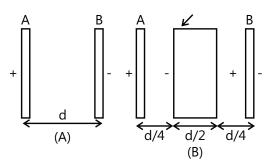


Q.5 A 4x10⁻⁶F capacitor is charged by a 200V supply. It is then disconnected from the supply and is connected across another uncharged 2x10⁻⁶F capacitor. How much energy of the first capacitor is lost?

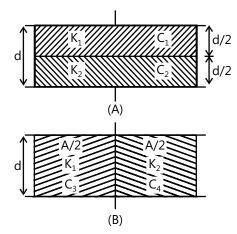
Q.6 The plates of a parallel plate capacitor of area 100cm² each and are separated by 2.0mm. The capacitor is charged by a 100V supply. Find energy store by the capacitor.

Q.7 What capacitance is required to store an energy of 100kW h at a potential difference of 10^4 V?

Q.8 A capacitor is filled with two dielectrics of the same dimensions but of dielectric constants 2 and 3 respectively. Find the ratio of capacitances in the two arrangements shown in figure A and B.



Q.9 Two metal plates separated by a distance d constitute a parallel plate capacitor. A metal slab of thickness (d/2) and same area as the plate is inserted between the plates. What is the ratio of the capacitances in the two cases?



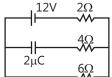
Q.10 Keeping the voltage of the charging source constant, what would be the percentage change in the energy stored in a parallel plate capacitor if the separation between its plates were to be decreased by 10%?

Q.11 A parallel plate air capacitor with its plates spaced 2cm apart is charged to a potential of 300 volts. What will be the electric field intensity inside the capacitor, if the plates are moved apart to a distance of 5cm without disconnecting the power source? Calculate the change in energy of the capacitor. Area of the plates is equal to A = 100cm². Also solve the problem assuming

the entire operation was done after disconnecting the power source. Account for the change in energy in both

the cases. $(\in_0 = 9 \times 10^{-12} \text{ SI units})$

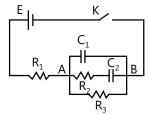
Q.12 Find the charge on the capacitor C in the following circuit in steady state.



Q.13 Three uncharged capacitors of capacitance C_1, C_2 and C_3 are connected as shown in figure to one another and to points A, B and D potentials (ϕ_A), (ϕ_B) and (ϕ_D). Determine the potential (ϕ_A) at point O.



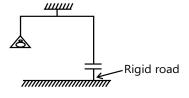
Q.14 Determine the current through the battery in the circuit shown.



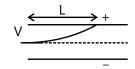
(i) Immediately after the key K is closed and

(ii) In a long time interval, assuming that the parameters of the circuit are known.

Q.15 The lower plate of a parallel plate capacitor lies on an insulating plane. The upper plate is suspended from one end of a balance. The two plates are joined together by a thin wire and subsequently disconnected. The balance is then counterpoised. A voltage V=5000 volt is applied between the plates. What additional mass should be placed to maintain balance? The distance between the plates is d=5mm and the area of each plate is A=100cm²? [all the elements other than plates are massless and nonconducting]

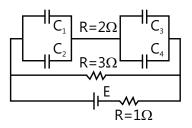


Q.16 Two charge particulars one is electron and other is negatively charged ion have a velocity directed parallel to the plates. They are sent separately into the field. Both the electron and the ion have reveived their initial kinetic energy by passing the same potential difference. Which of the two particles will travel a greater distance (parallel to plates shown by 'l') before hitting the positively charged plate, if both fly into the capacitor at a point that is exactly in the middle of the distance between the plates?



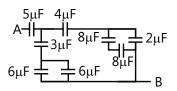
Q.17 A 3μ F capacitor is charged to a potential of 300 volt and 2μ F is charged to 200 volt. The capacitor are connected so that the plates of same polarity are connected together. What is the final potential difference between the plates of the capacitor after they are connected? If instead of this the plates of opposite polarity were joined together, what amount of charge will flow and from which capacitor does it come?

Q.18 In the following circuit, internal resistance of the battery $r = 1\Omega$.



 $E = 4V, C_1 = 8\mu F, C_2 = 2\mu F, C_3 = 6\mu F, C_4 = 4\mu F.$ Find the charge on plate of each capacitor.

Q.19 In the network given in the figure a potential difference of 10 volts is applied across the two points A and B find;



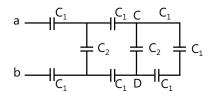
- (i) The potential difference across the capacitor of $2\,\mu\text{F}$.
- (ii) The charge in both of $6 \mu F$ capacitors.

Q.20 In the figure shown here, each capacitance C_1 in the network is $3 \mu F$ and each capacitance C_2 is $2\mu F$

(i) Compute the equivalent capacitance of the network between the points a and b.

(ii) Calculate charge on each capacitors nearest to a and b when V_{ab} =900volt.

(iii) With 900 volt across a and b, compute $\rm V_{\rm cd}$



Q.21 If you have serval $2.0 \,\mu$ F capacitors, each capable of withstantding 200 volts without breakdown, how would you assemble a combination having an equivalent capacitance of;

(a) 0.40 µF or of

(b) $1.2 \,\mu\text{F}$, each capable of withstanding 100 volts.

Q.22 Six $1 \mu F$ capacitors are so arranged that their equivalent capacitance is $0.70 \mu F$. If a potential difference of 600 volt is applied to the combination, what charge will appear on each capacitor?

Q.23 Two condensers are in parallel and the energy of the combination is 10^3 J, when the difference of potential between their terminals is 2 volts. With the same two condensers in series, the energy is 1.6×10^2 J for the same differences of potential across the series combination. What are their capacities?

Q.24 A capacitor of capacitance $C_1 = 1.0 \,\mu\text{F}$ charged upto a voltage V = 110V is connected in a parallel to the terminals of a circuit consisting of two uncharged capacitor connected in series and possessing the capacitance $C_2 = 2.0 \,\mu\text{F}$ and $C_3 = 3.0 \,\mu\text{F}$. What charge will flow through the connecting wires?

Q.25 Two capacitors A and B are connected in series across a 100V supply and it is observed that the potential difference across them are 60V and 40V. A capacitor of 2μ F capacitance is now connected in parallel with A and the potential difference across with A and the potential difference across B rise to 90V. Determine the capacitance of A and B.

Q.26 A capacitor of capacitance $C_1 = 1.0 \mu F$ withstands the maximum voltage $V_1 = 6.0$ kV while a capacitor of capacitance $C_2 = 2.0 \mu F$ withstands maximum voltage $V_2 = 4.0$ kV. What voltage will the system of these two capacitors withstand, if they are connected in series?

Q.27 Two identical parallel plate air capacitors are connected in one case in parallel and in the other in series. In each case the plates of one capacitor are brought closer together by a distance a and the plates of the other are moved apart by the same distance a. How will the total capacitance of each system change as result of such manipulation ?

Q.28 A 3 mega ohm resistor and $1 \mu F$ capacitor are connected in a single loop circuit with a source of constant 4 volt. At one second after the connection is made what are the rates at which;

- (i) The charge on the capacitor is increasing
- (ii) Energy is being stored in the capacitor
- (iii) Joule heat is appearing in the resistor
- (iv) Energy is being delived by the source

Q.29 A capacitor of capacity $1 \,\mu\text{F}$ is connected in closed series circuit with a resistance of 10^7 ohms, an open key and a cell of 2V with negligible internal resistance:

(i) When the key is switched on at time t=0, find;

(a) The time constant for the circuit.

(b) The charge on the capacitor at steady state.

(c) Time taken to deposit charge equaling half that at steady state.

(ii) If after fully charging the capacitor, the cell is shorted by zero resistance at time t=0, find the charge on the capacitor at t = 50s.

Q.30 An electric dipole, when held at 30° with respect to a uniform electric field of 30×10^{4} NC⁻¹ experiences a torque of 27×10^{26} N m. Calculate the dipole moment of the dipole.

Q.31 A regular hexagon of side 10 cm has a charge 5 μ C at each of its vertices. Calculate the potential at the center of the hexagon.

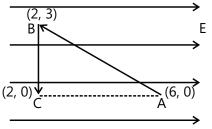
Q.32 What is the work done in moving a $2 \mu C$ point charge from corner A to B of a square ABCD, when a 10 μC charge exists at the center of the square?

Q.33 The potential at a point 0.1 m from an isolated point charge is +100 volt. Find the nature and magnitude of the point charge.

Q.34 Two charges equal to $+20\,\mu\text{C}$ and $-10\,\mu\text{C}$ are placed at points 6 cm apart. Find the value of the potential at a point distant 4 cm on the right bisector of the line joining the two charges.

Q.35 A system has two charges $q_A = 2.5 \times 10^{-9}$ C and $q_B = -2.5 \times 10^{-7}$ C located at points A: (0, 0, -15) cm and B: (0, 0, +15) cm, respectively. What are the total charge and electric dipole moment of the system?

Q.36 A test charge 'q' is moved without acceleration from A to C along the path from A to B and then from B to C in electric field E as shown in the figure. (i) Calculate the potential difference between A and C. (ii) At which point (of the two) is the electric potential more and why?



Q.37 An electric dipole is held in a uniform electric field.

(i) Show that the net force acting on it is zero.

(ii) The dipole is aligned parallel to the field.

Find the work done in rotating it through an angle of 180°.

Exercise 2

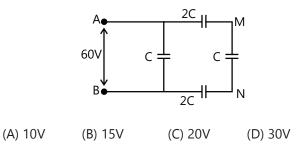
Single Correct Choice Type

Q.1 A capacitor of capacitance C is charged to a potential difference V from a cell and then disconnected from it. A charge +Q is now given to its positive plate. The potential difference across the capacitor is now

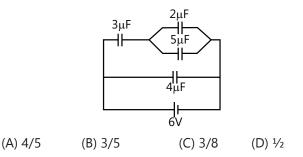
(A) V (B) V+
$$\frac{Q}{C}$$

(C) V +
$$\frac{Q}{2C}$$
 (D) V - $\frac{Q}{C}$, if V < CV

Q.2 In the circuit shown, a potential difference of 60V is applied across AB. The potential difference between the point the point M and N is

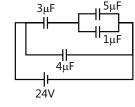


Q.3 In the circuit shown in figure, the ratio of charges on 5 μ F and 4 μ F capacitor:



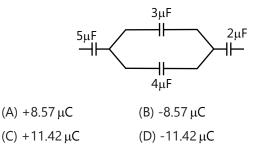
Q.4 From a supply of identical capacitors rated $8\,\mu$ F, 250V the minimum number of capacitros required to form a composite $16\,\mu$ F, 1000V is:

Q.5 In the circuit shown, the energy stored in $1\,\mu\text{F}$ capacitor is

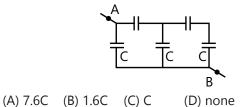


(A) $40 \,\mu J$ (B) $64 \,\mu J$ (C) $32 \,\mu J$ (D) None

Q.6 If charge on left plane of the $5 \,\mu\text{F}$ capacitor in the circuit segment shown in the figure is $-20 \,\mu\text{C}$, the charge on the right plate of $3 \,\mu\text{F}$ capacitor is



Q.7 What is equivalent capacitance of the system of capacitors between A & B.



Q.8 Three capacitors $2\,\mu$ F, $3\,\mu$ F and $5\,\mu$ F can withstand voltages to 3V, 2V and IV respectively. Their series combination can withstand a maximum voltage equal to

(A) 5Volts	(B) (31/6) Volts
(C) (26/5) Volts	(D) None

Q.9 A parallel plate capacitor has an electric field of 10^5 V/m between the plates. If the charge on the capacitor plate is $1\,\mu$ C, then the force on each capacitor plate is

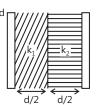
 $(A) \ 0.1 \ N \qquad (B) \ 0.05 \ N \qquad (C) \ 0.02 \ N \qquad (D) \ 0.01 \ N$

Q.10 A capacitor is connected to a battery. The force of attraction between the plates when the separation between them is halved.

(A) Remains the same (B) Becomes eight times

(C) Becomes four times (D) Becomes two times

Q.11 A parallel plate capacitor is make as shown in figure. Find capacirance and equivalent dielectric constant.



(A)
$$\frac{2\varepsilon_0 A(k_1k_2)}{k_1 + k_2}$$
 (B) $\frac{4\varepsilon_0 A(k_1k_2)}{k_1 + k_2}$

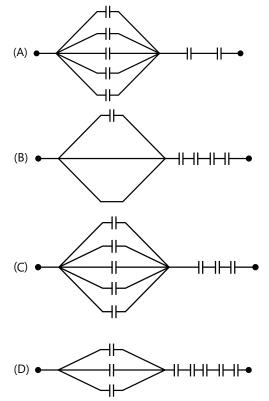
(C)
$$\frac{5\epsilon_0 A(k_1k_2)}{k_1k_2}$$
 (D) $\frac{3\epsilon_0 A(k_1k_2)}{k_1 + k_2}$

Q.12 A capacitor stores $60\,\mu$ C charge when connected across a battery. When the gap between the plates is filled with a dielectric, a charge of $120\,\mu$ C flows through the battery. The dielectric constant of the material inserted is :

(A) 1	(B) 2	(C) 3	(D) None
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Previous Years' Questions

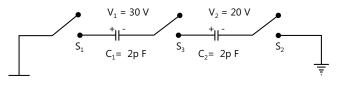
Q.1 Seven capacitors each capacitance $2 \mu F$ are connected in a configuration to obtain an effective capacitance $\frac{10}{11} \mu F$. Which of the following combinations will achieve the desired result? (1990)



Q.2 A parallel combination of $0.1M\Omega$ resistor and a $10\,\mu\text{F}$ capacitor is connected across a 1.5V source of negligible resistance. The time required for the capacitor to get charged upto 0.75V is approximately (in second) (1997)

(A) Infinite (B) $\log_{e} 2$ (C) $\log_{10} 2$ (D) Zero

Q.3 For the circuit shown, which of the following statement is true? (1999)



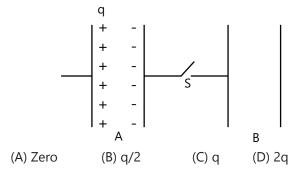
(A) With S_1 closed, V_1 =15V, V_2 =20V

(B) With S_3 closed, $V_1 = V_2 = 25V$

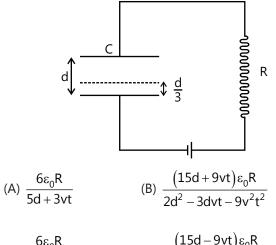
(C) With S₁ and S₂ closed,
$$V_1 = V_2 = 0$$

(D) With S₂ closed,
$$V_1 = 30 V$$
, $V_2 = 20V$

Q.4 Consider the situation shown in the figure. The capacitor A has a charge q on it whereas B is uncharged. The charge appearing on the capacitor B after a long time after the switch is closed is **(2001)**



Q.5 A parallel plate capacitor C with plates of unit are and separation d is filled with a liquid of dielectric constant K=2. The level of liquid is $\frac{d}{3}$ initially. Suppose the liquid level decreases at a constant speed V, the time constant as a function of time t is **(2008)**



(C)
$$\frac{6\epsilon_0 \kappa}{5d - 3vt}$$
 (D) $\frac{(13d - 9vt)\epsilon_0 \kappa}{2d^2 + 3dvt - 9v^2t^2}$

Q.6 When a negative charge is released and moves in electric field, it moves towards a position of (1982)

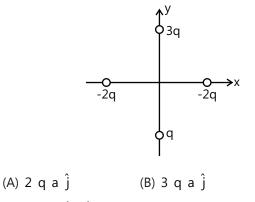
(A) Lower electric potential and lower potential energy

(B) Lower electric potential and higher potential energy

(C) Higher electric potential and lower potential energy

(D) Higher electric potential and higher potential energy

Q.7 An infinite non - conducting sheet of charge has a surface charge density of 10^{-7} C/m². The separation between two equipotential surfaces near the sheet whose potential differ by 5V is **(1983)** (A) 0.88 cm (B) 0.88 mm (C) 0.88 m (D) 5×10^{-7} m **Q.8** 4 charges are placed each at distance 'a' from origin. The dipole moment of configuration is **(1983)**



(C) 2 a q $[\hat{i} + \hat{j}]$ (D) None

Q.9 n small drops of same size are charged to V volts each. If they coalesce to form a single large drop, then its potential will be (1985)

(A) V/n	(B) Vn	(C) Vn ^{1/3}	(D) Vn ^{2/3}
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Q.10 A hollow metal sphere of radius 5 cm is charged such that the potential on its surface is 10 V. The potential at the center of the sphere is (1998)

(A) 0 V

(B) 10 V

(C) Same as at point 5 cm away from the surface outside sphere.

(D) Same as a point 25 cm away from the surface.

Q.11 If the electric potential of the inner metal sphere is 10 volt & that of the outer shell is 5 volt, then the potential at the center will be: (1999)

(A) 10 volt (B) 5 volt (C) 15 volt (D) 0

Q.12 Three concentric metallic spherical shell A, B and C or radii a, b and c (a<b<c) have surface charge densities - σ , + σ , and - σ respectively. The potential of shell A is : (1986)

(A) (σ ε ₀) [a+b-c]	(B) ($\sigma \epsilon_0$) [a-b+c]
(C) ($\sigma \epsilon_0$) [b-a-c]	(D) None

Q.13 A hollow metal sphere of radius 5 cm is charged such that the potential on its surface is 10 V. The potential at the centre of the sphere is **(1983)**

(A) Zero

(B) 10 V

(C) Same as at a point 5 cm away from the surface

(D) Same as at a point 25 cm away from the surface

Q.14 A solid conducting sphere having a charge Q is surrounded by an uncharged concentric conducting hollow spherical shell. Let the potential difference between the surface of the solid sphere and that of the outer surface of the hollow shell be V. If the shell is now given a change of -3Q, the new potential difference between the same two surfaces is **(1989)**

(A) V (B) 2 V (C) 4 V (D) -2 V

Q.15 Two identical thin rings, each of radius R, are coaxially placed a distance R apart. If Q_1 and Q_2 are respectively the charges uniformly spread on the two rings, the work done in moving a charge q from the center of one ring to that of the other is **(1992)**

(A) Zero

(B) $q(Q_1 - Q_2)(\sqrt{2} - 1) / \sqrt{2}(4\pi\epsilon_0 R)$ (C) $q\sqrt{2}(Q_1 + Q_2) / (4\pi\epsilon_0 R)$ (D) $q(Q_1 / Q_2)(\sqrt{2} + 1)\sqrt{2}(4\pi\epsilon_0 R)$

Q.16 Two point charges +q and –q are held fixed at (-d, 0) and (d, 0) respectively of a x-y co-ordinate system. Then (1995)

(A) The electric field E at all point on the x-axis has the same direction.

(B) Work has to be done in bringing a test charge from ∞ to the origin

- (C) Electric field at all point on y-axis is along x-axis
- (D) The dipole moment is 2qd along the x-axis

Q.17 A parallel plate capacitor of capacitance C is connected to a battery and is charged to a potential difference V. Another capacitor of capacitance 2C is similarly charged to a potential difference 2V. The charging battery is now disconnected and the capacitors are connected in parallel to each other in such a way that the positive terminal of one is connected to the negative terminal of the other. The final energy of configuration is **(1995)**

(A) Zero (B)
$$\frac{3}{2}$$
CV² (C) $\frac{25}{6}$ CV² (D) $\frac{9}{2}$ CV²

Q.18 A charge +q is fixed at each of the points $x = x_0$, $x = 3x_0$, $x = 5x_0$ ∞ on the x-axis and a charge -q is fixed at each of the points $x = 2x_0$, $x = 4x_0$, $x = 6x_0$ ∞ . Here, x_0 is a positive constant. Take the electric potential at a point due to a charge Q at a distance r from it to be Q/ $4\pi\varepsilon_0$ r.

Then the potential at the origin due to the above system of charges is (1998)

(A) Zero (B)
$$\frac{q}{8\pi\epsilon_0 x_0 \ln 2}$$

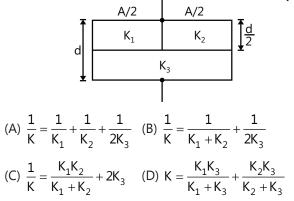
(C) Infinite

Q.19 Two identical metal plates are given positive charges Q_1 and Q_2 (< Q_1) respectively. If they are now brought close together to form a parallel plate capacitor with capacitance C, the potential difference between them is **(1999)**

(D) $\frac{q \ln(2)}{4\pi\epsilon_0 x_0}$

(A)
$$(Q_1 + Q_2) / 2C$$
 (B) $(Q_1 + Q_2) / C$
(C) $(Q_1 - Q_2) / C$ (D) $(Q_1 - Q_2) / 2C$

Q.20 A parallel plate capacitor of area A, plate separation d and capacitance C is filled with three different dielectric materials having dielectric constants K_1, K_2 and K_3 as shown, If a single dielectric material is to be used to have the same capacitance C in this capacitor then its dielectric constant K is given by (2000)



Q.21 A uniform electric field pointing in positive x-direction exists in a region. Let A be origin, B be he point on the x-axis at x=+1 cm and C be the point on the y-axis at y=+1 cm. Then the potentials at the points A, B and C satisfy (2001)

(A)
$$V_A < V_B$$
 (B) $V_A > V$

(C) $V_A < V_C$ (D) $V_A > V_C$

Q.22 Two equal point charges are fixed at x=-a and x=+a on the x-axis. Another point charge Q is placed at the origin. The change in the electrical potential energy of Q, when it is displaced by a small distance x along the x-axis, is approximately proportional to **(2002)**

(A) x (B)
$$x^2$$
 (C) x^3 (D) $1/x$

Q.23 Two identical capacitors, have the same capacitance C. One of them is charged to potential V_1 and the other to V_2 . Likely charged plates are then connected. Then, the decrease in energy of the combined system is **(2002)**

(A)
$$\frac{1}{4}C(V_1^2 - V_2^2)$$
 (B) $\frac{1}{4}C(V_1^2 + V_2^2)$
(C) $\frac{1}{4}C(V_1 - V_2)^2$ (D) $\frac{1}{4}C(V_1 + V_2)^2$

Q.24 A long, hollow conducting cylinder is kept coaxially inside another long, hollow conducting cylinder of larger radius. Both the cylinders are initially electrically neutral. (2007)

(A) A potential difference appears between the two cylinders when a charge density is given to the inner cylinder

(B) A potential difference appears between the two cylinders when a charge density is given to the outer cylinder

(C) No potential difference appears between the two cylinders when a uniform line charge is kept along the axis of the cylinders

(D) No potential difference appears between the two cylinders when same charge density is given to both the cylinders

Q.25 Positive and negative point charges of equal

magnitude are kept at $\left(0,0,\frac{a}{2}\right)$ and $\left(0,0,\frac{-a}{2}\right)$,

respectively. The work done by the electric field when another positive point charge in moved from (-a, 0, 0) to (0, a, 0) is (2007)

(A) Positive

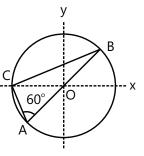
(B) Negative

(C) Zero

(D) Depends on the path connecting the initial and final position

Q.26 Consider a system of three charges $\frac{q}{3}, \frac{q}{3}$ and $-\frac{2q}{3}$

placed at points A, B and C respectively, as shown in the figure. Take O to the center of the circle of radius R and angle $CAB = 60^{\circ}$ (2008)



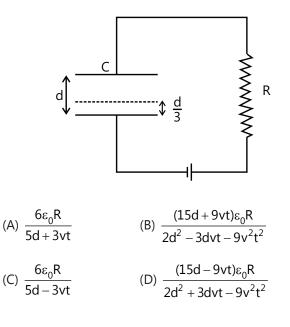
(A) The electric field at point O is $\frac{q}{8\pi\epsilon_0 R^2}$ directed along the negative x-axis

(B) The potential energy of the system is zero

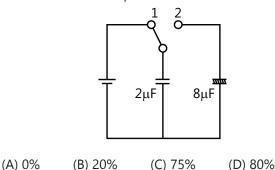
C and B is
$$\frac{q^2}{54\pi\epsilon_0 R^2}$$

(D) The potential at point O is $\frac{q}{12\pi\epsilon_0 R}$

Q.27 A parallel plate capacitor C with plates of unit area and separation d is filled with a liquid of dielectric constant K = 2. The level of liquid is $\frac{d}{3}$ initially. Suppose the liquid level decreases at a constant speed v, the time constant as a function of time t is **(2008)**



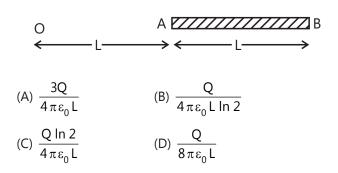
Q.28 A 2μ F capacitor is charged as shown in the figure. The percentage of its stored energy dissipated after the switch S is turned to potion 2 is **(2011)**



Q.29 Two capacitors C_1 and C_2 are charged to 120 V and 200 V respectively. It isfound that by connecting them together the potential on each one can be madezero. Then: **(2013)**

(A) $3C_1 = 5C_2$ (B) $3C_1 + 5C_2 = 0$ (C) $9C_1 = 4C_2$ (D) $5C_1 = 3C_2$

Q.30 A charge Q is uniformly distributed over a long rod AB oflength L as shown in the figure. The electric potential at the point O lying at a distance L from the end A is: (2013)



Q.31 A parallel plate capacitor is made of two circular plates separated by a distance of 5 mm and with a dielectric of dielectric constant 2.2 between them. When the electric field in the dielectric is 3×104 V/m, the charge density of the positive plate will be close to: **(2014)**

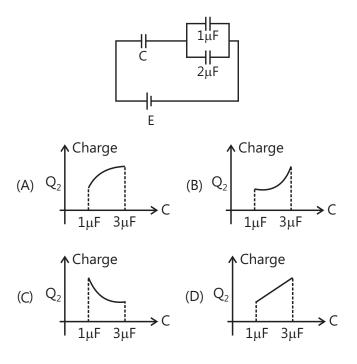
(A) 3×10^4 C / m ²	(B) 6×10^4 C / m ²
(C) 6×10^{-7} C / m ²	(D) 3×10^{-7} C / m ²

Q.32 Assume that an electric field $\vec{E} = 30 x^2 \hat{i}$ exists in space. Then the potential difference $V_A - V_0$, where V_0 is the potential at the origin and V_A the potential at x = 2 m is: (2014)

(A) – 80 V	(B) 80 V
(C) 120 V	(D) None of these

Q.33 A uniformly charged solid sphere of radius R has potential V₀ (measured with respect to ∞) on its surface. For this sphere the equipotential surfaces with potentials $\frac{3V_0}{2}$, $\frac{5V_0}{4}$, $\frac{3V_0}{4}$ and $\frac{V_0}{4}$ have radius R₁,R₂,R₃ and R₄ respectively. Then (2015) (A) R₁ \neq 0 and (R₂-R₁)>(R₄-R₃) (B) R₁ = 0 and R₂ < (R₄-R₃) (C) 2R<R₄ (D) R₁ = 0 and R₂ > (R₄-R₃)

Q.34 In the given circuit, charge Q_2 on the 2μ F capacitor changes as C is varied from 1μ F to 3μ F. Q_2 as a function of 'C' is given properly by : (figures are drawn schematically and are not to scale) (2015)



Q.35 A combination of capacitors is set up as shown in the figure. The magnitude of the electric field, due to a point charge Q (having a charge equal to the sum of the charges on the $4 \,\mu\text{F}$ and $9 \,\mu\text{F}$ capacitors), at a point distant 30 m from it, would equal: (2016)

(A) 360 N/C	(B) 420 N/C

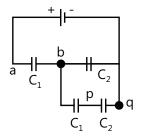
(C) 400 N/C $(D) 240 N/C$	(C) 480 N/C	(D) 240 N/C
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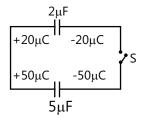
Exercise 1

Q.1 A parallel plate capacitor has plate area 100 cm2 and place separation 1 cm. A glass plate (k = 6) of thickness 6 mm and an ebonite plate (k = 4) are inserted to fill the gap between the plates. Find new capacitance.

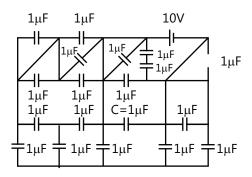
Q.2 In the given network (See figure) if Potential difference between p and q is 2V and $C_2=3C_1$. Then find difference between a & b.



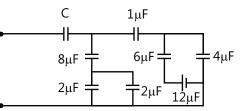
Q.3 Find field produced in the circuit shown in figure on closing the switch S.



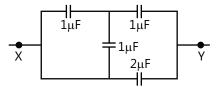
Q.4 In the following circuit (See figure), the resultant capacitance between A and B is $1 \,\mu$ F. Find equivalent capacitance of the circuit.



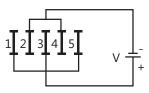
Q.5 Find the charge on the capacitor $C=1\,\mu F$ in the circuit shown in the figure.



Q.6 The figure shows a circuit consisting of four capacitors. Find the effective capacitance between X and Y



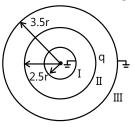
Q.7 Five identical capacitor plates, each of area A are arranged such that adjacent plates are at a distance'd' apart, the plates are connected to a source of emf V as shown in figure. The charge on plate 1 is ----- and that on plate 4 is ----



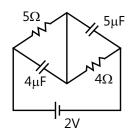
Q.8 Find the capacitance of the system shown in figure.

T		Plate ar	ea = A
d	k = 1	k = 2	
d	k = 3	k = 4	
±			

Q.9 Figure shows three concentric conducting spherical shells with inner and outer shells earthed and the middle shell is given a charge q. find the electrostatic energy of the system stored in the region I and II.

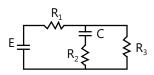


Q.10 Find the ratio between the energy stored in 5μ F capacitor to the 4μ F capacitor in the given circuit in stedy state.

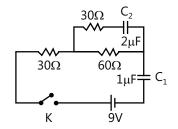


Q.11 A solid conducting sphere of radius 10cm is enclosed by a thin metallic shell of radius 20cm. a charge $q=20\,\mu$ C is given to the inner sphere. Find the heat generated in the process, the inner sphere is connected to the shell by a conducting wire.

Q.12 In the circuit shown here, At the steady state, the charge on the capacitor is ------.



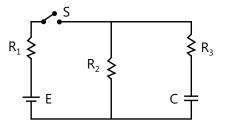
Q.13 For the arrangement shown in the figure, the key is closed at t=0. C_2 is initially uncharged while C_1 has a charge of $2 \mu C$



(a) Find the current coming out of the battery just after switch is closed.

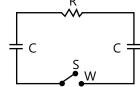
(b) Find the charge on the capacitors in the steady state condition.

Q.14 In the circuit shown in figure $R_1 = R_2 = 6R_3 = 300M \Omega$, C=0.01 µF and E=10V. The switch is closed at t=0, find



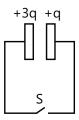
- (a) Charge on capacitor as a function of time.
- (b) Energy of the capacitor at t=20s.

Q.15 In the circuit shown in figure the capacitance of each capacitor is equal to C and resistance R. One of the capacitor was charged to a voltage V and then at the moment t=0 was shorted by means of the switch S. find:

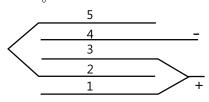


- (a) The current in the circuit as a function of time t.
- (b) The amount of generated heat.

Q.16 The two identical parallel plates are given charges as shown in figure. If the plate area of either face of each plate is A and separation between plates is d, then find the amount of heat liberated after closing the switch.



Q.17 Five identical conducting plates 1, 2, 3, 4 & 5 are fixed parallel to and equidistant from each other (see figure). Plates 2 & 5 are connected by a conductor while 1 & 3 are joined by another conductor. The junction of 1 & 3 and the plate 4 are connected to a source of constant e.m.f. V_0 find:

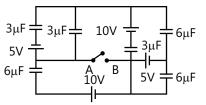


(i) The effective capacity of the system between the terminals of the source.

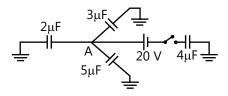
(ii) The charges on plates 3 & 5. Given

- D = Distance between any 2 successive plate &
- A = Area of either face of each plate.

Q.18 Find the charge flown through the switch from A to B when it is closed.



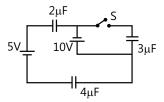
Q.19 Three capacitors of $2 \mu F$, $3 \mu F$ and $5 \mu F$ are independently charged with batteries of emf's 5V, 20V and 10V respectively. After disconnecting from the voltage source. These capacitors are connected as shown in figure with their positive polarity plates connected to A and negative polarity is earthed. Now a battery of 20V and an uncharged capacitor of $4 \mu F$ capacitance are connected to the junction A as shown with a switch S. when switch is closed, find:



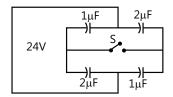
(a) The potential of the junction A.

(b) Final charge on all four capacitros.

Q.20 In the circuit shown in figure, find the amount of heat generated when switch s is closed.



Q.21 the connection shown in figure are established with the switch S open. How much charge will flow through the switch if it is closed?



Q.22 The figure shows two identical parallel plate capacitors connected to a battery with the switch S closed. The switch is now opened and the free space between the plates of the capacitors is filled with a

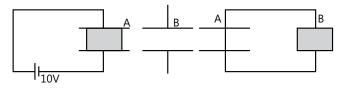
dielectric of dielectric constant (or relative permittivity) 3. Find the ratio of the total electrostatic enegry stored in both capacitors

before and after the introduction of the dielectric.

Q.23 A parallel plate capacitor has plates with area A & separation d. A battey charges the plates to a potential difference of V_0 . The battery is then disconnected & a di-electric slab of constant K & thickness d is introduced. Calculate the positive work done by the system (capacitor+slab) on the man who introduces the slab.

Q.24 A parallel plate capacitor is filled by a di-electric whose relative permittivity varies with the applied voltage according to the law= α V, where α = 1 per volt. The same (but containing no di-electric) capacitor charged to a voltage V=156 volt is connected in parallel to the first "non-linear" uncharged capacitor. Determine the final voltage V_f across the capacitors.

Q.25 Two parallel plate capacitors A & B have the same separation $d=8.85+10^4$ m between the plates. The plate areas of A & B are 0.04 m² & 0.02m² respectively. A slab of di-electric constant (relative permittivity) K=9 has dimensions such that it can exactly fill the space between the plates of capacitor B.



(i) The di-electric slab is placed inside A and A is then charged to a potential difference of 110volt. Calculate the capacitance of A and the energy stored in it.

(ii) The battery is disconnectd & then the di-electric slab is removed from A. find the work done by the external agency in removing the slab from A.

(iii) The same di-electric slab is now placed inside B, filling it completely. The two capacitors A & B are then connected. Calculate the energy stored in the system.

Q.26 Two square metallic plates of 1m side are kept 0.01m apart, like a parallel plate capacitor, in air in such a way that one of their edges is perpendicular, to an oil surface in a tank filled with an insulating oil. The plates are connected

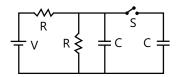
to a battery of e.m.f. 500 volt. The plates are then lowered vertically into the oil at a speed of 0.001 m/s. calculate the current drawn from the battery during the process.

[Di-electric constant of oil= $\varepsilon_0 = 8.85 \times 10^{12} \text{C}^2 / \text{N}^2 \text{m}^2$]

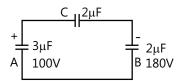
Q.27 A 10 μ F and 20 μ F capacitor are connected to a 10V cell in parallel for some time after which the capacitors are disconnected from the cell and reconnected at t=0 with each other, in series, through wires of finite resistance. The +ve plate of the first capacitor. Draw the graph which best describes the charge on the +ve plate of the 20 μ F capacitor with increasing time.

Q.28 A capacitor of capacitance C_0 is charged to a potential V_0 and then isolated. A small capacitor C is then charged from C_0 , discharged and charged again, the process being repeated in times. The potential of the large capacitor has now fallen to V. Find the capacitance of the small capacitor. If V_0 =100volts, V=35volts, find the value of n for C_0 =0.2 µF and C=0.01075 µF. Is it possible to remove charge on C_0 this way?

Q.29 In the figure shown initially switch is open for a long time. Now the switch is closed at t=0. Find the charge on the rightmost capacitor as a function of time given that it was initially unchanged.



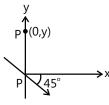
Q.30 Two capacitors A and B with capacitor are connected as shown in figure with one wire from each capacitor free. The upper plate of A is positive and that of B is negative. An uncharged $2 \mu F$ capacitor C with lead wires falls on the free ends to complete the circuit. Calculate:



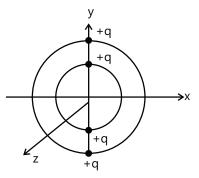
(i) The final charges on the three capacitors (ii) The amount of electrostatic energy stored in the system before and after the completion of the circuit.

Q.31 Three charges 0.1 coulomb each are placed on the comers of an equilateral triangle of side 1 m. If the energy is supplied to this system at the rate of 1 kW, how much time would be required to move one of the charges onto the midpoint of the line joining the other two?

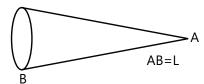
Q.32 A dipole is placed at origin of coordinate system as shown in figure, find the electric field at point P (0, y).



Q.33 Two concentric rings of radii r and 2r are placed with center at origin. Two charges +q each are fixed at the diametrically opposite points of the rings as shown in figure. Smaller ring is now rotated by an angle 90° about Z-axis then it is again rotated by 90° about Y-axis. Find the work done by electrostatic force in each step. If finally larger ring is rotated by 90° about X-axis, find the total work required to perform all three steps.



Q.34 A cone made of insulating material has a total charge Q spread uniformly over its sloping surface. Calculate the energy required to take a test charge q from infinity to apex A of cone.



The slant length is L.

Q.35 A non-conducting disc of radius a and uniform positive surface charge density σ is placed on the ground, with its axis vertical. A particle of mass m & positive charge q is dropped, along the axis of the disc, from a height H with zero initial velocity. The particle

has
$$\frac{q}{m} = \frac{4\varepsilon_0 g}{\sigma}$$

(a) Find the value of H if the particle just reaches the disc.

(b) Sketch the potential energy of the particle as a function of its height and find its equilibrium position.

Exercise 2

Single Correct Choice Type

Q.1 Two capacitor having capacitance 8 µF and 16 μ F have breaking voltage 20V and 80V. They are combined in series. The maximum charge they can store individually in the combination is:

(A) 160 μC (B) 200 µC

(C) 1280 µC (D) None of these

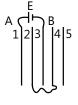
Q.2 Three plate A, B and C each of area 0.1m² are separated by 0.885mm from each other as shown in the figure. A 10V battery is used to charge the system. The energy stored in the system is

(B) 10⁻¹μ J (C) 10 ₂µ J (D) 10⁻³µ J (A) 1µ J

Q.3 A capacitor of capacitance C is initially charge to a potential difference of V. Now it is connected to battery of 2V with opposite polarity. The ratio of heat generated to the final erergy stored in the capacitor will be

(A) 1.75 (B) 2.25 (C) 2.5 (D) 1/2

Q.4 Five conducting parallel plates having area A and separation between them being d, are placed as shown in the figure. Plate number 2 and 4 are connected with a wire and between point A and B, a cell of emf E is connected. The charge flown

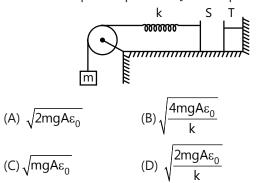


С

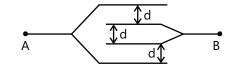
10V

(A)
$$\frac{3}{4} \frac{\varepsilon_0 AE}{d}$$
 (B) $\frac{2}{3} \frac{\varepsilon_0 AE}{d}$ (C) $\frac{4\varepsilon_0 AE}{d}$ (D) $\frac{\varepsilon_0 AE}{2d}$

Q.5 The plates S and T of an uncharged parallel plate capacitor are connected acorss a battey. The battery is then disconnected in a system as shown in the figure. The system shown is in equilibrium. All the strings are insulating and massless. The magnitude of charge on one of the capacitor plates is: [Area of plates = A]

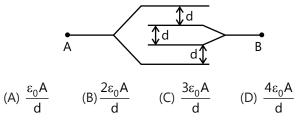


Q.6 Four metallic plates are arranged as shown in the figure. If the distance between each plate is d, The capacitance of the given system between points A and B is (Given d < A)

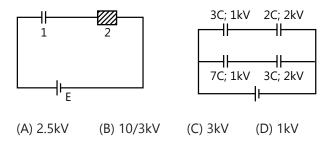




Q.7 Find the equivalent capacitance across A and B



Q.8 The diagram shows four capacitors with capacitances and break down voltage as mentioned. What should be the maximum value of the external emf source such that no capacitor breaks down? [Hint: First of all find out the break down voltage of each branch. After that compare them.]

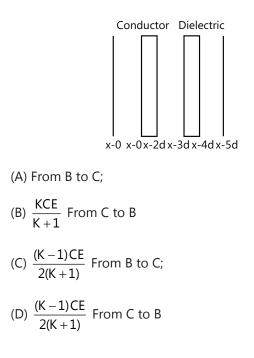


Q.9 A conducting body 1 has some initial charge Q, and its capacitance is C. There are two other conducting bodies, 2 and 3, having capacitances: $C_2 = 2C$ and $C_3 \rightarrow \infty$. Bodies 2 and 3 are initially uncharged. "Body 2 is touched with body 1 and touched with body 3, and the removed." This process is repeated N times. Then, the charge on body 1 at the end must be

(A) Q/3ⁿ (B) Q/3ⁿ⁻¹
$$\frac{\text{KCE}}{\text{K}+1}$$

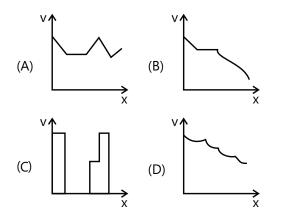
(C) Q/2ⁿ (D) None

Q.10 In the adjoining figure, capacitor (1) and (2) have a capacitance 'C' each. When the dielectric of dielectric constant K is inserted between the plates of one of the capacitor, the total charge flowing through battery is



Q.11 The distance between plates of a parallel plate capacitor is 5d. Let the positively charged plate is at X = 0 and negatively charged plate is at X = 5d. Two slabs one of conductor and other of a dielectric of equal thickness d are inserted between the plates as shown in figure.

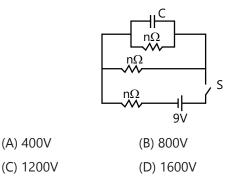
Potential versus distance graph will look like:



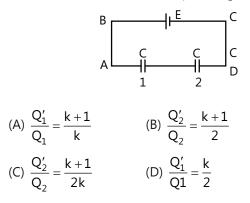
Q.12 The distance between the plates of a charged parallel plate capacitor is 5cm and electric field inside the plates is 200V cm⁻¹. An uncharged metal bar of width 2cm is fully immersed into the capacitor. The length of the metal bar is same as that of plate of capacitor. The voltage across capacitor after the immersion of the bar is

(A) Zero	(B) 400V
(C) 600V	(D) 100V

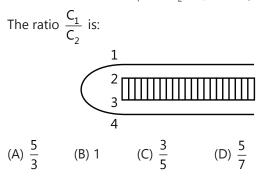
Q.13 Condenser A has a capacity of 15μ F when it is filled with a medium of dielectric constant 15. Another condenser B has a capcity 1μ F with air between the plates. Both are charged separately by a battery of 100V. After charging, both are connected in parallel without the battery and the dielectric material being removed. The common potential now is



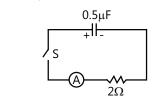
Q.14 Two identical capacitors 1 and 2 are connected in series to a battery as shown in figure. Capacitor 2 contains a dielectric slab of dielectric constant k as shown. Q_1 and Q_2 are the charges stored in the capacitors. Now the dielectric slab is removed and the corresponding charges are Q'_1 and Q'_2 . Then



Q.15 Four identical plates 1, 2, 3 and 4 are placed parallel to each other at equal distance as shown in the figure. Plates 1 and 4 are joined together and the space between 2 and 3 is filled with a dielectric of dielectric constant k=2. The capacitance of the system between 1 and 3 & 2 and 4 are C₁ and C₂ respectively.

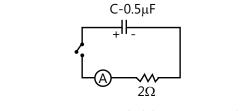


Q.16 A charged capacitor is allowed to discharge through a resistance 2Ω by closing the switch S at the instant t = 0. At time t = $ln2 \mu s$, the reading of the ammeter falls half of its initial value. The resistance of the ammeter is equal to



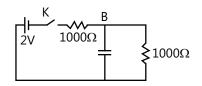
(A) 0 (B) 2Ω (C) $2K\Omega$ (D) $2M\Omega$

Q.17 A capacitor C = $100 \,\mu\text{F}$ is connected to three resistor each of resistance $1k\,\Omega$ and a battery of emf 9V. The switch S has been closed for long time so as to charge the capacitor. When switch S is opened, the capacitor discharges with time constant



(A) 33ms (B) 5ms (C) 3.3ms (D) 50ms

Q.18 In the circuit shown, when the key k is pressed at time t=0, which of the following statements about current I in the resistor AB is true.



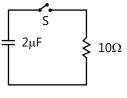
(A) I = 2mA at all t

(B) I oscillates between 1mA and 2mA

(C) I = 1mA at all t

(D) At t = 0, I = 2mA and with time it goes to 1mA

Q.19 In the R-C circuit shown in the figure the total energy of 3.6×10^{-3} J is dissipated in the 10Ω resistor when the switch S is closed. The initial charge on the capacitor is



(A) 60 μC

(B) $120 \,\mu\text{C}$ (C) $60 \,\sqrt{2}\mu\text{C}$ (D) $\frac{60}{\sqrt{2}}\mu\text{C}$

Q.20 A charged capacitor is allowed to discharge through a resistor by closing the key at the instant t=0. At the instant t=(ln 4) μ S, the reading of the ammeter falls half the initial value. The resistance of the ammeter is equal to

(A) $1 M\Omega$ (B) 1Ω (C) 2Ω (D) $2 M\Omega$

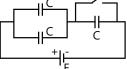
Multiple Correct Choice Type

Q.21 Two capacitors of 2 μ F and 3 μ F are charged to 150 volt and 120 volt respectively. The plates of capacitor are connected as shown in the figure. A discharged capacitor of capacity 1.5 μ F falls to the free ends of the wire. Then 1.5 μ F

$$150V = \frac{1}{2}\mu F \qquad 3\mu F = \frac{1}{4} 120V$$

- (A) Charge on the $1.5 \,\mu\text{F}$ capacitors is $180 \,\mu\text{C}$
- (B) Charge on the $2 \,\mu$ F capacitor is $120 \,\mu$ C
- (C) Positive charge flows through A from right to left.
- (D) Positive charge flows thorugh A from left to right.

Q.22 In the circuit shown, each capacitor has a capacitance C. The emf of the cell is E. If the switch S is closed



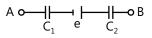
(A) Positive charge will flow out of the positive terminal of the cell.

(B) Positive charge will enter the positive terminal of the cell

(C) The amount of charge flowing through the cell will be CE.

(D) The amount of charge flowing through the cell will be 4/3 CE.

Q.23 A circuit shown in the figure consists of a battery of emf 10V and two capacitance C_1 and C_2 of capacitances 1.0 μ F and 2.0 μ F respectively. Which of the options are correct?



(A) Charge on capacitor $\rm C_1$ is equal to charge on capacitor $\rm C_2$

(B) Voltage across capacitor C_1 is 5V

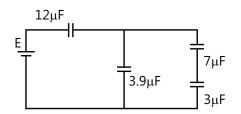
(C) Voltage across capacitor C_2 is 10V

(D) Energy stored in capacitor C_1 is two times the energy stored in capacitor C_2 .

Q.24 If Q is the charge on the plates of a capacitor of capacitance C, V the potential difference between the plates, A the area of each plate and d the distance between the plates, The force of attraction between the plates is

(A)
$$\frac{1}{2} \left(\frac{Q^2}{\varepsilon_0 A} \right)$$
 (B) $\frac{1}{2} \left(\frac{CV^2}{d} \right)$
(C) $\frac{1}{2} \left(\frac{CV^2}{A \varepsilon_0} \right)$ (D) $\frac{1}{4} \left(\frac{Q^2}{\pi \varepsilon_0 d^2} \right)$

Q.25 Four capacitors and a battery are connected as shown. The potential drop across the $7 \,\mu\text{F}$ capacitor is 6V. Then the;



(A) Potential difference across the $3 \,\mu\text{F}$ capacitor is 10V

(B) Charge on the 3μ F capacitor is 42μ C

(C) Emf on the battery is 30V

(D) Potential difference across the $12\,\mu\text{F}$ capacitor is 10V

Q.26 The capacitance of a parallel plate capacitor is C when the region between the plates has air. This region is now filled with a dielectric slab of dielectric constant k. the capacitor is connected to a cell of emf E, and the slab is taken out

(A) Charge CE (k-1) flows through the cell

(B) Energy E^2C (k-1) is absorbed by the cell.

(C) The energy stored in the capacitor is reduced by $E^2C\ (k\text{-}1)$

(D) The external agent has to do $\frac{1}{2}E^2C(k-1)$ amount of work to take the slab out.

Q.27 A parallel plate air-core capacitor is connected across a source of constant potential difference. When a dielectric plate is introduced between the two plates then:

(A) Some charge from the capacitor will flow back into the source.

(B) Some extra charge from the sourch will flow back into the capacitor.

(C) The electric field intensity between the two plates does not charge.

(D) The electric field intensity between the two plates will decrease.

Q.28 A parallel plate capacitor of plate area A and plate separation d is charged to potential difference V and then the battery is disconnected. A slab of dielectric constant K is then inserted between the plates of the capacitor so as to fill the space between the plates. If Q, E and W denote respectively, the magnitude of charge on each plate, the electric field between the plates (after the slab is inserted) and the work done on the system, in question, in the process of inserting the slab, then

(A)
$$Q = \frac{\varepsilon_0 AV}{d}$$
 (B) $Q = \frac{\varepsilon_0 KAV}{d}$
(C) $E = \frac{V}{Kd}$ (D) $W = \frac{\varepsilon_0 AV^2}{2d} \left(1 - \frac{1}{K}\right)$

Q.29 A parallel plate capacitor has a parallel slab of copper inserted between and parallel to the two plates, without touching the plates. The capacity of the capacitor after the introduction of the copper sheet is:

(A) minimum when the copper slab touches one of the plates.

(B) Maximum when the copper slab touches one of the plates.

(C) Invariant for all positions of the slab between the plates.

(D) Greater than that before introducing the slab.

Q.30 The plates of a parallel plate capacitor with no dielectric are connected to a voltage source. Now a dielectric of dielectric constant K is inserted to fill the whole space between the plates with voltage source remaining connected to the capacitor.

(A) The energy stored in the capacitor will become K-times

(B) The electric field inside the capacitor will decrease to K-times

(C) The force of attraction between the plates will increase to K^2 times.

(D) The charge on the capacitor will increase to K-times

Q.31 A parallel-plate capacitor is connected to a cell. Its positive plate A and its negative palte B have charges +Q and –Q respectively. A third plate C, identical to A and B, with charge+Q, is now introduced midway between A and B, parallel to them, which of the following are correct?

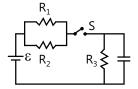
(A) The charge on the inner face of B is now $-\frac{3Q}{2}$

(B) There is no change in the potential difference between A and B.

(C) The potential difference between A and C is onethird of the potential difference between B and C.

(D) The charge on the inner face of A is now Q/2.

Q.32 The circuit shown in the figure consists of a battery of emf $\varepsilon = 10V$; a capacitor of capacitance C=1.0 μ F and three resistor of values R₁=2 Ω , R₂=2 Ω and R₃=1 Ω . Initially the capacitor is completely uncharged and the switch S is open. The switch S is closed at t=0.



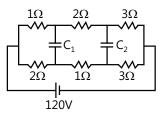
(A) The current through resistor R_3 at the moment the switch closed is zero.

(B) The current through resistor $\rm R_{3}$ a long time after the switch closed is 5A

(C) The ratio of current through $\rm R_1$ and $\rm R_2$ is always constant.

(D) The maximum charge on the capacitor during the operation is 5 μC

Q.33 In the circuit shown in figure $C_1 = C_2 = 2 \,\mu\text{F}$ Then charge stored in



(A) Capacitor C_1 is zero (B) Capacitor C_2 is zero (C) Both capacitor is zero (D) Capacitor C_1 is $40 \,\mu$ C

Assertion Reasoning Type

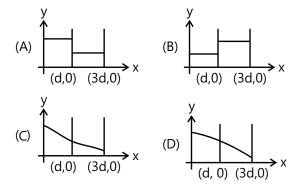
(A) Statement-I is true, statement-II is true and statement-2 is correct explanation for statement-I.

(B) Statement-I is true, statement-II is true and statement-II is not the correct explatnation for statement-I.

- (C) Statement-I is true, statement-II is false.
- (D) Statement-I is false, statement-II is true.

Q.34 Statement-I: The electrostatic force between the plates of a charged isolated capacitor decreases when dielectric fills whole space between plates.

Statement-II: The electric field between the plates of a charged isolated capacitance decreases when dielectric fills whole space between plates.



Q.35 Statement-I: If temperature is increased, the dielectric constant of a polar dielectric decreases whereas that of a non-polar dielectric does not change significantly.

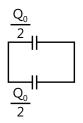
Statement-II: The magnitude of dipole moment of individual polar molecule decreases significantly with increase in temperature.

Q.36 Statement-I: The heat produced by a resistor in any time t during the charging of a capacitor in a series circuit is half the energy stored in the capacitor by that time.

Statement-II: Current in the circuit is equal to the rate of increase in charge on the capacitor.

Comprehension Type

Paragraph 1: Two capacitors each having area A and plate separation'd' are connected as shown in the circuit. Each capacitor carries charge $Q_0/2$.



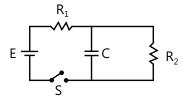
The plates of one capacitor are slowly pulled apart by an external agent till the separation between them becomes 2d. The other capacitor is not disturbed.

Q.37 The force applied by the external agent when the separation between the plates is 'X' is given by

(A)
$$\frac{Q_0^2 d}{3A\epsilon_0}$$
 (B) $\frac{Q_0^2 d}{12A\epsilon_0}$ (C) $\frac{Q_0^2}{2A\epsilon_0}$ (D) $\frac{Q_0^2 d}{6A\epsilon_0}$

Q.38 At this position the potential difference across the capacitors is given by

Paragraph 2: In the circuit as shown in figure the switch is closed at t = 0.



Q.39 At the instant of closing the switch

(A) The battery delivers maximum current

(B) No current flows through C

(C) Voltage drop across R₂ is zero

(D) The current through the battery decreases with time and finally becomes zero.

Q.40 A long time after closing the switch

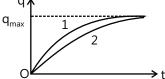
(A) Voltage drop acorss the capacitor is E

(B) Current through the battery is
$$\frac{E}{R_1 + R_2}$$

(C) Energy stores in the capacitor is $\frac{1}{2}C\left(\frac{R_2E}{R_1+R_2}\right)^2$

(D) Current through the capacitor becomes zero.

Paragraph 3: The charge across the capacitor in two different RC circuit 1 and 2 are plotted as shown in figure.



Q.41 Choose the correct statement (S) related to the two circuits.

(A) Both the capacitors are charged to the same charge.

- (B) The emf's of cells in both the circuit are equal.
- (C) The emf's of the cell may be different.
- (D) The emf's E_1 is more than E_2

Q.42 Identify the correct statement (s) related to the R_1 , R_2 , C_1 and C_2 of the two RC circuits.

(A)
$$R_1 > R_2$$
 if $E_1 = E_2$ (B) $C_1 < C_2$ If $E_1 = E_2$
(C) $R_1C_1 > R_2C_2$ (D) $\frac{R_1}{R_2} < \frac{C_2}{C_1}$

Previous Years' Questions

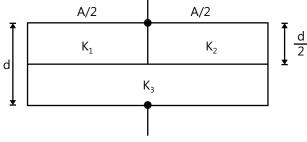
Q.1 A parallel plate capacitor of capacitance C is connected to a battery and is charged to a potential difference V. Another capacitor of capacitance 2C is similarly charged to a potential difference 2V. The charging battery is now disconnected and the capacitors are connected in parallel to each other in such a way that the positive terminal of one is connected to the negative terminal of the other. The final energy of the configuration is **(1995)**

(A) Zero (B)
$$\frac{3}{2}$$
CV² (C) $\frac{25}{6}$ CV² (D) $\frac{9}{2}$ CV²

Q.2 Two identical metal plates are given positive charges Q_1 and $Q_2(<Q_1)$ respectively. If they are now brought close together to form a parallel plate capacitor with capacitance C, the potential difference between them is (1999)

(A) (Q ₁ +Q ₂)/2C	(B) (Q ₁ +Q ₂)/C
(C) (Q ₁ -Q ₂)/C	(D) (Q ₁ -Q ₂)/ ₂ C

Q.3 A parallel plate capacitor of area A, plate separation d and capacitance C is filled with three different dielectric materials having dielectric constants K_1 , K_2 and K_3 as shown. If a single dielectric material is to be used to have the same capacitance C in this capacitor then its dielectric constant K is given by **(2000)**



A = Area of plates

(A)
$$\frac{1}{K} = \frac{1}{K_1} + \frac{1}{K_2} + \frac{1}{2K_3}$$
 (B) $\frac{1}{K} = \frac{1}{K_1 + K_2} + \frac{1}{2K_3}$
(C) $\frac{1}{K} = \frac{K_1K_2}{K_1 + K_2} + 2K_3$ (D) $K = \frac{K_1K_3}{K_1 + K_3} + \frac{K_2K_3}{K_2 + K_3}$

Q.4 Two identical capacitors, have the same capacitance C. One to them is charged to potential V_1 and the other to V_2 . Likely charged plates are then connected. Then, the decrease in energy of the combined system is **(2002)**

(A)
$$\frac{1}{4}C(V_1^2 - V_2^2)$$
 (B) $\frac{1}{4}C(V_1^2 + V_2^2)$
(C) $\frac{1}{4}C(V_1 - V_2)^2$ (D) $\frac{1}{4}C(V_1 + V_2)^2$

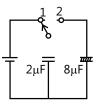
Q.5 A 2μ F capacitor is charged as shown in the figure. The percentage of its stored energy dissipated after the switch S is turned to position 2 is (2011)

(B) 20%

(D) 80%

(A) 0%

(C) 75%



Q.6 A parallel plate air capacitor is connected to a battery. The quantities charge, voltage, electric field and energy associated with this capacitor are given by Q_0 , V_0 , E_0 and U_0 respectively. A dielectric slab is now introduced to fill the space between the plates with the battery still in connection. The corresponding quantities now given by Q, V, E and U are related to the previous one as (1985)

(A)
$$Q > Q_0$$
 (B) $V > V_0$
(C) $E > E_0$ (D) $U > U_0$

Q.7 A parallel plate capacitor is charged and the charging battery is then disconnected. If the plates of the capacitor are moved farther apart by means of insulating handles (1987)

(A) The charge on the capacitor increases

(B) The voltage across the plates increases

(C) The capacitance increases

(D) The electrostatic energy stored in the capacitor increases.

Q.8 A parallel plate capacitor of plate area A and plate separation d is charged to potential difference V and then the battery is disconnected. A slab of dielectric constant K is then inserted between the plates of the capacitor so as to fill the space between the plates. If Q, E and W denote respectively, the magnitude of charge on each plate, the electric field between the plates (after the slab in inserted), and work done on the system, in question, in the process of inserting the slab, then

(A)
$$Q = \frac{\varepsilon_0 AV}{d}$$
 (B) $Q = \frac{\varepsilon_0 KAV}{d}$
(c) $E = \frac{V}{Kd}$ (D) $W = \frac{\varepsilon_0 AV^2}{2d} \left[1 - \frac{1}{K} \right]$

Q.9 A dielectric slab of thickness d is inserted in a parallel plate capacitor whose negative plate is at X=0 and positive plate is at X=3d. the slab is equidistant from the plates. The capacitor is given some charge. As X goes from 0 to 3d (1998)

(A) The magnitude of the electric field remains the same

(B) The direction of the electric field remains the same

(C) The electric potential increases continuously

(D) The electric potential increases at first, then decreases and again increases

Q.10 Two point charges Q and -Q/4 are separated by a distance x. Then (2001)

Q x -Q/4

(A) Potential is zero at a point on the axis which is x/3 on the right side of the charge -Q/4.

(B) Potential is zero at a point on the axis which is x/5 on the left side of the charge -Q/4.

(C) Electric field is zero at a point on the axis which is at a distance x on the right side of the charge -Q/4.

(D) There exists two points on the axis where electric field is zero.

Q.11 An electric charge 10^{-8} C is placed at the point (4m, 7m, 2m). At the point (1m, 3m, 2m), the electric *(2000)*

(A) Potential will be 18 V

(B) Field has no Y-component

(C) Field will be along Z-axis

(D) Potential will be 1.8 V

Q.12 Potential at a point A is 3 volt and at a point B is 7 volt, an electron is moving towards A from B. (2004)

(A) It must have some K.E. at B to reach A

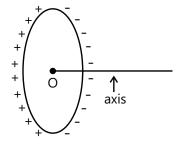
(B) It need not have any K.E at B to reach A

(C) to reach A it must have more than or equal to 4 eV K. E at B.

(D) When it will reach A, it will have K.E. more than or at least equal to 4eV if it was released from rest at B.

Q.13 The figure shows a non - conducting ring which has positive and negative charge non uniformly distributed on it such that the total charge is zero.

Which of the following statements is true? (2007)



(A) The potential at all the points on the axis will be zero.

(B) The electric field at all the points on the axis will be zero.

(C) The direction of electric field at all points on the axis will be along the axis.

(D) If the ring is placed inside a uniform external electric field then net torque and force acting on the ring would be zero.

Q.14 An electric dipole is placed at the center of a sphere. Mark the correct answer (2003)

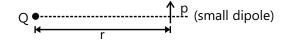
(A) The flux of the electric field through the sphere is zero

(B) The electric field is zero at every point of the sphere.

(C) The electric potential is zero everywhere on the sphere.

(D) The electric potential is zero on a circle on the surface.

Q.15 For the situation shown in the figure below (assume r>> length of dipole) mark out the correct statement (s) (2002)



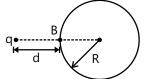
(A) Force acting on the dipole is zero

(B) Force acting on the dipole is approximately $\frac{pQ}{4\pi\epsilon_0 r^3}$

(C) Torque acting on the dipole is $\frac{pQ}{4\pi\epsilon_0 r^2}$ in clockwise direction

(D) Torque acting on the dipole is $\frac{pQ}{4\pi\epsilon_0 r^2}$ in anticlockwise direction.

Q.16 For the situation shown in the figure below, mark out the correct statement (s) (2006)



Hollow neutral conductor

(A) Potential of the conductor is
$$\frac{q}{4\pi\epsilon_0(d+R)}$$
.

(B) Potential of the conductor is $\frac{q}{4\pi\epsilon_0 d}$.

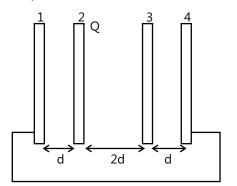
(C) Potential of the conductor can't be determined as nature of distribution of induced charges is not known

(D) Potential at point B due to induced charges is -qR

$$4\pi\varepsilon_0(d+R)d$$

Paragraph for Question No. 17 to 19

Four metallic plates are placed as shown in the figure. Plate 2 is given a charge Q whereas all other plates are uncharged. Plates 1 and 4 are jointed together. The area of each plate is same.



Q.17 The charge appearing on the right on the right side of plate 3 is (2009)

Q.18 The charge appearing on right side of plate 4 is (2009)

Q.19 The potential difference between plates 1 and 2 is (2009)

(A)
$$\frac{3}{2} \frac{\text{Qd}}{\varepsilon_0 A}$$
 (B) $\frac{\text{Qd}}{\varepsilon_0 A}$ (C) $\frac{3}{4} \frac{\text{Qd}}{\varepsilon_0 A}$ (D) $\frac{3\text{Qd}}{\varepsilon_0 A}$

(A) If statement-I is true, statement-II is true; statement II is the correct explanation for statement-I.

(B) If statement-I is true, statement-II is true; statement-II is not a correct explanation for statement-I.

(C) If statement-I is true; statement-II is false.

(D) If statement-I is false; statement-II is true.

Q.20 Statement-I: For practical purposes, the earth is used as a reference at zero potential in electrical circuits.

Statement-II: The electrical potential of a sphere of radius R with charge Q uniformly distributed on the

surface is given by
$$\frac{Q}{4\pi \in_0 R}$$
 (2008)

Q.21 Six point charges, each of the same magnitude q, are arranged in different manners as shown in column II. In each case, a point M and line PQ passing through M (potential at infinity is zero) due to the given charge distribution when it is at rest. Now, the whole system is set into rotation with a constant angular velocity about the line PQ. Let B be the magnetic field at M and μ be the magnetic moment of the system in this condition. Assume each rotating charge to be equivalent to a steady current. (2009)

Column I		Column II
(A) E = 0	$(p) \xrightarrow{+} \overbrace{-}^{+} \overbrace{+}^{-} \overbrace{+}^{Q}$	Charges are at the comers of a regular hexagon. M is at the centre of the hexagon. PQ is perpendicular to the hexagon.
(B) V ≠ 0	(q) P +-+-++ M Q	Charges are on a line perpendicular to PQ at equal intervals. M is the mid-point between the two innermost charges.
(C) B = 0	(r) (r) (r) (r) (r) (r) (r) (r)	Charges are placed on two coplanar insulation rings at equal intervals. M is the common centre of the rings. PQ is perpendicular to the plane of the rings.

Column I		Column II
(D) µ ≠ 0		Charges are placed at the corners of a rectangle of the sides a and 2a and at the mid points of the longer sides. M is at the centre of the rectangle. PQ is parallel to the longer sides.
	(t)+ PMQ	Charges are placed on two coplanar, identical insulating rings at equal intervals. M is the mid points between the centres of the rings. PQ is perpendicular to the line joining the centres and coplanar to the rings.

Q.22 A parallel plate air capacitor is connected to a battery. The quantities charge, voltage, electric field and energy associated with this capacitor are given by Q_0, V_0, E_0 and U_0 respectively. A dielectric slab is now introduced to fill the space between the plates with the battery still in connection. The corresponding quantities now given by Q, V, Eand U are related to the previous one as (1985)

 $(A) \ Q > Q_0 \qquad (B) \ V > V_0 \qquad (C) \ E > E_0 \qquad (D) \ U > U_0$

Q.23 A parallel plate capacitor is charged and the charging battery is then disconnected. If the plates of the capacitor are moved farther apart by means of insulating handles (1987)

- (A) The charge on the capacitor increases.
- (B) The voltage across the plates increases.
- (C) The capacitance increases.

(D) The electrostatic energy stored in the capacitor increases.

Q.24 A parallel plate capacitor of plate area A and plate separation d is charged to potential difference V and then the battery is disconnected. A slab of dielecric constant K is then inserted between the plates of the capacitor so as to fill the space between the plates If Q, E and W denote respectively, the magnitude of charge on each plate, the electric field between the plates (after the slab is inserted), and work done on the system, in question, in the process of inserting the slab, then **(1991)**

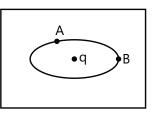
(A)
$$Q = \frac{\varepsilon_0 AV}{d}$$
 (B) $Q = \frac{\varepsilon_0 KAV}{d}$
(C) $E = \frac{V}{Kd}$ (D) $W = \frac{\varepsilon_0 AV^2}{2d} \left[1 - \frac{1}{K} \right]$

Q.25 A dielectric slab of thickness d is inserted in a parallel plate capacitor whose negative plate is at x=0 and positive plate is at x=3d. The slab is equidistant from the plates. The capacitor is given some charge. As x goes from 0 to 3d (1998)

- (A) The magnitude of the electric field remains the same
- (B) The direction of the electric field remains the same
- (C) The electric potential increases continuously

(D) The electric potential increases at first, then decreases and again increases

Q.26 An elliptical cavity is carved within a perfect conductor. A positive charge q is placed at the center of the cavity. The points A and B are on the cavity surface as shown in the figure. Then **(1999)**

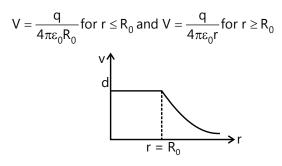


(A) Electric field near A in the cavity = electric field near B in the cavity.

- (B) Charge density at A= potential at B.
- (C) Potential at A=potential at B.

(D) Total electric field flux through the surface of the cavity is q/ ϵ_0 .

Q.27 For spherical symmetrical charge distribution, variation of electric potential with distance from center is given in diagram. Given that: **(2006)**



Then which option(s) are correct:

(A) Total charge within $2R_0$ is q

(B) Total electrostatic energy for $r \le R_0$ is zero

(C) At $r = R_0$ electric field is discontinuous.

(D) There will be no charge anywhere expect at $r = R_0$.

Q.28 Which of the following statement(s) is/are correct? (2011)

(A) If the electric field due to a point charge varies as

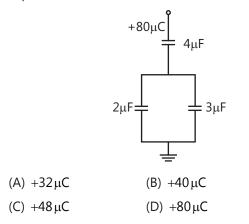
 $r^{-2.5}$ instead of r^{-2} , then the Gauss's law will still be valid

(B) The Gauss's law can be used to calculate the field distribution around an electric dipole

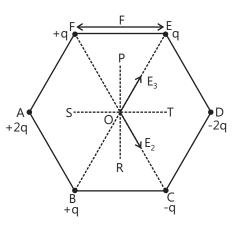
(C) If the electric field between two point charges is zero somewhere, then the sign of the two charges is the same

(D) The work done by the external force in moving a unit positive charge from point A at potential V_A to point B at potential V_B is $(V_B - V_A)$

Q.29 In the given circuit, a charge of +80 μ C is given to the upper plate of the μ F capacitor. Then in the steady state, the charge on the upper plate of the 3μ F capacitor is (2012)

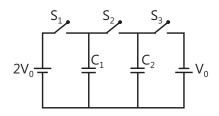


Q.30 Six point charges are kept at the vertices of a regular hexagon of side L and centre O, as shown in the figure. Given that $K = \frac{1}{4\pi\epsilon_0} \frac{q}{L^2}$, which of the following statement(s) is (are) correct ? (2012)



- (A) The electric field at O is 6K along OD.
- (B) The potential at O is zero
- (C) The potential at all points on the line PR is same
- (D) The potential at all points on the line ST is same

Q.31 In the circuit shown in the figure, there are two parallel plate capacitors each of capacitance C. The switch S_1 is pressed first to fully charge the capacitor C_1 and then released. The switch S_2 is then pressed to charge the capacitor C_2 . After some time, S_2 is released and then S_3 is pressed. After some time, (2013)



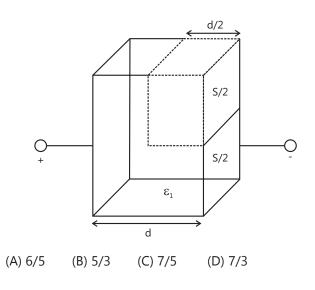
- (A) The charge on the upper plate of C_1 is 2 C V_0
- (B) The charge on the upper plate of C_1 is CV_0
- (C) The charge on the upper plate C_1 is 0
- (D) The charge on the upper plate of C_1 is CV_0

Q.32 A parallel plate capacitor has a dielectric slab of dielectric constant K between its plates that covers 1/3 of the area of its plates, as shown in the figure. The total capacitance of the capacitor is C while that of the portion with dielectric in between is C_1 . When the capacitor is charged, the plate area covered by the dielectric gets charge Q_1 and the rest of the area gets charge Q_2 . The electric field in the dielectric is E_1

and that in the other portion is E_2 . Choose the correct option/options, ignoring edge effects (2014)

(A)
$$\frac{E_1}{E_2} = 1$$
 (B) $\frac{E_1}{E_2} = \frac{1}{K}$ Q₁ $\frac{E_1}{E_2}$
(C) $\frac{Q_1}{Q_2} = \frac{3}{K}$ (D) $\frac{C}{C_1} = \frac{2+K}{K}$ Q₂ E_2

Q.33 A parallel plate capacitor having plates of area S and plate separation d, has capacitance C_1 in air. When two dielectrics of different relative permittivities $(\varepsilon_1 = 2 \text{ and } \varepsilon_2 = 4)$ are introduced between the two plates as shown in the figure, the capacitance becomes C_2 . The ratio $\frac{C_2}{C_1}$ is (2015)



MASTERJEE Essential Questions

JEE Main/Boards

JEE Advanced/Boards

Exercise 1

Q.1	Q.3	Q.4
Q.11	Q.13	Q.14
Q.18	Q.20	Q.29

Exercise 2

Q. 2	Q.3	Q.4
Q.5	Q.6	Q.11

Previous Years' Questions

Q.5	Q.23	Q.30
Q.31	Q.32	

Exercise 1

Q.3	Q.5	Q.6
Q.7	Q.14	Q.15
Q.16	Q.19	Q.20

Exercise 2

Q.6	Q.12
Q.15	Q.16
Q.18	Q.22
Q.34	
	Q.15 Q.18

Previous Years' Questions

Q.21 Q.27

Answer Key

JEE Main/Boards

Exercise 1

Q.1 1.29 μF

Q.2 5x10³ V

Q.3 4 μF

Q.4 1.39 μF

Q.5 2.67 x 10⁻² J

Q.6 2.21x10⁻⁷ J

Q.7 7.2F

Q.8 $\frac{C}{C'} = \frac{24}{25}$ **Q.9** C = 2C₀

Q.10 11.1% energy is increased

Q.11 $6x10^3$ V/m, $\Delta E = -12.15 \times 10^{-8}$ J $\Delta E = 30.4 \times 10^{-8}$ J

Q.12 18 μC

Q.13 $\phi_0 = \frac{\phi_A C_1 + \phi_B C_2 + \phi_D C_3}{C_1 + C_2 + C_3}$ **Q.14** (i) $\frac{E}{R_1}$ (ii) $\frac{E}{R_1 + R^3}$ **Q.15** 4.5g **Q.16** Both will travel the same distance **Q.17** 260volts, $6x10^{-4}$ C charge flows from 3 µF to 2 µF

Q.18 12 μC, 3 μC, 9 μC, 6 μC

Q.19 (i) 2.04V; (ii) 6.12 μC

Q.21 (a) Five $2 \mu C$ capacitors in series;

Exercise 2

Q.1 C	Q.2 D	Q.3 C	Q.4 D	Q.5 C	Q.6 A
Q.7 B	Q.8 B	Q.9 B	Q.10 C	Q.11 A	Q.12 C

(b) 3 parallel rows; each consisting of five; 2.0 µF capacitors in series Q.22 420 µC one one, 180 µC on two, 60 µC on remaining 3 capacitors **Q.23** 4x10²F,10²F Q.24 60 μC Q.25 0.16µF, 0.24µF **Q.26** $V_{max} < 9 \, kV$ **Q.27** (i) In parallel \rightarrow new capacitance greater than the initial one (ii) In series \rightarrow unchanged **Q.28** (i) $0.9 \,\mu\text{C} / \text{s}$; (ii) $1.09 \times 10^{-6} \,\text{J} / \text{s}$; (iii) $2.73 \times 10^{-6} \text{ J/s}$; (iv) $3.82 \times 10^{-6} \text{ J/s}$ **Q.29** (i) (a) 10s ; (b) 2 µC ; (c) 6.94s (ii) $q = 1.348 \times 10^{-8} C$ **Q.30** 1.8×10²⁴ Cm **0.31** 2.7×10⁶ V **Q.32** 0 **Q.33** 1.11×10⁻⁹C positive **Q.34** 1.8×10^{6} V **Q.35** Total charge is zero. Dipole moment $=7.5 \times 10^{-8}$ m along z-axis. **Q.36** (i) dV = 4E, (ii) $V_c > V_A$

Q.37 (i) 0

Previous Years' Questions

Q.1 A	Q.2 D	Q.3 D	Q.4 A	Q.5 A	Q.6 C
Q.7 B	Q.8 A	Q.9 D	Q.10 B	Q.11 A	Q.12 C
Q.13 B	Q.14 A	Q.15 B	Q.16 C	Q.17 B	Q.18 D
Q.19 D	Q.20 D	Q.21 B	Q.22 B	Q.23 C	Q.24 A
Q.25 C	Q.26 C	Q.27 A	Q.28 D	Q.29 A	Q.30 C
Q.31 C	Q.32 D	Q.33 B C	Q.34 A	Q.35 B	

JEE Advanced/Boards

Exercise 1

- **Q.1** 44.25pF
- **Q.2** 30V
- **Q.3** 0
- **Q.4** $\frac{32}{23}\mu$ F
- **Q.5** 10 μC
- **Q.6** $\frac{8}{3} \mu F$
- **Q.7** $\frac{A\epsilon_0 V}{d}$
- **Q.8** $\frac{25\varepsilon_0}{24}\frac{A}{d}$

Q.9 $\frac{2k(q-x)^2}{35r}$

Q.100.8

Q.119J

Q.12 C $\left(\frac{E}{R_1 + R_3}\right)R_3$ **Q.13** (a) $\frac{7}{50}A$ (b) Q₁ = 9µC, Q₂ = 0

Q.14 (a) $0.05 \left[1 - e^{-t/2} \right] \mu C$;

(b) 0.125 µJ

Q.15 (a)
$$I = \frac{V_0}{R} e^{-2t/Rc}$$
; (b) $\frac{1}{4}CV_0^2$
Q.16 $\frac{1}{2}\frac{q^2d}{\varepsilon_0 A}$
Q.17 (i) $\frac{5}{3}\left(\frac{\varepsilon_0 A}{d}\right)$;
(ii) $Q_3 = \frac{4}{3}\left(\frac{\varepsilon_0 AV}{d}\right)$; $Q_5 = \frac{2}{3}\left(\frac{\varepsilon_0 AV}{d}\right)$

Q.1869 mC

Q.19 (a) $\frac{100}{7}$ Volts (b) 28.56mC, 42.84mC, 71.4mC, 22.88mC

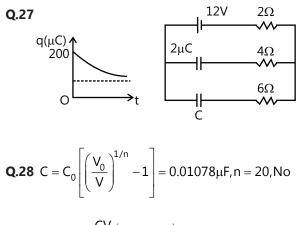
Q.20 150 μJ

Q.21 16 μC

Q.22
$$\frac{3}{5}$$

Q.23 W = $\frac{1}{2} A \epsilon_0 V_0^2 \left(1 - \frac{1}{K} \right)'$

Q.24 12Volt **Q.25** (i) 0.2×10^{-8} F, 1.2×10^{-5} J; (ii) 4.84×10^{-5} J (iii) 1.1×10^{-5} J **Q.26** 4.425 × 10⁻⁵ Amp



Q.29
$$q = \frac{CV}{2} (1 - e^{-t/RC})$$

Q.30
$$Q_A = 90\mu C, Q_B = 150\mu C, Q_C = 210\mu C, U_i$$

= 47.4mJ, U_f = 18mJ

Q.31 1.8×10^{5} sec

Q.32
$$\frac{k\overline{P}}{\sqrt{2}y^{3}}(-\overline{i}-2\overline{j})$$
Q.33
$$W_{\text{first step}} = \left(\frac{8}{3} - \frac{4}{\sqrt{5}}\right)\frac{Kq^{2}}{r}, W_{\text{second step}} = 0, W_{\text{total}} = 0$$
Q.34
$$\frac{Qq}{2\pi \epsilon_{0} L}$$
Q.35 (a)
$$H = \frac{4a}{3},$$
(b)
$$U = mg\left[2\sqrt{h^{2} + a^{2}} - h\right]$$
 equilibrium at
$$h = \frac{a}{\sqrt{3}}$$

Exercise 2

Single Correct Choice Type							
Q.1 A	Q.2 B	Q.3 B	Q.4 B	Q.5 A	Q.6 B		
Q.7 B	Q.8 A	Q.9 A	Q.10 D	Q.11 B	Q.12 C		
Q.13 B	Q.14 C	Q.15 B	Q.16 A	Q.17 D	Q.18 D		
Q.19 B	Q.20 C						
Multiple Correct Choice Type							
Q.21 A, B, C	Q.22 A, D	Q.23 A, D	Q.24 A, B	Q.25 B, C, D	Q.26 A, B, D		
Q.27 B, C	Q.28 A, C, D	Q.29 C, D	Q.30 A, C, D	Q.31 A, B, C, D	Q.32 A, B, C, D		
Q.33 B,D							
Assertion Reasoning Type							
Q.34 D	Q.35 C	Q.36 D					
Comprehension Type							
Paragraph 1:	Q.37 B	Q.38 B	Paragraph 2:	Q.39 A, C	Q.40 A, B, C		
Paragraph 3:	Q.41 A, C	Q.42 D					

Previous Years' Questions

Q.3 D	Q.4 C	Q.5 D	Q.6 A, D	Q.7 B, D	Q.8 A, C, D
Q.9 B, C	Q.10 A, B, C	Q.11 A	Q.12 A, C	Q.13 A	Q.14 A, D
Q.15 B, C	Q.16 A, D	Q.17 B	Q.18 B	Q.19 C	Q.20 B
$\textbf{Q.21} \text{ A} \rightarrow p, \text{ r, s; B} \rightarrow \text{r, s; C} \rightarrow p, \text{ q, t; D} \rightarrow \text{r, s}$			Q.22 A, D	Q.23 B, D	Q.24 A, C, D
Q.25 B, C	Q.26 C, D	Q.27 A, B, C, D	Q.28 C, D	Q.29 C	Q.30 A, B, C
Q.31 B, D	Q.32 A, D	Q.33 D			

Solutions

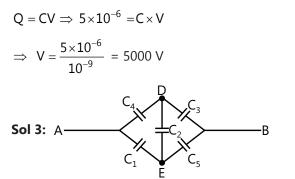
JEE Main/Boards

Exercise 1

Sol 1: Parallel
$$\Rightarrow$$
 (4.5 + 4.5) μ F = 9 μ F = C'₂

Total $\Rightarrow \frac{1}{C_{total}} = \frac{1}{3} + \frac{1}{3} + \frac{1}{9}$ $\rightarrow H = \frac{1}{3\mu F} + \frac{1}{C_2} + \frac{1}{3\mu F}$ $\frac{1}{C_{total}} = \frac{7}{9} \Rightarrow C_{total} = 9 / 7 \mu F = 1.29 \mu F$

Sol 2: We have



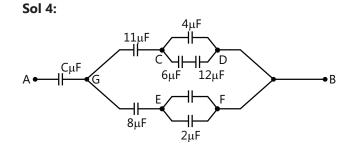
Now from symmetry, we can argue that the charge at $\rm C_2$ must be zero and hence potential diff. across D and E.

So (capacitance across ADB)⁻¹ = $\frac{1}{C_4} + \frac{1}{C_3} = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$

 \Rightarrow Capacitance across ADB = 2μ F

Similarly, Capacitance across AEB = 2μ F

So total capacitance = $2 + 2 = 4\mu F$



Capacitance b/w C and D

$$=4\mu F + \left(\frac{1}{6} + \frac{1}{12}\right)^{-1} \mu F$$

$$= 4\mu F + 3\mu F$$

Let capacitance b/w E and F

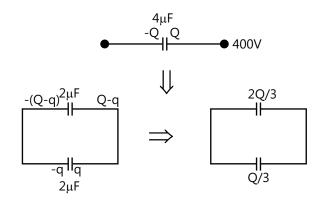
$$= 2 + 2 = 4 \mu F$$

Net capa. b/w G and B

$$= \left(\frac{1}{8} + \frac{1}{4}\right)^{-1} \mu F + \left(1 + \frac{1}{7}\right)^{-1} \mu F$$
$$= \left(\frac{8}{3} + \frac{7}{8}\right) \mu F = \frac{64 + 21}{24} \mu F = \frac{85}{24} \mu F$$
Now $1 = \frac{1}{6} + \frac{24}{85}$

$$\Rightarrow C = \frac{85}{61} \mu F = 1.39 \mu F$$

Sol 5: Now Q = $4 \times 10^{-6} \times 200 = 800$ HQ



Now, an applying Kirchhoff's law,

$$\frac{Q-q}{4\mu F} - \frac{q}{2\mu F} = 0$$

$$Q = 3q \Rightarrow q = Q/3$$

$$E_{initial} = \frac{1}{2} \times C \times V^{2} = \frac{1}{2} \times 4 \times 10^{-6} \times (200)^{2} = 8 \times 10^{-2}$$

$$E_{final} = Q^{2}_{1}/2C_{1} + Q^{2}_{2}/2C_{2} = \frac{4Q^{2}}{9 \times 2C_{1}} + \frac{Q^{2}}{2C_{2} \times 9}$$

$$= Q^{2} \left[\frac{2}{9C_{1}} + \frac{1}{18C_{2}} \right]$$

$$= (8 \times 10^{-4})^{2} \left[\frac{2}{9 \times 4 \times 10^{-6}} + \frac{1}{18 \times 2 \times 10^{-6}} \right] = \frac{64 \times 10^{-2}}{2 \times 6}$$

$$= 5.33 \times 10^{-2} J$$

$$\Rightarrow \text{ Energy lost} = 8 - 5.33 = 2.67 \times 10^{-2} J$$

Sol 6:
$$C = \frac{\varepsilon_0 A}{d} = \frac{8.854 \times 10^{-12} \times 100 \times 10^{-4}}{2 \times 10^{-3}}$$

= $\frac{8.854 \times 10^{-11}}{2} = 4.427 \times 10^{-11} F$
So, $E = \frac{1}{2} \times C \times V^2$
= $\frac{1}{2} \times 4.427 \times 10^{-11} \times (100)^2 = \frac{4.427}{2} \times 10^{-7} = 0.221 \mu J$

Sol 7: =
$$\frac{1}{2}$$
CV² =100×10³×3600
 \Rightarrow C = $\frac{200×10^3×3600}{(104)^2}$ = 7.2 F

Sol 8: (A) (Capacitance total) =
$$\frac{1}{C_1} + \frac{1}{C_2}$$

$$\Rightarrow \frac{d}{2 \times k_1 \varepsilon_0 A} + \frac{d}{2 \times k_2 \varepsilon_0 A}$$
Capacitance $^{-1} = \frac{d}{2 \varepsilon_0 A} \cdot \left[\frac{1}{k_1} + \frac{1}{k_2}\right]$

$$\Rightarrow C_A = \frac{2 \varepsilon_0 A}{d} \cdot \left[\frac{1}{k_1} + \frac{1}{k_2}\right]^{-1}$$
(B) Capacitance Total = $C_1 + C_2$

$$= \frac{k_1 \varepsilon_0 (A/2)}{d} + \frac{k_2 \cdot \varepsilon_0 \cdot (A/2)}{d}$$

$$\Rightarrow C_B = (k_1 + k_2) \cdot \frac{\varepsilon_0 A}{2d}$$
Sol, = $C_A / C_B = \frac{2 \varepsilon_0 A}{(k_1 + k_2) \cdot \varepsilon_0 A/2d}$

$$= \frac{C_A}{C_B} = \frac{4 \cdot k_1 k_2}{(k_1 + k_2)^2} = \frac{4 \times 2 \times 3}{(5)^2} = \frac{24}{25}$$
Sol 9: $C_A = \frac{\varepsilon_0 A}{d}$ and $C_B^{-1} = \frac{1}{C_1} + \frac{1}{C_2}$

$$= \frac{d}{4 \varepsilon_0 A} + \frac{d}{4 \varepsilon_0 A} = \frac{d}{2 \varepsilon_0 A} \Rightarrow C_B = \frac{2 \varepsilon_0 A}{d}$$
So $C_A / C_B = 1/2$
Sol 10: We have Q = CV
Now energy = $\frac{1}{2} \times CV^2$

$$V = \text{Same, but } C_1 = \frac{\varepsilon_0 A}{d} \text{ and } C_2 = \frac{\varepsilon_0 A}{0.9d}$$
So energy change
$$= -\frac{1}{2} \times \frac{\varepsilon_0 A}{d} \times V^2 + \frac{1}{2} \times \frac{\varepsilon_0 A}{0.9d} \times V^2 = \frac{1}{2} \times \frac{\varepsilon_0 A}{d} \times V^2 \cdot \left[\frac{1}{0.9} - 1\right]$$

$$= \text{Sol 11: } C = \frac{\varepsilon_0 A}{d} = \frac{9 \times 10^{-12} \times 100 \times 10^{-4}}{2 \times 10^{-2}}$$

=
$$4.5 \times 10^{-12}$$
 F
Change in energy = $\frac{1}{2} \times C_1 \times V^2 - \frac{1}{2} \times C_2 \times V^2$
= $E_{initial} - E_{final} = \frac{1}{2} \times V^2 \cdot [C_1 - C_2]$
= $\frac{1}{2} \times (300)^2 \cdot \varepsilon_0 A \left[\frac{1}{d_1} - \frac{1}{d_2} \right]$
= $\frac{9 \times 10^4 \times 9 \times 10^{-12} \times 100 \times 10^{-4}}{2 \times 10^{-2}} \times \left[\frac{1}{2} - \frac{1}{5} \right]$
= $40.5 \times 10^{-8} [3/10]$
= 1.215×10^{-7} J
E = $\frac{Q}{\varepsilon_0 A} = \frac{CV}{\varepsilon_0 A} = \frac{\varepsilon_0 A}{d_2 \cdot \varepsilon_0 A} \cdot V = \frac{300}{5 \times 10^{-2}} = 60 \times 10^2$
= 6×10^3 V/m
Now in 2nd case , Q = constant
We have Q = CV
= $4.5 \times 10^{-12} \times 300 = 13.5 \times 10^{-10} \cdot C$
= Q = $1.35 \times 10^{-9} \cdot C$
Now change in energy: $E_{initial} - E_{final}$
 $\Rightarrow \left(\frac{Q^2}{2C_1} - \frac{Q^2}{2C_1} \right) = \frac{Q^2}{2} \cdot \left[\frac{d_1}{\varepsilon_0 A} - \frac{d_2}{\varepsilon_0 A} \right]$
= $\frac{Q^2}{2\varepsilon_0 A} [d_1 - d_2] = \frac{Q^2 \cdot (d_1 - d_2)}{2\varepsilon_0 A}$
= $\frac{(1.35 \times 10^{-9})^2 \cdot (2 - 5) \times 10^{-2}}{2 \times 9 \times 10^{-12}} = \frac{(1.35 \times 10^{-9})^2 \times (-3)}{2 \times 9 \times 10^{-12}}$
= $\frac{-(1.35 \times 10^{-9})^2}{2 \times 3 \times 10^{-12}} = -0.3 \times 10^{-6} = -3 \times 10^{-7}$ Joules
Sol 12: $\int_{0}^{12V} \frac{2\Omega}{4\Omega}$

Now no current will pass through the capacitor.

So, i = 12/8 = 3/2A

Thus, potential diff. across capacitor

= $6 \times 3 / 2 = 9V \implies Q = CV = 18\mu C$.

Sol 13: $q_1 + C_1$ $C_2 q_1 + Q_3 + Q_$

$$\Rightarrow (C_1 + C_2 + C_3)\phi_0 = C_1\phi_A + C_2\phi_B + C_3\phi_D$$
$$\Rightarrow \phi_0 = \frac{C_1\phi_A + C_2\phi_B + C_3\phi_D}{C_1 + C_2 + C_3}$$

Sol 14: (i) Now, at just t = 0, charge at $C_1 = 0$ and charge at $C_2 = 0$ so V = Q / C = 0 so potential diff. between AB = 0

$$i = E / R_1 + R_{AB} = E / R_1$$

(ii) After long time , no current through both capacitors

$$\Rightarrow E = iR_1 + iR_3 \Rightarrow i = \frac{E}{R_1 + R_3}$$

Sol 15: E due to one plate =
$$\frac{Q}{2\epsilon_0 A}$$

So force = $Q \cdot \times \frac{Q}{2\epsilon_0 A} = \frac{Q^2}{2\epsilon_0 A}$
So $T = mg = \frac{Q^2}{2\epsilon_0 A}$
 $mg = \frac{C^2 V^2}{2\epsilon_0 A}$
 $m = \frac{C^2 V^2}{2\epsilon_0 A g} = \frac{\epsilon_0 A \cdot V^2}{2g d^2} = \frac{9 \times 10^{-12} \times 10^{-12} \times (5 \times 10^8)^2}{2 \times 10 \times (5 \times 10^{-3})^2}$
= 4.5×10⁻³ kg = 4.5 gm

Sol 16: Let there, masses be m_e and m_i

Then Vd =
$$\frac{1}{2}$$
m_ev_e² = $\frac{1}{2}$ ×M_i×V_i² (i)

Now acceleratio of particles $\Rightarrow \frac{Ee}{m_e} = a_e$ and $= \frac{Ee}{M_i} = a_i$

So time to hit the plate \Rightarrow S = ut + $\frac{1}{2}at^2$

$$\Rightarrow \sqrt{\frac{2d}{a_e}} = t_e = \sqrt{\frac{2d.m_e}{Ee}}$$

...(ii)

Similarly,
$$t_i = \sqrt{\frac{2d}{a_i}} = \sqrt{\frac{2d.M_i}{Ee}}$$

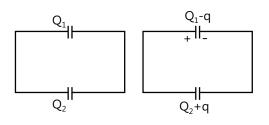
Now distance = $V_e \times t_e$

$$= \sqrt{\frac{2Vd}{m_e}} \times \sqrt{\frac{2d.m_e}{Ee}}$$
$$= 2d.\sqrt{\frac{V}{Ee}} \text{ (independent of mass)}$$

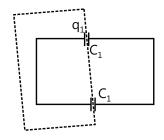
Same distance can be found for the ion and hence the time is same.

Sol 17: $Q = 3 \times 300 = 900 \,\mu$ C.

And $Q_2 = 2 \times 200 = 400 \,\mu$ C.



So using Kirchhoff's law, $\Rightarrow \frac{Q_1 - q}{3} - \frac{(Q_2 + q)}{2} = 0$ $\Rightarrow 2Q_1 - 2q = 3Q_2 + 3q \Rightarrow q = \frac{2Q_1 - 3Q_2}{5}$



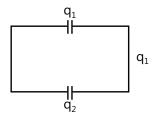
$$q_1 + q_2 = 900 - 400 = 500\,\mu\,C$$

(from charge conservation)

Also
$$\frac{q_1}{3} - \frac{q_2}{2} = 0 \implies 2q_1 = 3q_2 \implies \frac{q_1}{q_2} = \frac{3}{2}$$

$$\Rightarrow$$
 q₁ = 300µC and q₂ = 200µC

$$q_1 + q_2 = 1300 \,\mu$$
C



$$\begin{array}{l} \cdot\cdot \ \Rightarrow \ \frac{q_1}{3} = \frac{q_2}{2} \ \Rightarrow \ q_1 = \frac{3}{2} \ q_2 \\ q_2 = 520\,\mu\text{C} \ , q_1 = 780\,\mu\text{C} \\ \text{Potential difference} = \ \frac{520\,\mu\text{C}}{2\,\mu\text{F}} = 260 \text{ Volts} \end{array}$$

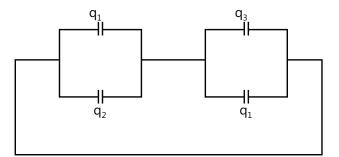
Thus the charge will flow from each positive terminal to the negative terminal.

Sol 18: No current will pass through, the upper portion, and voltage difference between the capacitors would be same as ϵ .

$$C_{\text{total}} = \left(\frac{1}{C_1 + C_2} + \frac{1}{C_3 + C_4}\right)^{-1} = \left(\frac{1}{10} + \frac{1}{10}\right)^{-1} = 5\mu F$$

Actual emf =
$$\varepsilon - \frac{(4)}{(3+1)} \times 1 = \varepsilon - 1 = 3V$$

So
$$Q = CV = 5\mu F \times 9 = 15\mu C$$



Now,
$$q_1 + q_2 = 15 \mu C$$

and
$$\frac{q_1}{C_1} - \frac{q_2}{C_2} = 0$$

$$\Rightarrow \frac{q_1}{8} = \frac{q_2}{2} \Rightarrow q_1 = 4q_2 \qquad \dots (i)$$

$$\Rightarrow q_1 = 12\mu C, q_2 = 3\mu C$$
Also $(q_3 + q_4) = 15$
 $\frac{q_3}{c_3} - \frac{q_4}{c_4} = 0$
 $\frac{q_3}{6} = \frac{q_4}{4} \Rightarrow \frac{q_3}{q_4} = \frac{3}{2}$
 $\Rightarrow q_3 = 9\mu C \Rightarrow q_4 = 6\mu C$

Sol 19: Diagram-1

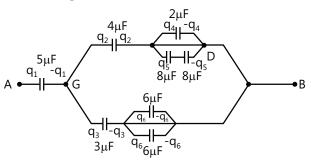


Diagram-2

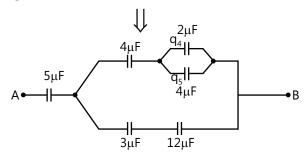
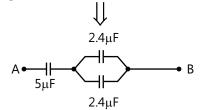


Diagram-3



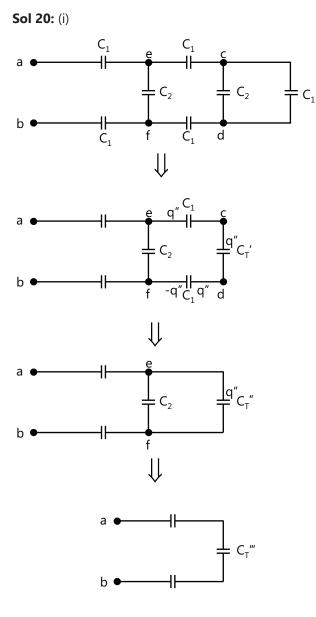
$$C_{total} = \left(\frac{1}{5} + \frac{1}{4.8}\right)^{-1} = \left(\frac{1}{5} + \frac{5}{24}\right)^{-1} = \frac{120}{49} = 2.45 \mu F$$

So, $Q = CV = 2.45 \times 10 = 24.5 \mu C$ Now from diagram (3), capacitance = same \Rightarrow charge is equally divided.

$$\Rightarrow q_2 = q_3 = \frac{24.5}{2} = 12.25 \,\mu\text{C}$$

Now from diagram (2)

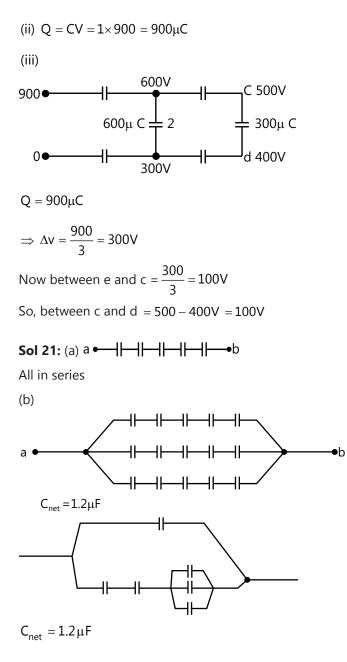
 $q_{4} + q_{5} = q_{2}$ And $\frac{q_{4}}{2} - \frac{q_{5}}{4} = 0 \implies 2q_{4} - q_{5}$ So $q_{4} = 12.25/3\mu C = 4.08\mu C$ and $q_{5} = \frac{12.25 \times 2}{3} = 8.166\mu C$ (i) So voltage diff. = $q / c = \frac{4.08\mu C}{2\mu F} = 2.04 V$ (ii) Charge = $\frac{12.25\mu C}{2} = 6.12\mu C$ $[q_{3} = 12.25\mu C \text{ and } 2q_{6} = q_{3}]$



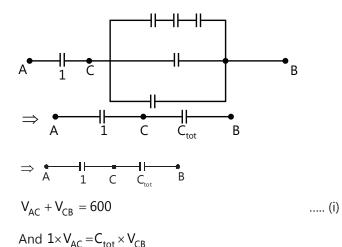
We have

$$C_{T} = \left(\frac{1}{3} + \frac{1}{3} + \frac{1}{2}\right)^{-1} = \left(\frac{2}{3} + \frac{1}{2}\right)^{-1} = (6 / 7)\mu C$$

Now $C_{T}' = \frac{6}{7} + 2 = \frac{20}{7}\mu C$
Now $C_{T}'' = \left(\frac{7}{20} + \frac{2}{3}\right)^{-1} = \left(\frac{61}{60}\right)^{-1} = \left(\frac{60}{61}\right)\mu C$
 $\Rightarrow C_{T}''' = \frac{60}{61} + 2 = \frac{182}{61}\mu C$
 $C_{Total} = \left(\frac{61}{182} + \frac{1}{3} + \frac{1}{3}\right)^{-1} = \left(\frac{61}{182} + \frac{2}{3}\right)^{-1} = 1\mu C$



Sol 22: By trial and error



$$V_{AC} = \frac{7}{3} \times V_{CB} \implies V_{AC} \Rightarrow \frac{7}{3} \cdot V_{CB}$$

$$\Rightarrow V_{AC} = 7 \times \frac{600}{10} = 420 \text{ V and } V_{CB} = 600 \times \frac{3}{10} = 180 \text{ V}$$

$$\Rightarrow Q_{AC} = CV = 1\mu C \times 420 = 420 \mu C$$

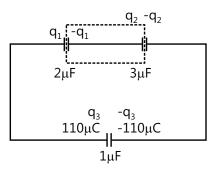
And $Q_{BC} = 180 \times 1 = 180 \mu C$
And in each 3, q will be equally distributed
 $q = 420 - 2 \times 180$ (on each)
Sol 23: We have $\frac{1}{2} \times C_1 \times (2)^2 + \frac{1}{2} \times C_2 \cdot (2)^2 = 10 \times 10^2$

$$\Rightarrow C_1 + C_2 = 500$$

And $160 = \frac{Q^2}{2C_1} + \frac{Q^2}{2C_2} \implies 320 = Q^2 \left[\frac{1}{C_1} + \frac{1}{C_2}\right]$
 $= V^2 \times C_{eq}^2 \left[\frac{1}{C_1} + \frac{1}{C_2}\right] = \frac{V^2}{\left(\frac{1}{C_1} + \frac{1}{C_2}\right)}$
 $320 = \frac{V^2 \cdot C_1 \cdot C_2}{C_1 + C_2}$
 $\Rightarrow 80 = \frac{C_1 \cdot C_2}{500} \implies C_1 \cdot C_2 = 40000$...(i)

 \Rightarrow On solving, C₁ = 400, C₂ = 100

Sol 24:



We have $q_3 + q_1 = 110\mu C$ and $q_2 - q_1 = 0$ $\Rightarrow q_2 = q_1$ and $\frac{q_3}{1} - \frac{q_1}{2} - \frac{q_2}{3} = 0 \Rightarrow q_3 = \frac{q_1}{2} + \frac{q_2}{3}$ $110 - q_1 = \frac{5 \cdot q_1}{6} \Rightarrow q_1 = \frac{6 \times 110}{11} = 60 \Rightarrow q_1 = 60\mu C$ So, $q_2 = 60\mu C$ and $q_5 = 50\mu C$ So, $110 - 50 = 60\mu C$ charge passes through wire.

Sol 25:
$$100V$$

 C_A
 C_B
 C_B

We have $C_A \times 60 = C_B \times 40$ (q charge is same)

$$\Rightarrow \frac{C_A}{C_B} = \frac{2}{3}$$

Similarly

$$\Rightarrow \frac{C_A + 2}{C_B} = 9 \Rightarrow C_A + 2 = \frac{9 \times 3}{2} \times C_A = 2 = \frac{25}{2}C_A$$
$$= C_A = \frac{4}{25} \Rightarrow C_A = 0.16\mu F$$

Similarly, $\frac{C_A}{C_B} = \frac{2}{3} \implies C_B = 0.24 \,\mu\text{F}$

Sol 26:
$$\bigvee_{e}$$
 $\downarrow \qquad 0$
 C_1 C_2

For $\,V_{max.(inseries)}\,,\,Q$ = same for both the capacitance (in series)

So,
$$C_1(V_{max} - V) = C_2(V - 0)$$

 $\Rightarrow 1 \times (V_{max} - V) = 2.(V - 0)$
 $\Rightarrow V_{max} - V = 2V \Rightarrow V = \frac{V_{max}}{3}$

Now $V < 4 \, kV$

$$\Rightarrow \frac{V_{max}}{3} < 4 \Rightarrow V_{max} < 12 \text{ kV}$$

And $V_{max} - V < 6kV$

$$\Rightarrow \frac{2V_{max}}{3} < 6kV \Rightarrow V_{max} < 9kV$$

Lower limit is 9 kV

Sol 27:
$$C_{eq}$$
 (Series) = $\frac{C_1 \cdot C_2}{(C_1 + C_2)}$
= $\left(\frac{1}{C_1} + \frac{1}{C_2}\right)^{-1} = \left(\frac{d+a}{\varepsilon_0 A} + \frac{d-a}{\varepsilon_0 A}\right)^{-1} = \left(\frac{2d}{\varepsilon_0 A}\right)^{-1} = \frac{\varepsilon_0 A}{2d}$

Which is same as without any difference a.

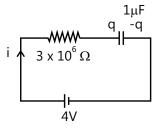
(unchanged)

$$C_{eq} \text{ (parallel)} = C_1 + C_2$$
$$= \varepsilon_0 A \cdot \left[\frac{1}{d+a} + \frac{1}{d-a} \right] = \frac{\varepsilon_0 A \cdot (2d)}{(d^2 - a^2)}$$

Without any a difference , $C_{eq} = \epsilon_0 A \times \left[\frac{1}{d} + \frac{1}{d}\right] = \frac{2\epsilon_0 A}{d}$

Now $1-a^2/d^2 < 1$ so the capacitance increases in case of parallel.

Sol 28:



(i) We have , iR + q / c = 4 $\Rightarrow iCR + q - 4C \Rightarrow dq + q - 4$

$$\Rightarrow 1CR + q = 4C \implies \frac{1}{dt} + \frac{1}{RC} = \frac{1}{R}$$

$$\Rightarrow \int_{0,0}^{q,t} d\left[q.e^{t/RC}\right] = \frac{4}{R} \int_{0}^{t} e^{t/RC}.dt$$

$$q.e^{t/RC} = \frac{4}{R}.(RC) = \left[e^{t/RC} - 1\right]$$

$$\Rightarrow q = 4C \left[1 - e^{-t/RC}\right]$$
Now $\frac{dq}{dt} = 4C.\left(\frac{1}{RC}\right).e^{-t/RC}$

$$= \frac{4}{3 \times 10^{6}} \times e^{-1/3} = 0.96 \,\mu\text{C/s}$$
(ii) $E = x \times \frac{Q^{2}}{2c}$

$$\Rightarrow \frac{dE}{dt} = \frac{1}{2C} \times 2 \times q. \frac{dq}{dt} = \frac{q}{C}.\frac{dq}{dt}$$

$$= \frac{4C\left[1 - e^{-1/3}\right]}{C}.\frac{4}{3 \times 10^{6}} \times e^{-1/3} = 1.09 \times 10^{-6} \text{ J/s}$$
(iii) $P = i^{2}R = \left(\frac{dq}{dt}\right)^{2}.R$

$$= (0.96 \,\mu\text{C})^{2}.3 \times 10^{6}$$

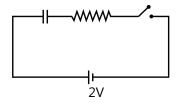
= $(0.96)^2 \times 3 \ \mu J = 2.73 \ \mu J / s$

(iv) Energy = Energy in Resistance + Energy in capacitance

$$= (2.73 + 1.09) \times 10^{-6} \text{ J/s}$$

 $= 3.82 \times 10^{-6} \text{ J/s}$

Sol 29:



(a) t = RC = $10^7 \times 10^{-6} = 10$ sec

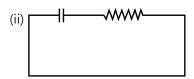
(b) Q = CV = $2 \times 1 \ \mu C = 2 \mu C$

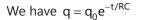
(c) Now , as in Ques. 29 above, $q = 2 \times \mu C [1 - e^{-t/10}]$

$$\Rightarrow \frac{1}{2} = 1 - e^{-t/10}$$

$$\Rightarrow e^{t/10} = 2$$

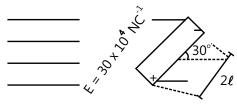
 \Rightarrow t = 10ln2 = 6.94 sec





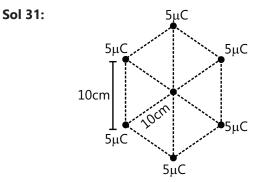
Now
$$q = 2 \times e^{-50/10} = 2 \cdot e^{-5} = 0.0135 \ \mu C$$

Sol 30:



 $T = (E_q) (2 \ell) \sin 30^{\circ}$ $T = E \sin 30^{\circ}. (q.2l)$ $\Rightarrow \text{Dipole moment (D)}$ $= q.2 l = \frac{T}{E \sin 30^{\circ}} = \frac{27 \times 10^{26}}{30 \times 10^4 \times 1/2}$

= 1.8 × 10²⁴ cm



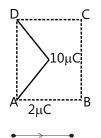
Potential at center due to one charge = $\frac{kq}{r}$

$$= \frac{9 \times 10^9 \times 5 \times 10^{-6}}{10^{-1}} = 45 \times 10^4 \text{ V}$$

Potential at center due to all the charges

$$= 6 \times V_{a} = 2.7 \times 10^{6} V$$

Sol 32:



$$V_{A} = \frac{(k)(10\mu C)}{\frac{a}{\sqrt{2}}} = \frac{\sqrt{2}k}{a} (10 \ \mu C)$$

$$V_{B} = \frac{(k)(10\mu C)}{\left(\frac{a}{\sqrt{2}}\right)} = \frac{\sqrt{2}k}{a} (10 \ \mu C)$$

Work done is moving charge of $2\mu C = q(V_{_B} - V_{_A}) = 2\mu C$ (0) = 0

 100×0.1

k

Sol 33:

$$q$$

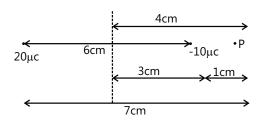
$$r = 0.1m$$

$$v = 100 \text{ volts}$$

$$\Rightarrow \frac{kq}{r} = 100 \Rightarrow q =$$

 $= 1.1 \times 10^{-9} C$ (positive)

Sol 34:



$$V_{p} = K \frac{q_{1}}{r_{1}} + k \frac{q_{2}}{r_{2}} = k \left(\frac{q_{1}}{r_{1}} + \frac{q_{2}}{r_{2}} \right)$$

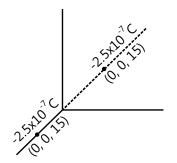
 $q_1 = -10\mu c$, $r_1 = 1 cm$

 $q_2 = 20\mu c$, $r_2 = 7$ cm

Put the values in the equation for $V_{p'}$

 $V_{p} = -1.8 \times 10^{6} V$





Total charge of system

 $= -2.5 \times 10^{-7} \text{ C} + 2.5 \times 10^{-7} \text{ C} = 0$

Dipole moment of system

 $= -2.5 \times 10^{-7} \times (-15 - 15) \times 10^{-2}$

 $=-7.5 \times 10^{-8}$ Cm (along –ve z-axis)

Sol 36: The motion perpendicular to electric field won't account in work

:. Work done in moving charge from A to B is

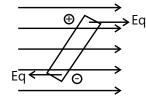
E(6-2) = 4E

 \therefore Potential difference between A and B = 4E also

 $V_{_B} = V_{_C}$ (since no parallel movement along E)

$$\Rightarrow$$
 V_C – V_A = 4E and V_C > V_A

Sol 37: (i)



 \therefore Net force = Eq – Eq = 0 (Assuming length of dipole is small)

(ii)
$$U_{i} = - \vec{P}.\vec{E} = -PE$$

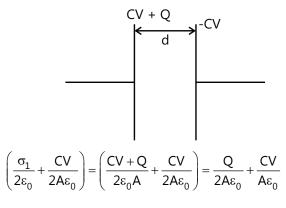
 $U_f = \vec{P}.\vec{E} = PE$

 $U_f - U_i = 2PE =$ work done is rotating dipole

Exercise 2

Single Correct Choice Type

Sol 1: (C)



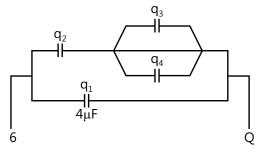
work done = $E \times d = \frac{Q}{2} \frac{d}{A\epsilon_0} + CV \times \frac{d}{A\epsilon_0}$

$$= \frac{Q}{2C} + C \times V' \times \frac{1}{C} = V + \frac{Q}{2C}$$

Sol 2: (D) $C_{eq} = C \left(\frac{1}{C} + \frac{1}{2C} + \frac{1}{2C} \right)^{-1} = C + C / 2 = 3C / 2$ Q = 60 × 3C / 2 = 90C

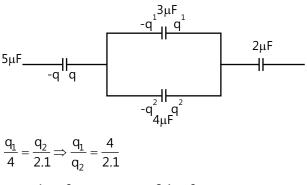
Now $\frac{q_1}{C} = \frac{q_2}{C/2}$; $q_1 = 2q_2$ and $q_1 + q_2 = 90C$ $\Rightarrow q_2 = 30C$. So potential difference = Q/C = 30V

Sol 3: (C)



$$C_{eq} = 4 + \left(\frac{1}{3} + \frac{1}{7}\right)^{-1} = 4 + \left(\frac{10}{21}\right)^{-1} = 6.1 \mu C.$$

So $q_{tot} = q_1 + q_2 = (6 / 6.1)\mu C$



$$q_1 = \frac{4}{6.1} \times \frac{6}{6.1} \mu C$$
 and $q_2 = \frac{2.1}{6.1} \times \frac{6}{6.1} \mu C$

and also
$$q_3 + q_4 = q_2$$

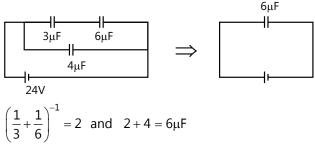
and
$$\frac{q_3}{2} = \frac{q_4}{5}$$

 $\Rightarrow q_4 = \frac{5}{7} \times q_2 = \frac{5}{7} \times \frac{2.1}{6.1} \times \frac{6}{6.1} \mu C$
 $\frac{q_4}{q_1} = \frac{\frac{5}{7} \times \frac{2.1}{6.1} \times \frac{6}{6.1}}{\frac{4 \times 6}{6.1 \times 6.1}} = \frac{3}{8}$

Sol 4: (D) 4 times in series. Let each be x, then $\frac{x}{4} = 16\mu F \Rightarrow x = 4\mu F$ Which is possible when 8 are connected in parallel

 $\Rightarrow 8 \times 4 = 32$

Sol 5: (C)



So charge = $Q = 6\mu F \times 24 = 144\mu C$

That much charge is divided in 4μ F and 2μ F (above eq. capacitance)

$$\frac{q_1}{4} = \frac{q_2}{2} \Rightarrow q_1 = 2q_2$$
$$\Rightarrow q_2 = \frac{144\mu F}{3} = 48\mu C$$

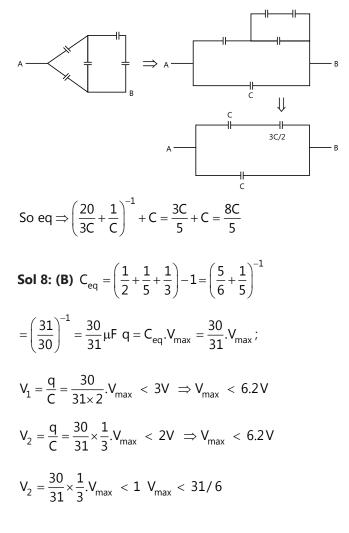
Out of this again, this is divided in $5\mu F$ and $1\!\mu V$

$$\frac{q_1}{5} = \frac{q_2}{1} \Rightarrow q_1 = 5q_2$$
$$\Rightarrow q_6 = \frac{48}{6} = 8\mu C$$
so energy = $\frac{Q^2}{2C} = \frac{8 \times 8}{2 \times 1} = 32\mu J$

Sol 6: (A) Charge on right should be positive and

$$q_1 + q_2 = 20\mu C \text{ and } \frac{q_1}{3} = \frac{q_2}{4} \Longrightarrow \frac{q_1}{q_2} = \frac{3}{4}$$
$$\Longrightarrow q_1 = \frac{3}{7} \times 20 = \frac{60}{7} = 8.57\mu C$$

Sol 7: (B)

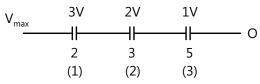


Sol 9: (B)
$$\frac{\sigma}{\epsilon_0} = 10^5 \,\text{V} \,/\,\text{m} \Rightarrow \frac{\sigma}{2\epsilon_0} = 0.5 \times 10^5 \,\text{V} \,/\,\text{m}$$

Now, force =
$$\frac{\sigma}{2\epsilon_0} \times Q = 0.5 \times 10^5 \times 1\mu C = 0.05 \text{ N}$$

Sol 10: (C) Force
$$=\frac{\sigma}{2\epsilon_0} \times Q = \frac{Q^2}{2A\epsilon_0}$$

so Force $\propto Q^2$



Now, when d is halved \Rightarrow C is doubled; Q=CV \Rightarrow Q is doubled.

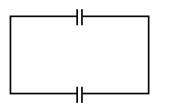
So Force $\propto Q^2 \Rightarrow$ F becomes four times.

Sol 11: (A)
$$d_{eff} = \frac{d/2}{k_1} + \frac{d/2}{k_2} = d\left(\frac{k_1 + k_2}{2k_1k_2}\right)$$

$$\therefore k_{eff} = \frac{d}{d_{eff}} = \frac{2k_1k_2}{k_1 + k_2}$$

Also,
$$C = \epsilon_0 \frac{A}{d_{eff}} = \frac{2 \epsilon_0 A(k_1k_2)}{k_1 + k_2}$$

Sol 12: (C)

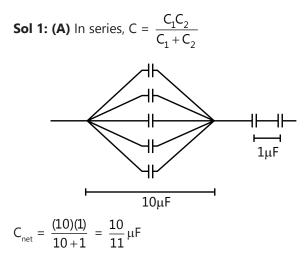


Capacitance increases = kC_0

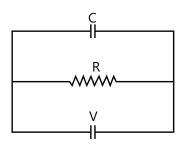
Now,

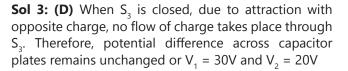
$$\begin{split} & q_i = C_i V = 60 \mu C \quad \text{and} \quad q_f = C_f V = 180 \mu C (60 + 120) \\ & \Rightarrow \ C_f = k C_i \ \Rightarrow \ k = C_i . V = 180 \mu C \Rightarrow k = 3 \end{split}$$

Previous Years' Questions



Sol 2: (D) Since, the capacitor plates are directly connected to the battery, it will take no time in charging





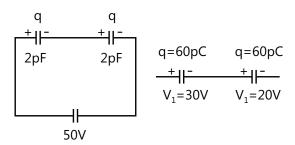
Alternate solution

Charges on the capacitors are

 $q_1 = (30)(2) = 60pC$ and

 $q_2 = (20)(3) = 60pC \text{ or } q_1 = q_2 = q(say)$

The situation is similar as the two capacitors in series are first charged with a battery of emf 50 V and then disconnected.



 \therefore When S₃ is closed, V₁ = 30V and V₂ = 20 V.

Sol 4: (A) Due to attraction with positive charge, the negative charge on capacitor A will not flow through the switch S.

Sol 5: (A) After time t, thickness of liquid will

remain
$$\left(\frac{d}{3} - vt\right)$$

Now, time constant as function of time:

$$\tau_{c} = CR = \frac{\varepsilon_{0}(1)R}{\left(d - \frac{d}{3} - vt\right) + \frac{d/3 - vt}{2}}$$
$$\left(Applying C = \frac{\varepsilon_{0}A}{d - t + \frac{t}{k}}\right)$$
$$= \frac{6\varepsilon_{0}R}{5d + 3Vt}$$

Sol 6: (C) Option C is correct because electron gets attracted towards positive charge (moves against electric field) larger the potential, lower the potential energy for electron.

 $\therefore U = V(-q)$

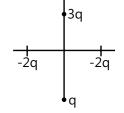
Given, V = 5 volts

but V =
$$\frac{\sigma}{\varepsilon_0}$$
.r

$$\Rightarrow r = \frac{\varepsilon_0(V)}{\sigma} = \frac{8.854 \times 10^{-12} \times 10}{10^{-7}}$$

= 8.8 × 10⁻⁴ m = 0.88 mm

Sol 8: (A)



(Center of charge) of negative charges is origin (center of charge) of positive charges is

$$\frac{3q(a)-q(a)}{4q} = \frac{q}{2}$$

Dipole moment

$$\frac{4q}{-4q} = \frac{a/2}{-4q}$$

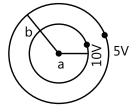
$$P = 4q \left(\frac{a}{2}\right)\hat{j} = 2qa \hat{j}$$

Sol 9: (D) Potential of each drop = V = $\frac{kq}{R} \Rightarrow q = \frac{VR}{k}$ If n drops coalse, Q = nq = $n\frac{VR}{k}$ Radius R' = $n^{1/3}$ R The potential of new drop = $\frac{nkVR}{kn^{1/3}R} = Vn^{2/3}$

Sol 10: (B) The potential at center is same as that of the surface.

 \therefore V = 10 Volts

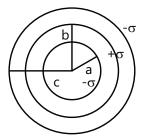
Sol 11: (A)



At center the potential will be same as the potential of the sphere enclosing it first

If it is any other potential, there will exist a electric field inside sphere contradicting gauss law.

Sol 12: (C)



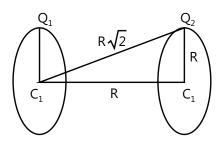
Potential at a due to charge of $a = -(\sigma / \in_0)(a)$ Potential at b due to charge of $b = (\sigma / \in_0)(b)$ Potential at C due to charge of $c = -(\sigma / \in_0)(c)$ \therefore Potential at $a = \frac{\sigma}{\epsilon_0}(b - a - c)$ **Sol 13: (B)** Electric potential at any point inside a hollow metallic sphere is constant. Therefore, if potential at surface is 10 V, potential at centre will also be 10 V.

Sol 14: (A) In such situation potential difference depends only on the charge on inner sphere. Since, charge on inner sphere is unchanged. Therefore, potential difference V will remain unchanged.

Sol 15: (B)
$$V_{C_1} = V_{Q_1} = V_{Q_2} = \frac{1}{4\pi\epsilon_0} \frac{Q_1}{R} + \frac{1}{4\pi\epsilon_0} \frac{Q_2}{R\sqrt{2}}$$

$$= \frac{1}{4\pi\epsilon_0 R} \left(Q_1 + \frac{Q_2}{\sqrt{2}} \right)$$

Similarly
$$V_{C_2} = \frac{1}{4\pi\epsilon_0 R} \left(Q_2 + \frac{Q_1}{\sqrt{2}} \right)$$

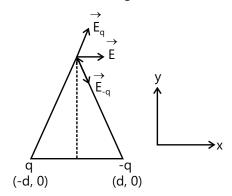


$$\therefore \Delta V = V_{C_1} - V_{C_2}$$
$$= \frac{1}{4\pi\epsilon_0 R} \left[(Q_1 - Q_2) - \frac{1}{\sqrt{2}} (Q_1 - Q_2) \right]$$

$$= \frac{Q_1 - Q_2}{\sqrt{2(4\pi\epsilon_0 R)}} (\sqrt{2} - 1)$$

 $W = q\Delta V = q(Q_1 - Q_2)(\sqrt{2} - 1)/\sqrt{2} (4\pi\epsilon_0 R)$

Sol 16: (C) The diagrammatic representation of the given question is shown in figure.



The electrical field E at all points on the x-axis will not have the same direction.

For $-d \le x \le d$, electric field is along positive x-axis while for all other points it is along negative x-axis. The electric field $\stackrel{\rightarrow}{E}$ at all points on the y-axis will be parallel to the x-axis (i.e., \hat{i})

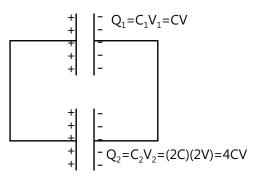
The electrical potential at the origin due to both the charges is zero, hence no work is done in bringing a test charge from infinity of the origin.

Dipole moment is directed from the -q charge to the +q charge (i.e., $-\hat{i}$ direction)

Sol 17: (B) The diagrammatic representation of given problem is shown in figure.

The net charge shared between the two capacitors is

$$Q' = Q_2 - Q_1 = 4CV - CV = 3CV$$



The two capacitors will have the same potential, say V' The net capacitance of the parallel combination of the two capacitors will be

 $C' = C_1 + C_2 = C + 2C = 3C$

The potential difference across the capacitors will be

$$V' = \frac{Q'}{C'} = \frac{3CV}{3C} = V$$

The electrostatic energy of the capacitors will be

$$U' = \frac{1}{2}C'V'^2 = \frac{1}{2}(3C)V^2 = \frac{3}{2}CV^2$$

Sol 18: (D) Potential at origin will be given by

$$V = \frac{q}{4\pi\epsilon_0} \left[\frac{1}{x_0} - \frac{1}{2x_0} + \frac{1}{3x_0} - \frac{1}{4x_0} + \dots \right]$$
$$= \frac{q}{4\pi\epsilon_0} \cdot \frac{1}{x_0} \left[1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots \right] = \frac{q}{4\pi\epsilon_0 x_0} \ln(2)$$

Sol 19: (D) Electric field within the plates $\vec{E} = \vec{E}_{Q_1} + \vec{E}_{Q_2}$

$$\mathsf{E} = \mathsf{E}_1 - \mathsf{E}_2 = \frac{\mathsf{Q}_1}{2\mathsf{A}\varepsilon_0} - \frac{\mathsf{Q}_2}{2\mathsf{A}\varepsilon_0}, \, \mathsf{E} = \frac{\mathsf{Q}_1 - \mathsf{Q}_2}{2\mathsf{A}\varepsilon_0}$$

... Potential difference between the plates

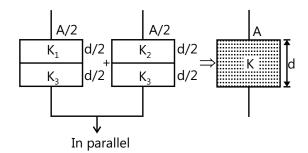
 \rightarrow

$$+Q_{1} | \xrightarrow{E} | +Q_{2} | \xrightarrow{E_{2}} | E_{2} \xrightarrow{E_{1}} |$$

$$V_{A} - V_{B} = Ed = \left(\frac{Q_{1} - Q_{2}}{2A\varepsilon_{0}}\right)d = \frac{Q_{1} - Q_{2}}{2\left(\frac{A\varepsilon_{0}}{d}\right)} = \frac{Q_{1} - Q_{2}}{2C}$$

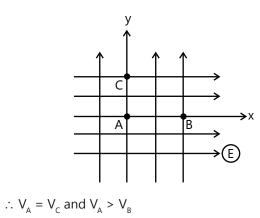
Sol 20: (D) Applying C=
$$\frac{\epsilon_0 A}{d - t_1 - t_2 + \frac{t_1}{K_1} + \frac{t_2}{K_2}}$$
, we have
 $\frac{\epsilon_0 (A/2)}{d - d/2 - d/2 + \frac{d/2}{K_1} + \frac{d/2}{K_3}}$
 $+ \frac{\epsilon_0 (A/2)}{d - d/2 - d/2 + \frac{d/2}{K_2} + \frac{d/2}{K_3}} = \frac{K\epsilon_0 A}{d}$

Solving this equation, we get



$$K = \frac{K_1 K_3}{K_1 + K_3} + \frac{K_2 K_3}{K_2 + K_3}$$

Sol 21: (B) Potential decreases in the direction of electric field. Dotted lines are equipotential lines.



Sol 22: (B)
$$\begin{array}{c} q & Q & q \\ \hline x = -a & x = 0 & x = +a \end{array}$$

Initial Position

$$\begin{array}{c} q & Q & q \\ x=-a & x=x & x=a \end{array}$$

Final position

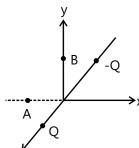
$$U_{i} = \frac{2KQq}{q} + \frac{K.q.q}{2a}$$

and $U_{f} = KQq \left[\frac{1}{a+x} + \frac{1}{a-x} \right] + \frac{K.q.q}{2a}$
Here, $K = \frac{1}{4\pi\epsilon_{0}}$
 $\Delta U = U_{f} - U_{t}$ or $|\Delta U| = \frac{2KQqx^{2}}{2}$

for x << a
$$\therefore \Delta U \propto x^2$$

Sol 23: (C)
$$\Delta U$$
 = decrease in potential energy
= $U_i - U_f$
= $\frac{1}{2}C(V_1^2 + V_2^2) - \frac{1}{2}(2C)\left(\frac{V_1 + V_2}{2}\right)^2$
= $\frac{1}{4}C(V_1 - V_2)^2$

Sol 24: (A) There will be an electric field between two cylinders (using Gauss theorem). This electric field will produce a potential difference,



Point charges is moved from A to B

$$V_{A} = V_{B} = 0 \therefore W = 0$$

Sol 26: (C) Distance BC= AB sin 60°=(2R) $\frac{\sqrt{3}}{2} = \sqrt{3}$ R

$$\therefore |Fe_{BC}| = \frac{1}{4\pi\epsilon_0} \frac{(q/3)(2q/3)}{(\sqrt{3}R)^2} = \frac{q^2}{54\pi\epsilon_0 R^2}$$

Sol 27: (A) After time t, thickeness of liquid will remain $\left(\frac{d}{3} - vt\right)$

Now, time constant as function of time:

$$\tau_{c} = CR = \frac{\varepsilon_{0}(1)R}{\left(d - \frac{d}{3} - vt\right) + \frac{d/3 - vt}{2}}$$
$$\left(ApplyingC = \frac{\varepsilon_{0}A}{d - t + \frac{t}{k}}\right) = \frac{6\varepsilon_{0}R}{5d + 3Vt}$$

Sol 28: (D) $q_1 = C_1 V = 2V = q$

This charge will remain constant after switch is shifted from position 1 to position 2.

$$U_{i} = \frac{1}{2} \frac{q^{2}}{C_{i}} = \frac{q^{2}}{2 \times 2} = \frac{q^{2}}{4}$$
$$U_{f} = \frac{1}{2} \frac{q^{2}}{C_{f}} = \frac{q^{2}}{2 \times 10} = \frac{q^{2}}{20}$$

:. Energy dissipated = $U_i - U_f = \frac{q^2}{5}$

This energy dissipated $\left(=\frac{q^2}{5}\right)$ is 80% of the initial stored energy $\left(=\frac{q^2}{4}\right)$

Sol 29: (A)
$$120C_1 = 200C_2$$

 $6C_1 = 10C_2$
 $3C_1 = 5C_2$
Sol 30: (C)
 0
 x
 dx
 dx

 $V = \int_{x=L}^{x=2L} \frac{k}{x} \left(\frac{Q}{L}\right) dx = \frac{Q \ln 2}{4 \pi \varepsilon_0 L}$

Sol 31: (C) By formula of electric field between the plates of a capacitor $E = \frac{\sigma}{K\epsilon_0}$ $\Rightarrow \sigma = E K\epsilon_0 = 3 \times 10^4 \times 2.2 \times 8.85 \times 10^{-12}$ $= 6.6 \times 8.85 \times 10^{-8}$ $= 5.841 \times 10^{-7}$ $\cong 6 \times 10^{-7}$ C / m² Sol 32: (A) $\vec{E} = 30x^2$ î $dV = -\int E.dx$

$$\int_{V_0}^{V_A} dV = -\int_0^2 30 x^2 dx$$
$$V_A - V_0 = -80 \text{ volt}$$

Sol 33: (B, C) The potential at the centre

$$=k\frac{Q}{\frac{4}{3}\pi R^{3}}\int_{0}^{R}\frac{4\pi r^{2} dr}{r}=\frac{3}{2}\frac{kQ}{R}=\frac{3}{2}V_{0}; k=\frac{1}{4\pi \varepsilon_{0}}$$

$$\therefore R_1 = 0$$

Potential at surface, $V_0 = \frac{kQ}{R}$

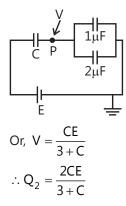
Potential at
$$R_2 = \frac{5V_0}{4} \Rightarrow R_2 = \frac{R}{\sqrt{2}}$$

Potential at R_3 , $\frac{kQ}{R_3} = \frac{3}{4} \frac{kQ}{R} \Longrightarrow R_3 = \frac{4R}{3}$

Similarly at
$$R_4$$
, $\frac{kQ}{R_4} = \frac{kQ}{4R} \Longrightarrow R_4 = 4R$

Sol 34: (A) Let the potential at P be V,

Then, C (E – V) = $1 \times V + 2 \times V$ (we take C in μ F)



Sol 35: (B) Charge on 9 μ F capacitor = 18 μ C Charge on 4 μ F capacitor = 24 μ C $\therefore Q = 24 + 18 = 42 \mu$ C $\therefore \frac{KQ}{r^2} = \frac{9 \times 10^9 \times 42 \times 10^{-6}}{(30)^2} = 420 \text{ N/C}$

So total charge =
$$(24 + 6)C_1 = 30C_1$$

Same charge would be there at capacitor b/w a and b
So , $\Delta V = \frac{30 C_1}{C_1} = 30V$
Sol 3: $E_{initial} = \frac{(20 \ \mu C)^2}{2 \times 2\mu F} + \frac{(50 \ \mu C)^2}{2 \times 5\mu F}$
= $100 \ \mu J + \frac{2500}{10} \ \mu J = 350 \ \mu J$
Now $\frac{q_1}{2} = \frac{q_2}{5} \Rightarrow q_1 = \frac{2}{7} \times 70 \ \mu C = 20 \ \mu C$

Now q on $C_2 = 8C_2 = 24C_2$

5μF

And thus , $q_2 = 50 \mu C$ $E_{initial}$ = same (thus there would be no heat produced)

1μF

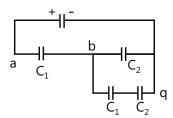
JEE Advanced/Boards

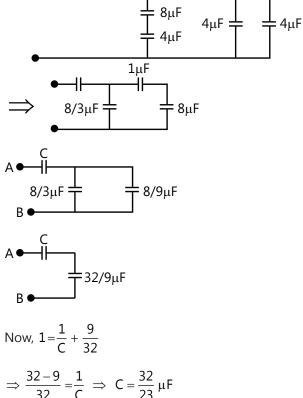
Exercise 1

Sol 1:
$$d_{eff} = \frac{6 \text{ mm}}{6} + \frac{4 \text{ mm}}{4} = 2 \text{ mm}$$

$$\therefore C = \epsilon_0 \frac{A}{d_{eff}}$$

$$= \frac{8.85 \times 10^{-12} \times 100 \times 10^{-4}}{2 \times 10^{-3}} = 44.25 \text{ pF}$$



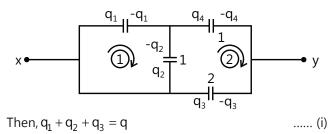
Now $q_{pq} = 2 \times C_2 = 6C_1$ So voltage difference across b and p = $6C_1 / C_1 = 6V$ 

Sol 5: $\Delta V = 10 V$

So, $Q = CV = 10 \times 1 \,\mu C$

(The ends of $C = 1\mu F$ are connected to the terminals of the battery)

Sol 6: Suppose a charge q is given to the system.



And $q_4 + q_3 = q$ (ii)

Also, applying kirchoffs law in loop (i)

$$\frac{-q_1}{1} + \frac{q_2}{1} = 0 \implies q_1 = q_2 \qquad ...(iii)$$

And
$$\frac{1}{2} - \frac{1}{2} - \frac{1}{1} = 0$$

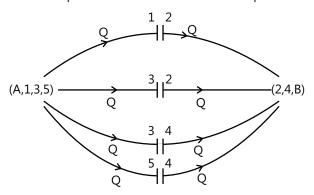
 $\Rightarrow q_3 = 2(q_2 + q_4)$
Now, $2q_1 + q_3 = q$ (form (i))
 $\Rightarrow q_2 = q_1 = \frac{(q - q_3)}{2}$
 $\Rightarrow q_3 = 2 \cdot \left[\frac{(q - q_3)}{2} + q - q_3 \right]$
 $\Rightarrow 4q_3 = q - q_3 + 2q - 2q_3$

$$\Rightarrow q_3 = 3q / 4$$

Now, $\Delta V = 3q / 4 \times \frac{1}{2} = \frac{3q}{8} V$

So Capacitance = $q / \Delta V = \frac{8}{3} \mu F$

Sol 7: The Circuit can be converted to all branches have the same capacitance and are connected in parallel.



$$4Q = (4C)V = \left(\frac{4\varepsilon_0 A}{d}\right)V \implies Q = \frac{\varepsilon_0 AV}{d}$$

So, the charge on plate 1 is $\frac{\epsilon_0 AV}{d}$ and that on plate 4 is $-\frac{2\epsilon_0 AV}{d}$

Sol 8: Capacitance (left side):
$$\frac{C_1 \cdot C_2}{C_1 + C_2}$$
$$= \frac{\frac{1 \times (A / 2) \cdot \varepsilon_0}{d}}{4 \cdot \frac{(A / 2) \cdot \varepsilon_0}{d}} = \frac{3A\varepsilon_0}{8d} = \frac{3A\varepsilon_0}{8d}$$

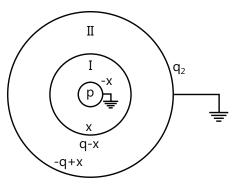
Capacitance: (right side)

$$= \frac{\frac{2 \times (A/2).\varepsilon_0}{d}}{\frac{4 \times (A/2).\varepsilon_0}{6}} = \frac{4}{6} \frac{A\varepsilon_0}{d} = \frac{2A\varepsilon_0}{3d}$$

So
$$C_{\text{total}} = \frac{3A\epsilon_0}{8d} + \frac{2A\epsilon_0}{3d}$$

$$C_{\text{total}} = \left(\frac{9+16}{24}\right) \frac{A\varepsilon_0}{d} = \frac{25}{24} \frac{A\varepsilon_0}{d}$$

Sol 9:



Now V at outer must = 0

$$\Rightarrow \frac{k.(-x)}{3.5r} + \frac{kq}{3.5r} + \frac{k[(-q+x)+q_2]}{3.5r} = 0$$

 \Rightarrow kq₂ = 0 \Rightarrow q₂ = 0

And now potential at inner cell = 0

$$\frac{k.(-q+x)}{3.5r} + \frac{k(q-x)}{2.5r} + \frac{k.x}{2.5r} - \frac{kx}{r} = 0$$
$$\Rightarrow \frac{k(-q+x)}{3.5r} + \frac{kq}{2.5r} - \frac{kx}{r} = 0$$

$$\frac{(x-q)}{3.5} + \frac{q}{2.5} - x = 0$$

$$\frac{2(x-q)}{7} + \frac{2q}{5} - x = 0$$

$$\Rightarrow 10(x-q) + 14q - 35x = 0$$

$$\Rightarrow 4q = 25x$$

$$\Rightarrow x = 4q/25$$
So in region (I), $E = \frac{kx}{r^2}$
Energy = $\int_{r}^{2.5r} \frac{1}{2}\varepsilon_0 \cdot E^2 \cdot (4\pi r^2) \cdot dr$

$$= \frac{1}{2} \times \varepsilon_0 \times 4\pi \cdot kx^2 \int_{r}^{2.5} \frac{1}{r^2} r^2 \cdot dr$$

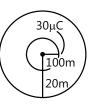
$$= \frac{kx^2}{2r} \left[1 - \frac{2}{5} \right] = \frac{3k}{10r} \cdot x^2 \text{ where } x = 4q/25$$
Similarly in region II
$$E = \frac{-kx}{2r} + \frac{k(q)}{2r} = \frac{k(-x+q)}{2r}$$

$$E = \frac{1}{r^2} + \frac{1}{r^2} = \frac{1}{r^2}$$
$$\Rightarrow Energy = \int_{2.5r}^{3.5r} \frac{1}{2} \varepsilon_0 E^2 (4\pi r^2) dr$$
$$= \frac{k(q-x)^2}{2r} \left[\frac{2}{5} - \frac{2}{7}\right] = \frac{2k(q-x)^2}{35r}$$

Sol 10:
$$i = 2/4 + 5 = 2/9$$

So ΔV for $4\mu F = iR = 5 \times \frac{2}{9} = \frac{10}{9} V$
And ΔV for $5\mu F = iR = 4 \times \frac{2}{9} = \frac{8}{9} v$
So Energy ratio $= \frac{1/2 \times 5 \times (8/9)^2}{1/2 \times 4 \times (10/9)^2}$
 $= \frac{5}{4} \times \frac{64}{100} = \frac{4}{5} = 0.8$

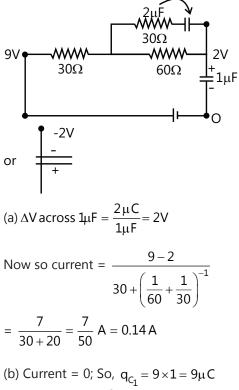
Sol 11: Now after connection all the charge will transfer to be outer shall. Now, the heat generated would be same as then energy of the region between the sphere and the shell (Electric field elsewhere is same)



So Energy =
$$\int_{10}^{20} \frac{1}{2} \varepsilon_0 \cdot E^2 \cdot (4\pi r^2) \cdot dr$$

= $\frac{\varepsilon_0}{2} \cdot 4\pi \cdot k^2 q^2 \frac{20}{10} \int \frac{dr}{r^2}$
= $\frac{kq^2}{2} \cdot \left[\frac{1}{0.1} - \frac{1}{0.2}\right] = \frac{5kq^2}{2}$
= $\frac{5 \times 9 \times 10^9 \times (20)^2 \times 10^{-12}}{2}$
= 9 J
Sol 12: $i = \frac{E}{R_1 + R_3}$
So, $\Delta v = R_3 \cdot i = \frac{R_3 E}{R_1 + R_3}$

Now,
$$Q = C \times (\Delta V) = \frac{CR_3E}{R_1 + R_3}$$



And
$$q_{C_2} = (\Delta V) \times C^2 = 0 \times C_2 = 0$$

So, $E = \frac{kq}{r^2}$

Sol 14: \Rightarrow E-iR₁-i₁R₃- $\frac{q}{c}=0$ (i) And $E - iR_1 - i_2R_2 = 0$ (ii) $i = i_1 + i_2$ (iii) So $i_2 R_2 - i_1 R_3 - \frac{q}{c} = 0$ $(i - i_1) R_2 - i_1 R_3 - \frac{q}{c} = 0$ $iR_2 - i_1(R_2 + R_3) - \frac{q}{c} = 0$ $\Rightarrow iR_1 \cdot \left(\frac{R_2}{R_1}\right) = i_1(R_2 + R_3) + \frac{q}{C}$ $\Rightarrow \left(\mathsf{E} - \mathsf{i}_1\mathsf{R}_3 - \frac{\mathsf{q}}{\mathsf{C}}\right) \cdot \frac{\mathsf{R}_2}{\mathsf{R}_2} = \mathsf{i}_1(\mathsf{R}_2 + \mathsf{R}_3) + \frac{\mathsf{q}}{\mathsf{C}}$ $\Rightarrow E \cdot \frac{R_2}{R_2} = i_1 \left(R_2 + R_3 + \frac{R_3 \cdot R_2}{R_1} \right) + \frac{q}{C} \left[1 + \frac{R}{R_1} \right]$ $\Rightarrow E.R_{2} = i_{1}(R_{1}.R_{2} + R_{1}.R_{3} + R_{3}.R_{2}) + \frac{q}{c}.[R_{1}.R_{2}]$ $\Rightarrow \frac{2}{\sum R_1 R_2} = \frac{dq}{dt} + \frac{q(R_1 + R_2)}{c(\sum R_1 R_2)}$ $\Rightarrow \left(\frac{\text{E.R}_2}{\sum \text{R}_1.\text{R}_2}\right) \int_0^t e^{\frac{\text{t.}(\text{R}_1+\text{R}_2)}{\text{c}(\sum \text{R}_1.\text{R}_2)}\text{dt}} = \int_{0,0}^{q,t} d\left[q_{\star}e^{\frac{\text{t.}(\text{R}_1+\text{R}_2)}{\text{c.}(\sum \text{R}_1+\text{R}_2)}}\right]$ $\Rightarrow \frac{\mathsf{E}.\mathsf{R}_{2}}{\Sigma(\mathsf{R}_{1}.\mathsf{R}_{2})} \frac{\mathsf{C}(\Sigma\mathsf{R}_{1}.\mathsf{R}_{2})}{(\mathsf{R}_{1}+\mathsf{R}_{2})} \cdot \left[\mathsf{e}^{\frac{\mathsf{t}(\mathsf{R}_{1}+\mathsf{R}_{2})}{\mathsf{C}(\Sigma\mathsf{R}_{1}.\mathsf{R}_{2})}} - 1\right] = \mathsf{q}.\mathsf{e}^{\frac{\mathsf{t}(\mathsf{R}_{1}+\mathsf{R}_{2})}{\mathsf{C}(\Sigma\mathsf{R}_{1}.\mathsf{R}_{2})}}$ $\Rightarrow \frac{\text{ECR}_2}{(R_1 + R_2)} \left[1 - e \frac{-t(R_1 + R_2)}{C(\Sigma R_1 R_2)} \right] = q$ $q = \left(\frac{10 \times 0.01 \times 300}{300 + 300}\right) \cdot \left| 1 - e^{\frac{-t(300 + 300) \times 2}{0.01 \times 10^{6} [300 \times 300 + 300 \times 50 + 300 \times 50 \times 18^{6}]}} \right|$ $=\frac{0.1}{2} \cdot \left[1-e^{-t/2}\right] = 0.05 \left[1-e^{-t/2}\right] \mu C$

(b) Energy =
$$\frac{Q^2}{2C} = \frac{(0.05)^2 \cdot [1 - e^{-t/2}]^2 \times (\mu c)^2}{2 \times 0.01(\mu F)}$$

= $\frac{5 \times 0.05}{2} [1 - e^{-10}]^2$
= 0.125 µJ
Sol 15:
(a) $q_2 = \frac{q_2}{q_1} = \frac{q_1}{q_1}$
= $i = \frac{dq_1}{dt} = \frac{dq_2}{dt}$
And $\frac{q_1}{C} - iRC = \frac{q_2}{C}$
and $q_1 + q_2 = CV$
 $\Rightarrow q_1 - iRC = CV - q_1$
 $\Rightarrow 2q_1 + \frac{dq_1}{dt} \cdot (RC) = CV$
 $\Rightarrow \frac{2q_1}{C} + \frac{dq_1}{dt} = V / R$
 $\Rightarrow \int_{q_0,0}^{q_1} d(q_1 \cdot e^{2t/RC}) = \int_0^t \frac{V}{R} \cdot e^{2t/RC} \cdot dt$
 $\Rightarrow q_1 \cdot e^{2t/RC} - q_0 = \frac{V}{R} \cdot \frac{(RC)}{2} \cdot [e^{2t/RC} - 1]$
 $\Rightarrow q_1 = q_0 \cdot e^{-2t/RC} + \frac{VC}{2} \cdot [1 - e^{-2t/RC}]$
So, $\frac{dq_1}{dt} = q_0 \cdot (\frac{-2}{RC}) \cdot e^{-2t/RC} + \frac{VC}{2} (\frac{2}{RC}) \cdot e^{-2t/RC}$
 $= \frac{-V}{R} \times 2 \cdot e^{-2t/RC} + \frac{V}{R} \cdot e^{-2t/RC}$
(b) Heat generated = $E_{initial} - E_{final}$
 $= \frac{1}{2} \times CV_0^2 - [\frac{1}{2} \times (\frac{CV}{2})^2 \times \frac{1}{C} \times 2]$

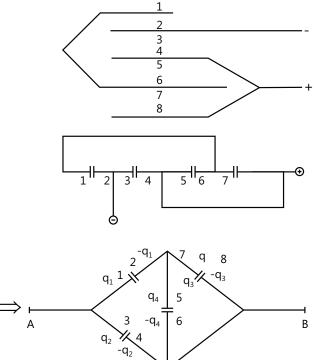
$$= \frac{CV_0^2}{2} - \frac{CV_0^2}{4} = \frac{CV_0^2}{4}$$

Sol 16:
$$E = \frac{3q}{2A\epsilon_0} - \frac{q}{2A\epsilon_0} = \frac{q}{A\epsilon_0}$$

 $\Rightarrow \text{Voltage} = E \times d = \frac{qd}{A\epsilon_0} = \frac{q}{C}$
So energy initial $= \frac{1}{2} \times C \times V^2$
 $= \frac{1}{2} \times C \times \left(\frac{q}{C}\right)^2 = \frac{q^2}{2C} = \frac{q^2d}{2A\epsilon_0}$
and $E_{\text{final}} = 0$ (both have $q = 2q$)
So $E_{\text{initial}} = E_{\text{final}}$ + heat

$$\Rightarrow \frac{q^2 d}{2A\epsilon_0} = Heat$$

Sol 17:



Let q charge be given to the system.

$$q_1 + q_2 = q$$
 (i

 $q_3 + q_4 + q_2 = q$ (ii)

$$\frac{q_3}{1} - \frac{q_4}{1} = 0 \Rightarrow q_3 = q_4$$
 (iii)

 $q_1 - q_2 + q_4 = 0$ $q_1 + q_4 = q_2$ (iv)

So on solving,

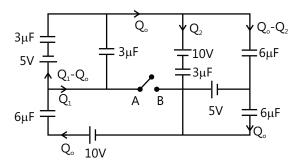
$$\Rightarrow$$
 q₂=3q/5

So $\Delta V = 3q / 5C$ (C = capacitance of each capacitors)

= q/3q/5c= $\frac{5C}{3} = \frac{5A\epsilon_0}{3d}$ (ii) Charge on plate $3 \Rightarrow q_4$ $2q_4 + q_2 = q$ (from 2 and 3) $\Rightarrow q_4 = -q/10$ Now, we have $\Delta v = 3q/5C$, So $v_0 = 3q/5C$ $\Rightarrow \frac{5V_0C}{3} = q$ $\Rightarrow \frac{5V_0}{3} \cdot \frac{A\epsilon_0}{d} = q$ So, $q_4 = \frac{A\epsilon_0 \cdot V_0}{6d} \Rightarrow$ on plate 3 And charge on plate $5 = q_1$ Now, $q_1 + q_2 = q$ $\Rightarrow q_1 = 2q/5$ $= \frac{2}{5} \times \frac{5V_0 \cdot A\epsilon_0}{3d} = \frac{2}{3} \frac{V_0 A\epsilon_0}{d}$

So capacitance = Q / ΔV

Sol 18:



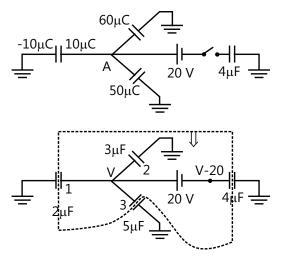
Set up potential drop equations to get the values of $\rm Q_{_{0'}}$ $\rm Q_{_1}$ and $\rm Q_{_2}$

Now, close the switch 'AB' and draw a similar charge distribution diagram.

This will give you the new charges across all the plates.

By using appropriate arithmetic, you can easily get to the charge flown across the switch AB.

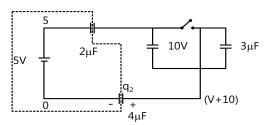
Sol 19:



Charge is conserved

 $(V-0) \times 3 + (V-0) \times 2 + (V-0) \times 5 + (V-20) \times 4$ = 10 + 60 + 50 $\Rightarrow 14V - 80 = 120$ $\Rightarrow V_{A} = 200 / 14 = 100 / 7$ (b) $q_{1}=2 \times (100 / 7)$, $q_{2} = 3 \times V = \frac{300}{7} \mu C$ And $q_{3} = \frac{5 \times 100}{7} = \frac{300}{7} \mu C$ = $q_{4} = (V_{A} - 20) \times 4 \mu F = (\frac{100}{7} - 20) \times 4 \mu F$ = $\frac{-160}{7} \mu F = 22.88$

Sol 20:



Now, $q_1 + q_2 = 0$

$$\Rightarrow$$
 (V - 5)2 + (V + 10)4 = 0 (Cons. of charge)

- $\Rightarrow 6V + 30 = 0$
- \Rightarrow V = -5

So
$$q_1 = (-5 - 5)2 = -20 \mu C$$

And
$$q_2 = (-5+10) \times 4 = 20 \,\mu\text{C}$$

After the switch is closed, the above $eq^n s$ would s + 111 be valid , and hence q_1 and q_2 would be same.

Only change would be there In q_3

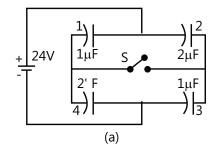
$$q_3 = CV = 3\mu F \times 10 = 30\mu F$$

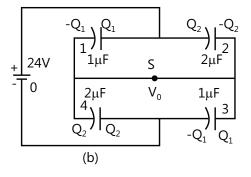
So energy or heat generated = work done by battery energy stored in capacitor

=
$$10 \times 30 - \frac{1}{2} \times 3 \times (10)^2 = 300 - 150 = 150 \ \mu \text{J}$$

Sol 21: $C_{eq} = \left(1 + \frac{1}{2}\right)^{-1} + \left(\frac{1}{2} + 1\right)^{-1}$
= $\frac{2}{3} + \frac{2}{3} = \frac{4}{3} \ \mu \text{F}$
So , $Q = C_{eq} \cdot \text{V} = \frac{4}{3} \times 24 = 32 \ \mu \text{C}$

This will be divided equally, as the capacitor are equal \Rightarrow Q =16 μ C





When the switch S is closed as shown in the figure (b), then the charges stored across positive plates capacitors 1 and be Q_1 and Q_2 . The same charges will be distributed across negative plates of capacitor 3 and 4. Let the potential at the negative terminal is zero, then the charges across capacirots 1, 2, 3 and 4 will be

 $Q_1 = (24 - V_0) \times 1\mu F \qquad \dots (i)$

$$Q_2 = (24 - V_o) \times 2\mu F \qquad \dots (ii)$$

$$Q_3 = V_0 \times 1\mu F \qquad \dots (iii)$$

$$Q_4 = V_0 \times 2\mu F \qquad \dots (iv)$$

Thus from (i) and (iii) $V_{_0}$ = 12V and thus the charges be Q_1 = Q_3 =12 μF and Q_2 = Q_4 = 24 μF

Thus when switch is zero, 12μ F charge is passed through the switch.

Sol 22: Before opening the switch potential difference across both the capacitors is V, as they are in parallel. Hence, energy stored in them is,

$$U_{A} = U_{B} = \frac{1}{2}CV^{2}$$

$$\therefore \quad U_{Total} = CV^{2} = U_{i} \qquad ...(i)$$

After opening the switch, potential difference across it is V and its capacity is 3C

:.
$$U_A = \frac{1}{2}(3C)V^2 = \frac{3}{2}CV^2$$

In case of capacitor B, charge stored in it is q = CV and its capacity is also 3C.

Therefore,
$$U_{B} = \frac{q^{2}}{2(3C)} = \frac{CV^{2}}{6}$$

$$\therefore \quad U_{Total} = \frac{3CV^{2}}{2} + \frac{CV^{2}}{6}$$

$$= \frac{10}{6}CV^{2} = \frac{5CV^{2}}{3}U_{f} \qquad ...(ii)$$
From eqs. (i) and (ii) $\frac{U_{i}}{U_{f}} = \frac{3}{5}$
Sol 23: $C = \frac{A\varepsilon_{0}}{d}$, So $Q = CV = \frac{A\varepsilon_{0}}{d} \times V_{0} = \frac{AV_{0}}{d} \cdot \varepsilon_{0}$
So $Q = \frac{AV_{0}\varepsilon_{0}}{d}$, E. ..., $= \frac{Q^{2}}{2} = \frac{Q_{2}}{2}$

$$E_{\text{final}} = \frac{Q_2}{2C_f} = \frac{\left(\frac{A\varepsilon_0}{d}\right)^2 V_0^2}{2k} = \frac{1}{2} \cdot \frac{A\varepsilon_0}{d} \times V_0^2$$

$$E_{\text{initial}} = \frac{\varepsilon_0 A V_0^2}{2d}$$

$$E_{\text{final}} = \frac{Q_2}{2C_f} = \frac{\left(\frac{A\varepsilon_0}{d}\right)^2 V_0^2}{2k \cdot \left(\frac{A\varepsilon_0}{d}\right)} = \frac{V_0^2}{2k} \cdot \frac{A\varepsilon_0}{d}$$

 E_{final} + work done = $E_{initial}$

$$\Rightarrow \frac{A\epsilon_0 V_0^2}{2d} \cdot \frac{1}{k} + W = \frac{A\epsilon_0 V_0^2}{2d} \Rightarrow W = \frac{A\epsilon_0 V_0^2}{2d} \left[1 - \frac{1}{k} \right]$$

Sol 24:

$$V_{F}$$
 q_{1}
 Q_{2}
 q_{2}
 αVC
 q_{2}

So, Q = 156 × C
Thus, q₁ + q₂ = 156C

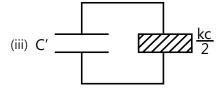
$$\Rightarrow$$
 CV + α CV² = 156C
 \Rightarrow V² + V - 156 = 0
 \Rightarrow (V - 12)(V + 13) = 0
 \Rightarrow V = 12 Volts

Sol 25: (i)
$$C = \frac{\varepsilon_0 (A/2)}{d} + \frac{K \varepsilon_0 (A/2)}{d}$$

= $\frac{8.85 \times 10^{-12}}{8.85 \times 10^{-4}} [0.02 + 0.18]$
= $0.2 \times 10^{-8} \text{ F}$
Energy = $\frac{1}{2} \text{CV}^2 = 1.2 \times 10^{-5} \text{ J}$
(ii) Q = CV

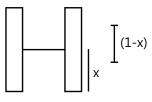
Find the new capacitance, C' = $\frac{\varepsilon_0 A}{d}$

Work done =
$$\frac{Q^2}{2C'} - \frac{Q^2}{2C} = 4.84 \times 10^{-5} \text{ J}$$



Find the new charge distribution, and proceed as (i) & (ii) Energy of system = 1.1×10^{-5} J

Sol 26:

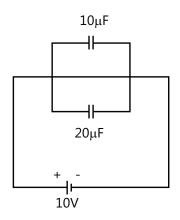


Now area of air = $1 \times (1-x)m^2 = (1-x)m^2$ = area of air = xm^2 So both are in parallel connection.

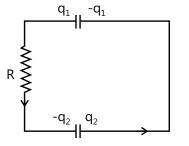
Capacitance =
$$\frac{(1-x).\epsilon_0}{d} + \frac{11 \times x.\epsilon_0}{d}$$

= $\frac{\epsilon_0}{d} + \frac{10x\epsilon_0}{d} = \frac{\epsilon_0}{d} [1+10x]$
Now, Q = CV
 $\Rightarrow \frac{dC}{dt} = i = \frac{dC}{dt}.(V)$
= $V.\frac{\epsilon_0}{d}\frac{d}{dt} [1+10x]$
= $\frac{V.\epsilon_0}{d} \times 10 \times \frac{dx}{dt} = \frac{500 \times 10 \times 0.001}{0.01 \times 8.85 \times 10^{-12}}$
= $5 \times 8.85 \times 10^{-10} = 4.425 \times 10^{-5}$ Amp.

Sol 27: We have $C_{eq} = 30 \,\mu\text{F}$



So, $q = 30 \times 10 = 300 \,\mu\text{C}$ Thus, q on $20 \,\mu\text{F} = 200 \,\mu\text{C}$ And q on $20 \,\mu\text{F} = 200 \,\mu\text{C}$ Now,



Now, $q_2 - q_1 = 200 - 100 = 100 \,\mu C \, Now$,

$$i = \frac{-dq_1}{dt} = -\frac{dq_2}{dt}$$

And, $\frac{q_1}{10} + \frac{q_2}{20} - iR = 0$

$$\Rightarrow \frac{q_{1}}{C} + \frac{q_{2}}{2C} - iR = 0$$

$$\Rightarrow \frac{q_{1}}{C} + \left(\frac{q_{1} + 100}{2C}\right) + \frac{qd_{1}}{dt} \cdot R = 0$$

$$\Rightarrow \frac{3q_{1}}{2CR} + \frac{50}{RC} + \frac{dq_{1}}{dt} \cdot R = 0$$

$$\Rightarrow \frac{dq_{1}}{dt} + \frac{3}{2CR} \cdot q_{1} = -50 / RC$$

$$\Rightarrow \int_{100,0}^{q_{1}t} d(q_{1} \cdot e^{t/20R/3}) = \frac{-50}{RC} \cdot \int_{q}^{d} e^{t/2RC/3} \cdot dt$$

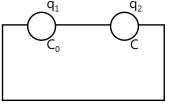
$$\Rightarrow \frac{-50}{RC} \times \frac{2CR}{3} \cdot \left[e^{t/2CR/3-1}\right]$$

$$\Rightarrow q_{1}e^{t/2CR/3} - 100 = \frac{-100}{3} \left[e^{(t/2RC/3)} - 1\right]$$

$$\Rightarrow q_{2} = q_{1} + 100 \mu C = \frac{200}{3} + \frac{400}{3} \cdot e^{-t/2RC/3}$$

$$Charge \frac{200}{3}$$

$$Charge Q = C_{0}V_{0}$$
Now,
$$q_{1} = \frac{q_{1}}{2} + \frac{q_{2}}{2} + \frac{q$$



So, $\frac{q_1}{C_0} - \frac{q_2}{C} = 0 \Rightarrow \frac{q_1}{C_0} = \frac{q_2}{C} \Rightarrow \frac{q_1}{q_2} = \frac{C_0}{C}$ So, $q_1 = \frac{C_0}{(C_0 + C)}(q_1 + q_2)$ (After first) $= \frac{C_0^2 V_0}{(C_0 + C)}$ (After First)

After 2nd

$$q_{1} = \frac{C_{0}}{(C_{0} + C)} \cdot \frac{C_{0}}{(C_{0} + C)} \cdot (C_{0}V_{0})$$

$$s = \left(\frac{C_{0}}{C_{0} + C}\right)^{2} \cdot C_{0}V_{0}$$
Now after $n \Rightarrow \left(\frac{C_{0}}{C_{0} + C}\right) \cdot C_{0}V_{0} = q_{1}$
So voltage $\frac{q_{1}}{C_{0}} = V_{0}\left(\frac{C_{0}}{C_{0} + C}\right)^{n} = 35$

$$\Rightarrow \left(\frac{C_{0}}{C_{0} + C}\right)^{n} = 0.35$$

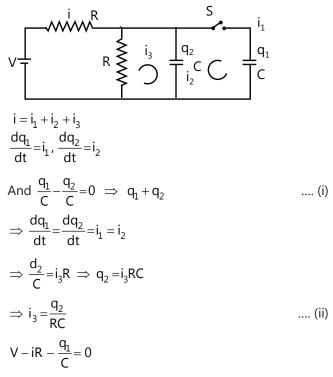
$$\Rightarrow \left(\frac{0.2}{0.2 + 0.01075}\right)^{n} = 0.35$$

$$\Rightarrow (0.094899)^{n} = 0.35$$

$$\Rightarrow n = \frac{\ln(0.35)}{\ln(0.94899)}$$

$$\Rightarrow n = 20$$

Sol 29:



(Kirchoff's Law in bigger loop)

$$\Rightarrow \frac{V}{R} = i + \frac{q_1}{RC} = i_1 + i_2 + i_3 + \frac{q_1}{RC}$$

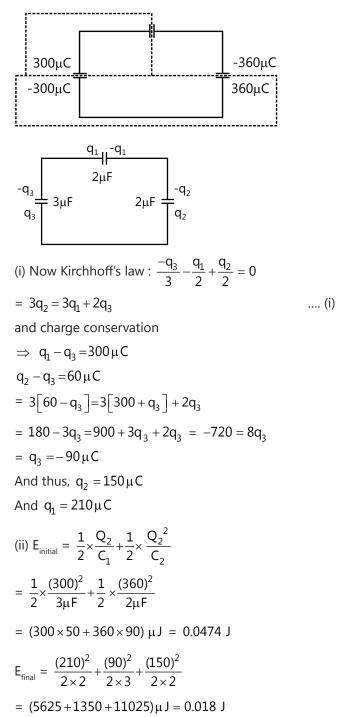
$$\Rightarrow \frac{V}{2R} = \frac{2dq_1}{dt} + \frac{2q_1}{C} \text{ (from i and ii)}$$

$$\Rightarrow \frac{V}{2R} \stackrel{t}{}_0 \int e^{t/RC} = {}^{q_{L_1}} \stackrel{t}{}_{0,0} \int d.(q_1.e^{t/RC})$$

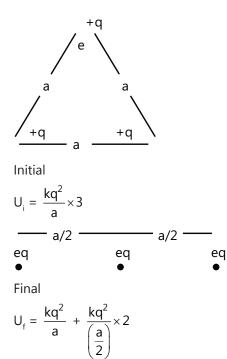
$$\Rightarrow \frac{VC}{2} \cdot \left[e.^{t/RC} - 1 \right] = q_1.e^{t/RC}$$

$$\Rightarrow q_1 = \frac{VC}{2} \left[1 - e^{-t/RC} \right]$$

Sol 30:







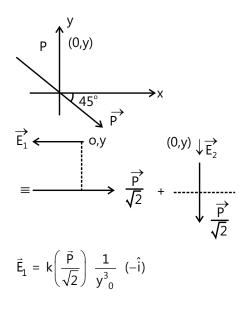
Work done = $U_f - U_i$

$$= \frac{5kq^2}{a} - \frac{3kq^2}{a} = \frac{2kq^2}{a}$$

Work done = Power × Time

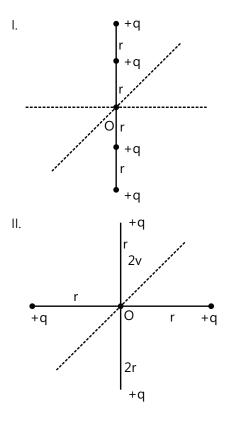
$$\Rightarrow t = \frac{2kq^2}{ap}$$
$$= \frac{2 \times 9 \times 10^9 \times 10^{-2}}{1 \times 10^3} = 18 \times 10^4 \text{ sec}$$





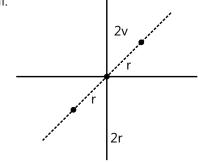
$$\vec{E}_2 + 2k\left(\frac{\vec{P}}{\sqrt{2}}\right)\left(\frac{1}{y^3}\right)(-\hat{j})$$
$$\vec{E} = \vec{E}_1 + \vec{E}_2 = \frac{k\vec{P}}{\sqrt{2}y^3}(-\hat{i}-2\hat{j})$$

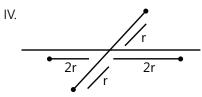
Sol 33:



$$U_{I} = \frac{kq^{2}}{r} \times 2 + \frac{kq^{2}}{2r} + \frac{kq^{2}}{3r} \times 2 + \frac{kq^{2}}{4r}$$
$$U_{II} = \frac{kq^{2}}{4r} + \frac{kq^{2}}{2r} + \frac{kq^{2}}{\sqrt{5}r} \times 4$$
$$W_{first step} = U_{II} - U_{I} = \frac{kq^{2}}{r} \left[\frac{8}{3} - \frac{4}{\sqrt{5}}\right]$$

III.

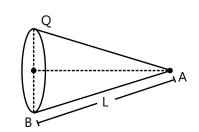




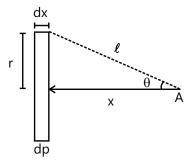
$$\begin{split} & U_{_{III}} = U_{_{II}} \ \therefore \ w_{_{secondstep}} = 0 \\ & \Longrightarrow w_{_{third}} = U_{_{IV}} - U_{_{III}} - U_{_{II}} - U_{_{I}} - W_{_{first step}} \end{split}$$

Sol 34:

: Total work done $= w_{first} + w_{second} + w_{third} = 0$



 σ = surface charge density = $\frac{Q}{\pi RL}$ take an elemental part



The potential due to this part at A is

$$dV = \frac{kdq}{\sqrt{R^2 + x^2}} = \frac{kdq}{\ell}$$

$$\Rightarrow dV = \frac{k}{\ell} \cdot \sigma \cdot 2\pi r \, d\ell$$

$$\Rightarrow dV = k\sigma \cdot 2\pi \sin \theta \, d\ell$$

$$\Rightarrow V = \int_0^V dV = k\sigma 2\pi \sin \theta \int^L d\ell$$

$$= \frac{1}{4\pi\epsilon_0} \frac{Q}{\pi RL} 2\pi \frac{R}{L} L$$

$$\Rightarrow V = \frac{Q}{2n\epsilon_0 L}$$

Energy required to bring the charge from infinity to open = ${\rm U_f}-{\rm U_i}$

Initial electric potential = V

$$= \int dv = \int_{0}^{Q} \frac{kdq}{(H^{2} + r^{2})^{1/2}}$$

$$\Rightarrow V = \int_{0}^{a} \frac{k\sigma 2\pi r, dr}{(H^{2} + r^{2})^{1/2}} \left(\text{where } \sigma = \frac{q}{\pi a^{2}} \right)$$

$$\Rightarrow V = \pi\sigma k \left[\frac{(H^{2} + r^{2})^{1/2}}{1/2} \right]_{0}^{a}$$

$$\Rightarrow V = 2\pi\sigma k \left((H^{2} + a^{2})^{1/2} - H \right) = 2$$
Final electric potential V_f = $2\pi\sigma k$ (a)
[substitute H = 0]
By equation conservation,
mg H + $2\pi\sigma k \left((H^{2} + a^{2})^{1/2} - H \right) q = (2\pi\sigma ka)q$

$$\Rightarrow gH + \sigma \left(\frac{q}{2\epsilon_{0}m} \right) \left((H^{2} + a^{2})^{1/2} - H \right) = (\sigma \cdot a) \left(\frac{q}{m2\epsilon_{0}} \right)$$

$$\Rightarrow H + 2 (H^{2} + a^{2})^{1/2} - H) = 2s$$

$$\Rightarrow \left(a + \frac{H}{2} \right)^{2} = H^{2} + a^{2} \Rightarrow 3\frac{H^{2}}{4} = aH$$

$$\Rightarrow H = \frac{4a}{3}$$

$$U = mg \left(2\sqrt{H^{2} + a^{2}} - H \right)$$

$$\frac{dU}{dH} = 0 \Rightarrow \frac{2H}{\sqrt{H^{2} + a^{2}}} - 1 = 0$$

$$\Rightarrow H = \frac{a}{\sqrt{3}} \text{ (equilibrium)}$$

$$U$$

 $H = \frac{a}{\sqrt{3}}$

$$= \frac{qQ}{2\pi\varepsilon_0 L}$$

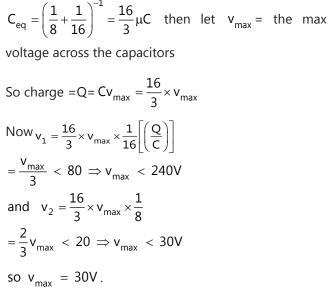
Sol 1: (A) V_{max} 16/3

Exercise 2

Single Correct Choice Type

 \Rightarrow 4.5CV² = Heat generated ratio = 4.5CV² / 2CV² = 2.25

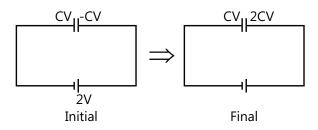
Sol 4: (B)



Thus $Q = \frac{16 \times 30}{3} = 160 \mu C$

Sol 2: (B) $C_{eq} = 2C$ where C= capacitance of each plate. So energy $= \frac{1}{2} \times C_{eq} \times V^2$ $= CV^2 = \frac{(0.1)(8.85 \times 10^{-12})}{0.885 \times 10^{-3}} \times 10^2 = 10^{-1} \text{ µJ}$

Sol 3: (B)

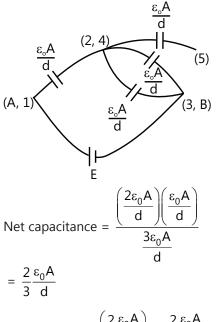


Now, initial energy + work done by battery

= Final energy + heat generated

$$\therefore \frac{1}{2} \times C \times V^{2} + 2V.(3CV)$$

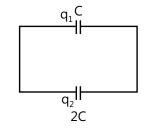
= $\frac{1}{2} \times C \times (2V)^{2}$ + Heat generated
$$\Rightarrow \frac{1}{2} CV^{2} + 6CV^{2} = 2CV^{2}$$
 + Heat generated



Charge flown = $\left(\frac{2}{3}\frac{\varepsilon_0 A}{d}\right)E = \frac{2}{3}\frac{\varepsilon_0 A}{d}E$

Sol 5: (A) Force between plates = mg And $\frac{\sigma}{2\epsilon_0} \times \sigma A = \frac{\sigma^2 A}{2\epsilon_0} = mg \Rightarrow \frac{Q^2}{2A\epsilon_0} = mg$ $\Rightarrow \sqrt{2mgA\epsilon_0} = Q$

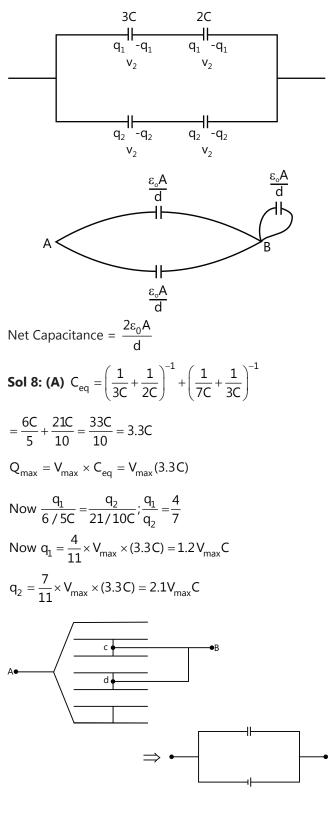
Sol 6: (B) Now across point c and $\Delta V = 0$



 $\Rightarrow \text{ The capacitance is 0 for that}$ $\Rightarrow C - C \pm C - 2\Delta_{\mathcal{E}} / d$

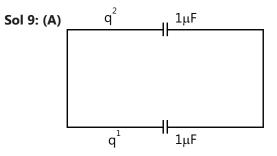
$$\Rightarrow C_{eq} = C_1 + C_2 = 2A\varepsilon_0 / c$$

Sol 7: (B)



$$V_{1} = \frac{1.2 \text{ } V_{\text{max}}.\text{C}}{3\text{C}} = 0.4 \text{ } V_{\text{max}} < 1 \text{ } \text{KV} \Rightarrow \text{ } V_{\text{max}} < 2.5 \text{ } \text{KV}$$
$$V_{1}' = \frac{1.2 \text{ } V_{\text{max}}.\text{C}}{2\text{C}} = 0.6 \text{ } V_{\text{max}} < 2 \text{ } \text{KV} \Rightarrow \text{ } V_{\text{max}} < \frac{10}{3} \text{ } \text{KV}$$

$$V_{2} = \frac{2.1 V_{max}.C}{7C} = 0.3 V_{max} < 1 \text{ KV} \Rightarrow V_{max} < \frac{10}{3} \text{ KV}$$
$$V_{2}' = \frac{2.1 V_{max}.C}{3C} = 0.7 V_{max} < 2 \text{ KV} \Rightarrow V_{max} < \frac{20}{7} \text{ KV}$$
$$= 2.5 \text{ KV}$$



Let there be a charge Q on body 1.

So
$$\frac{q_1}{1} = \frac{q_2}{2} \Longrightarrow \frac{q_1}{q_2} = \frac{1}{2}$$

and $q_1 + q_2 = Q \Rightarrow q_1 = Q / 3$ where q = initial charge $\Rightarrow q = Q / 3^n$

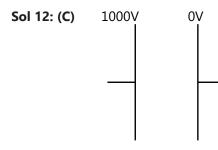
Sol 10: (D) Total charge now= E.C / 2 = $\frac{\text{EC}}{2}$ Now after dielectric is inserted,

$$C_{eff} = \frac{kC.C}{(kC+C)} = \frac{kC}{(k+1)} \text{ so } Q_{net} = \frac{kCE}{(k+1)}$$

so Q flowed = $\frac{KCE}{k+1} - \frac{CE}{2} = \frac{(K-1)CE}{2(k+1)}$ from B to A

as capacitance increases.

Sol 11: (B) Voltage would be highest at x = 0. And $E = \text{constant} \Rightarrow V \propto x$ so it would decrease linearly, from x = 0 to x-d, will remain constant from x = d to x = 2d.



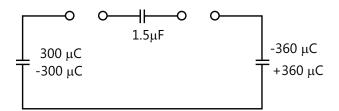
 $\Delta V = E \times \Delta d = 200 \times 5 = 1000 V.$

Now the electric field would be same so

 $\Delta V = E \times \Delta d = 200 \times 3 = 600 V.$

Sol 13: (**B**) $Q_1 = 1500\mu$ C and $Q_2 = 100\mu$ C $q_1 + q_2 = 1600\mu$ C and $\frac{q_1}{1} = \frac{q_2}{1} \Rightarrow q_1 = q_2 = 800\mu$ C $\Delta V = q / c = 800\mu$ C / 1μ C = 800V **Sol 14:** (**C**) $Q_1 = Q_2 = C_{eq}$. $E = \frac{E.kC}{(k+1)}$ and $Q_1' = Q_2' = C_{eq}$. $E = \frac{EC}{2}$; $\frac{Q_2'}{Q_2} = \frac{k+1}{2k}$

Sol 15: (B) From the symmetry, we can say that the capacitance would be same.



Sol 16: (A)
$$q = q_0 e^{-t/\tau}$$
 where $\tau = (2 + r)0.5\mu F$

$$\Rightarrow \frac{dq}{dt} = \frac{q_0}{z} e^{-t/\tau}$$

$$e^{-t/\tau} = 1/2 \Rightarrow \ln 2 = t/\tau \Rightarrow \frac{\ln 2 \times \mu s}{z} = \ln 2$$

$$\Rightarrow \tau = 1\mu s = (2 + r) \times 1/2 \Rightarrow r = 0$$
1.5 μF

$$q_3 - q_3$$

$$= -q_1 2\mu F$$

$$q_1 2\mu F$$

$$q_2 3\mu F$$

Sol 17: (D)
$$R_{eq} \times C = \frac{1}{2} \times 100 \mu F \times 10^{3}$$

= $0.5 \times 10^{5} \times 10^{-6} = 0.05 \text{ sec}$

Sol 18: (D) As at t = 0 the capacitor is assumed as a wire.

Sol 19: (B)
$$q = q_0 \cdot e^{-t/RC} \Rightarrow \frac{dq}{dt} = \frac{q_0}{RC} \cdot re^{-t/RC} = i$$

 $\Rightarrow i = \frac{q_0}{2 \times 10^{-6} \times 10} \cdot e^{-t/RC}$ Now $\int i^2 R \cdot dt = 3.6 \times 10^{-3}$

$$\Rightarrow \frac{q_0^{2}}{(RC)^{2}} \times R \times \frac{RC}{2} \times 1 = 3.6 \times 10^{-3} \times 2$$

$$\Rightarrow q_0^{2} = 7.2 \times 10^{-3} \times 2 \times 10^{-6}$$

$$= 14.4 \times 10^{-9} = 144 \times 10^{-10}$$

$$\Rightarrow q_0 = 12 \times 10^{-5}$$

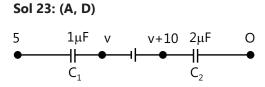
Sol 20: (C) $q = q_0 \cdot e^{-t/\tau} \Rightarrow \frac{dq}{dt} = q_0 \cdot \left(-\frac{1}{\tau}\right) \cdot e^{-t/\tau};$
 $i = -\frac{q_0}{\tau} \cdot e^{-t/\tau}$
 $\tau = RC = (r+2)0.5 \times 10^{-6} \text{ sec}$
and thus $\frac{1}{2} \times i_{|t=0} = i_{|t=|n.4\mu s.}$
 $\tau = 2\mu s = (r+2) \times \frac{1}{2} \times 10^{-6} \Rightarrow r = 2\Omega$
 $\Rightarrow \frac{1}{2} \times \left(-\frac{q_0}{\tau}\right) = \left(-\frac{q_0}{\tau}\right) \cdot e^{-t/\tau} = e^{t/\tau} = 2$
 $\Rightarrow \ln 2 \Rightarrow \ln 4/\tau$

Multiple Correct Choice Type

Sol 21: (A, B, C) Now from charge conservation

$$q_1 + q_2 = 60\mu C$$
 ... (i); $q_3 - q_1 = 300\mu C$... (ii)
 $\Rightarrow q_2 + q_3 = 360\mu C$
 $\frac{q_1}{2} + \frac{q_3}{1.5} - \frac{q_2}{3} = 0$; $3q_1 + 4q_3 = 2q_2$... (iii)
 $3(q_3 - 300) + 4q_3 = 2(360 - q_3)$
 $7q_3 - 900 = 720 - 2q_3 \Rightarrow 9q_3 = 1620$
 $\Rightarrow q_3 = \frac{1620}{9} = 180\mu C$
and $q_1 = -120\mu C$ and $q_2 = 180\mu C$

Sol 22: (A, D)
$$C_{eff} = \left(\frac{1}{C} + \frac{1}{2C}\right)^{-1} \frac{2C}{3}$$
 so charge $= \frac{2CE}{3}$
Final $C_{eff} = 2C \Rightarrow$ charge $= 2CE$
 $2CE - 2CE / 3 = 4CE / 3$



From charge conservation $Q_{C_1} = Q_{C_2}$

$$(5 - V) \times C_{1} = (v + 10) \times C_{2} \quad ; \quad 5 - V = (V + 10)2$$

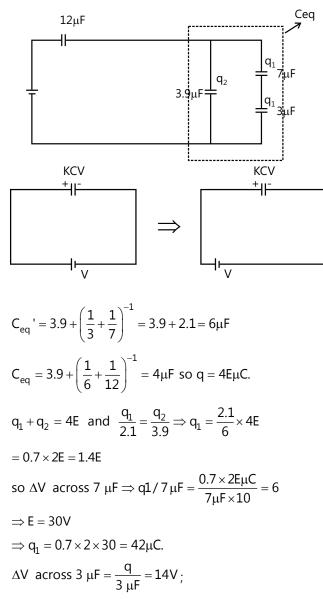
-15 = 3V \Rightarrow V = -5V
$$E_{C_{1}} = \frac{1}{2} \times 1 \times (10)^{2} = 50 \mu J ; \quad E_{C_{2}} = \frac{1}{2} \times 2 \times (5)^{2} = 25 \mu J$$

 $\Rightarrow 2E_{C_{1}} = E_{C_{1}}$

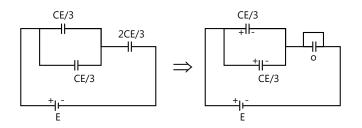
Sol 24: (A, B) We have $E = \frac{\sigma}{2\epsilon_0}$ (by one plate)

So force
$$= \frac{\sigma}{2\epsilon_0}$$
. $Q = \frac{Q^2}{2A\epsilon_0}$
 $Q = CV \Longrightarrow F = \frac{C^2 V^2}{2A\epsilon_0} \times \frac{d}{d} = \frac{CV^2}{2d}$

Sol 25: (B, C, D)



$$\Delta V$$
 across 12 $\mu F = 4 \times \frac{30}{12} = 10V$



Sol 26: (A, B, D) Charge = KCV – CV=(K-1)CV Energy absorbed = (K-1)CV² Energy = $\frac{1}{2} \times K \times C \times V^2 = \frac{(K-1)}{2}.CV^2$ Now $\frac{1}{2} \times K \times C \times V^2 + \text{work} = \frac{1}{2} \times C \times V^2 = (K-1)CV^2$ $\Rightarrow \text{Work} = \frac{1}{2}(K-1)CV^2$

Sol 27: (B, C)
$$V_{same} = E_{same}^{d}$$
, so E=same

Sol 28: (A, C, D)
$$C = \frac{A\epsilon_0}{d}$$
 and $Q = CV = \frac{A\epsilon_0 V}{d}$

Now
$$V_{net} = \frac{Q}{C} = \frac{CV}{KC} = \frac{V}{K} = E \times d \implies E = V / Kd$$

And energy initial + work done=energy final

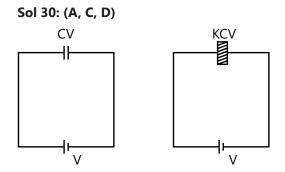
$$\frac{Q^{2}}{2C} + \text{work done} = \frac{Q^{2}}{2KC}$$

$$Work = \frac{Q^{2}}{2C} \left[\frac{1}{K} - 1 \right] = -\frac{CV^{2}}{2} \left[1 - \frac{1}{K} \right]$$

Putting the value of "C" from the first line, we get

$$W = \frac{\varepsilon_0 A V^2}{2d} \left(1 - \frac{1}{K} \right)$$

Sol 29: (C, D) $C_{eq} = \left(\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_2$



Q=C'V=KCV

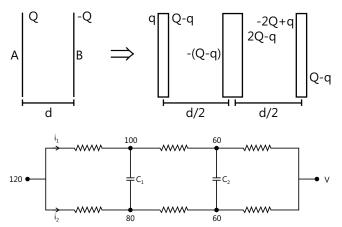
$$E_{\text{initial}} = \frac{1}{2}CV^2 \quad E_{\text{final}} = \frac{1}{2} \times K \times CV^2 = K \times E_{\text{initial}}$$

As $V = E \times d$ so $E = \text{same}$

As $v = E \times d$, so E = same

$$\mathsf{F} = \frac{\mathsf{Q}^2}{2\mathsf{A}\varepsilon_0} = \mathsf{K}^2 \frac{\mathsf{C}^2 \mathsf{V}^2}{2\mathsf{A}\mathsf{V}_0}$$

Sol 31: (A, B, C, D)



Now the charge on outer surfaces should be same $q = Q - q \implies q = Q / 2$

So (A) = -2Q + Q / 2 = -3Q / 2

Charge on A=Q/2 and charge on B = 3Q/2

So as $E \varpropto Q$ and $V \varpropto E \Rightarrow V \varpropto Q$ and hence C is correct.

Sol 32: (A, B, C, D) (A) at t=0 consider it as wire.

(B)
$$\frac{10}{R_{eq}} = i = \frac{10}{1 + \left(\frac{1}{2} + \frac{1}{2}\right)^{-1}} = \frac{10}{2} = 5A$$

(C) From kirchoff's law

$$i_1R_1 = i_2R_2 \Longrightarrow \frac{i_1}{i_2} = \frac{R_2}{R_1} = \text{constant}$$

$$\Delta V = iR = 5A \times 1\Omega = 5V.$$

So $Q = CV = 1\mu F \times 5 = 5\mu F$

Sol 33: (B, D)

$$i = \frac{120}{R_{eq}} = \frac{120}{\left(\frac{1}{2} + \frac{1}{2}\right)^{-1}} = 40A$$

Now this I will be divided equally, so $i_1 = 20A, i_2 = 20A$ Now $(\Delta V_2) = 0$

 $Q_{C_1}=20\!\times\!2\mu C=40\mu C$

Assertion Reasoning Type

Sol 34: (D) Statement-I is false electrostatic force remains the same.

Sol 35: (C) Statement-II is false.

Sol 36: (D) $Q = (\epsilon - iR)C \Longrightarrow i = (\epsilon - Q / C).1/R$

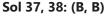
Work done by battery $= \varepsilon Q = \varepsilon (\varepsilon - iR)$

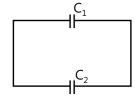
And energy in capacitor $= \frac{Q^2}{2C} = \frac{(\epsilon - iR)^2 C}{2}$

$$=\frac{(\varepsilon-iR)^2C}{2}+iR.(\varepsilon-iR).C$$

 \Rightarrow Statement-I is false.

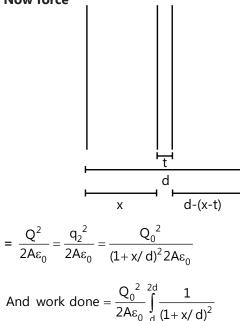
Comprehension Type





$$C_{2} = \frac{C_{1} \cdot d}{x} \quad \frac{q_{1}}{C_{1}} = \frac{q_{2}}{C_{2}} \implies \frac{Q_{0} - q_{2}}{q_{2}} = \frac{x}{d}$$
$$\implies \frac{Q_{0}}{q_{2}} = 1 + \frac{x}{d} \implies q_{2} = \left(\frac{Q_{0}}{1 + \frac{x}{d}}\right)$$





$$=\frac{Q_0^2}{2A\varepsilon_0}\times\frac{d}{6}=\frac{Q_0^2d}{12A\varepsilon_0}$$

And potential difference = q_1/C

$$q_1 = Q_0 - \frac{Q_0}{1 + x / d} = \frac{Q_0(x / d)}{1 + x / d} = \frac{Q_0 x}{x + d}$$

potential $q_1 / C_1 = \frac{Q_0 xd}{(x+d)A\epsilon_0}$

Sol 39: (A, C) i=E/R₁

Sol 40: (A, B, C) Current =
$$\frac{E}{R_1 + R_2}$$

Voltage = $\frac{E \times R_2}{(R_1 + R_2)}$;
 $\frac{1}{2} \times CV^2 = \frac{1}{2} \times C \times \left(\frac{ER_2}{(R_1 + R_2)}\right)^2$

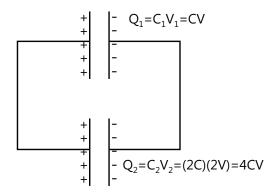
Sol 41: (A, C) (A) q_{max} = same.

(B) is wrong option as q = CV Now, C can be different

(D) Not necessarily, depends on R_1 and R_2 also.

Previous Years' Questions

Sol 1: The diagrammatic representation of given problem is shown in figure.



The net charge shared between the two capacitors is

 $Q' = Q_2 - Q_1 = 4CV - CV = 3CV$

The two capacitors will have the same potential, say V'

The net capacitance of the parallel combination of the two capacitors will be

$$C' = C_1 + C_2 = C + 2C = 3C$$

The potential difference across the capacitors will be

$$V' = \frac{Q'}{C'} = \frac{3CV}{3C} = V$$

The electrostatic energy of the capacitors will be

$$U' = \frac{1}{2}C'V'^2 = \frac{1}{2}(3C)V^2 = \frac{3}{2}CV^2$$

Sol 2: Electric field within the plates $\vec{E} = \vec{E}_{Q_1} + \vec{E}_{Q_2}$

$$+Q_{1} | \xrightarrow{\overrightarrow{E}} | +Q_{2} | \xrightarrow{\overrightarrow{E}} | +Q_{2} \Rightarrow | \xrightarrow{\overrightarrow{E}_{2}} | \xrightarrow{\overrightarrow{E}_{1}} | \xrightarrow{\overrightarrow{E}_{2}} | \xrightarrow{\overrightarrow{E}_{1}} |$$

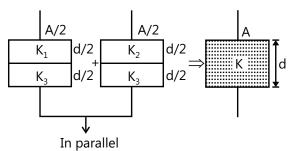
$$\mathsf{E} = \mathsf{E}_1 - \mathsf{E}_2 = \frac{\mathsf{Q}_1}{2\mathsf{A}\varepsilon_0} - \frac{\mathsf{Q}_2}{2\mathsf{A}\varepsilon_0}, \ \mathsf{E} = \frac{\mathsf{Q}_1 - \mathsf{Q}_2}{2\mathsf{A}\varepsilon_0}$$

.:. Potential difference between the plates

$$V_{A} - V_{B} = Ed = \left(\frac{Q_{1} - Q_{2}}{2A\varepsilon_{0}}\right)d = \frac{Q_{1} - Q_{2}}{2\left(\frac{A\varepsilon_{0}}{d}\right)} = \frac{Q_{1} - Q_{2}}{2C}$$

Sol 3: (D) Applying C =
$$\frac{\epsilon_0 A}{d - t_1 - t_2 + \frac{t_1}{K_1} + \frac{t_2}{K_2}}$$

we have



$$\frac{\varepsilon_0 (A/2)}{d-d/2-d/2+\frac{d/2}{K_1}+\frac{d/2}{K_3}}$$

$$+\frac{\epsilon_{0}(A/2)}{d-d/2-d/2+\frac{d/2}{K_{2}}+\frac{d/2}{K_{3}}}=\frac{K\epsilon_{0}A}{d}$$

Solving this equation, we get K = $\frac{K_1K_3}{K_1 + K_3} + \frac{K_2K_3}{K_2 + K_3}$

Sol 4: (C) ΔU = decrease in potential energy = U_i – U_f

$$= \frac{1}{2}C(V_1^2 + V_2^2) - \frac{1}{2}(2C)\left(\frac{V_1 + V_2}{2}\right)$$
$$= \frac{1}{4}C(V_1 - V_2)^2$$

Sol 5: (D) $q_1 = C_1 V = 2V = q$

This charge will remain constant after switch is shifted from position 1 to position 2.

$$U_{i} = \frac{1}{2} \frac{q^{2}}{C_{i}} = \frac{q^{2}}{2 \times 2} = \frac{q^{2}}{4}$$

$$U_{f} = \frac{1}{2} \frac{q^{2}}{C_{f}} = \frac{q^{2}}{2 \times 10} = \frac{q^{2}}{20}$$

$$\therefore \text{ Energy dissipated} = U_{i} - U_{f} = \frac{q^{2}}{5}$$
This energy dissipated $\left(=\frac{q^{2}}{5}\right)$ is 80% of the initial stored energy $\left(=\frac{q^{2}}{4}\right)$

Sol 6: (A, D) When dielectric slab is introduced capacity gets increased while potential difference remains unchanged.

$$\therefore V = V_{0'} C > C_{0}$$

$$Q = CV \therefore Q > Q_{0}$$

$$U = \frac{1}{2}CV^{2} \therefore U > U_{0}$$

$$E = \frac{V}{d} \text{ but } V \text{ and } d \text{ both are unchanged}$$
Therefore, E = E₀

Sol 7: (B, D) Charging battery is removed. Therefore, q = constant Distance between the plates is increased. Therefore, C decreases.

Now, V =
$$\frac{q}{C}$$
, q is constant and C is decreasing

Therefore, V should increase.

 $U = \frac{1}{2} \frac{q^2}{C}$ again q is constant and c is decreasing

Therefore U should increase.

Sol 8: (A, C, D) Battery is revoved. Therefore, charge stored in the plates will remain constant

$$Q = CV = \frac{\varepsilon_0 A}{d} V$$

Q = constant.

Now, dielectric slab is inserted. Therefore, C will increase. New capacity will be

$$C' = KC = \frac{\varepsilon_0 KA}{d}$$
$$V' = \frac{Q}{C'} = \frac{V}{K}$$

And new electric field $E = \frac{V'}{d} = \frac{V}{K.d}$

Potential energy stored in the capacitor,

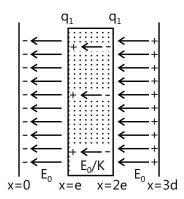
Initially,
$$U_i = \frac{1}{2}CV^2 = \frac{\varepsilon_0 AV^2}{2d}$$

Finally,
$$U_f = \frac{1}{2}C'V'^2 = \frac{1}{2}\left(\frac{K\epsilon_0 A}{d}\right)\left(\frac{V}{K}\right)^2 = \frac{\epsilon_0 A V^2}{2Kd}$$

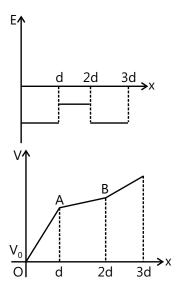
Work done on the system will be

$$|\Delta U| = \frac{\varepsilon_0 A V^2}{2d} \left(1 - \frac{1}{K} \right)$$

Sol 9: (B, C) The magnitude and direction of electric field at different points are shown in figure. The direction of the electric field remains the same. Hence, option (b) is correct. Similarly, electric lines always flow from higher to lower potential, therefore, electric potential increase continuously as we move from x = 0 to x = 3d.

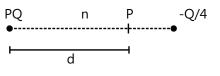


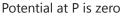
Therefore, option (c) is also correct. The variation of electric field (E) and potential (V) with x will be as follows



OA||BC and $(Slope)_{OA} > (Slope)_{AB}$ Because $E_{0-d} = E_{2d-3d}$ And $E_{0-d} > E_{d-2d}$

Sol 10: (A, B, C)





If (d > x)

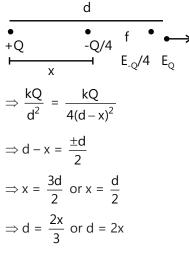
$$\Rightarrow \frac{kQ}{d} - \frac{kQ}{4(d-x)} = 0 \Rightarrow d = 4d - 4x$$

$$\Rightarrow x = \frac{3d}{4} = d = \frac{4x}{3}$$

if (d < n)

$$\Rightarrow \frac{kQ}{d} - \frac{kQ}{4(x-d)} = 0 \Rightarrow \frac{4x}{5} = d$$

Electric field at P is zero



(since d > x)

Sol 11: (A) $\vec{r} = (\hat{i} + 3\hat{j} + 2\hat{k}) - (4\hat{i} + 7\hat{j} + 2\hat{k})$ = $-3\hat{i} - 4\hat{j} + 0\hat{k}$ $|\vec{r}| = 5$ $V = \frac{k \times q}{r} = \frac{9 \times 10^9 \times 10^{-8}}{5} = 18 \text{ v}$

Field is parallel to $\,\vec{r}\,$ and thus has no 3-component

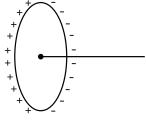
Sol 12: (A, C) It must have any K.E. at B to reach A

Since

$$U_{A} - U_{B} = -e (V_{A} - V_{B}) = +4eV$$

(K.E.)_f - (k.E.)_i = $U_{B} - U_{A} = -4eV$





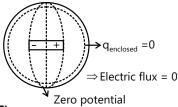
By symmetry potential due to negative part =(potential due to particle part). (Also every small charge is equidistant from axis)

.: Potential at all potential axis is zero

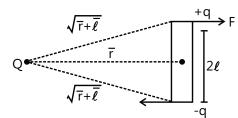
Direction of field is perpendicular to axis and towards negative side

There will be a torque when placed in uniform field

Sol 14: (A, D) Electric field due to dipole exists inside sphere only a circle on the sphere has zero potential which is equidistant from poles of dipole



Sol 15: (B, C)



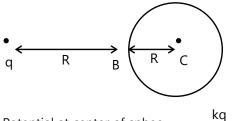
$$F_{R} = \frac{2F.\ell}{\sqrt{a^{2} + \ell^{2}}} (= 2F \sin \theta) = \frac{2\ell}{\sqrt{r^{2} + \ell^{2}}}$$
$$\left(\frac{kQ}{r^{2} + \ell^{2}}.q\right) = \frac{kQ(P)}{(r^{2} + \ell^{2})^{3/2}}$$
$$\Rightarrow F_{R} = \frac{1}{\sqrt{r^{2} + \ell^{2}}} \cdot \frac{pQ}{r^{2}} (r \ge \ell)$$

Torque on dipole =
$$\frac{F.r}{(r^2 + \ell^2)^{1/2}} (2 \ell)$$
$$= (=2 F \cos \theta \ell)$$

$$\Rightarrow \mathsf{T} = \frac{\mathsf{r}.(2\ell)}{(\mathsf{r}^2 + \ell^2)^{1/2}} \left(\frac{\mathsf{I}}{4\pi\varepsilon_0} \cdot \frac{\mathsf{Q}}{\mathsf{r}^2 + \ell^2} \cdot \mathsf{Q} \right)$$

$$\Rightarrow T = \frac{1}{4\pi\varepsilon_0} \frac{pQ}{r^2} (r >> \ell)$$

Sol 16: (A, D)



Potential at center of sphee = $\frac{kq}{4\pi \epsilon_0 (d+R)}$

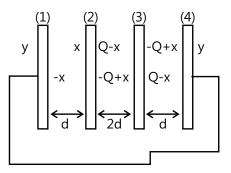
(It is independent of presence of conductor because induced charges provides zero potential at center)

Potential B = Potential at C

(Since electric field inside conduction is zero)

- \Rightarrow V = constant
- ... Potential at B due induced charges
- = Potential at B potential at B due to q

$$= \frac{kq}{4\pi \in_0 (d+R)} - \frac{kq}{4\pi \in_0 d} = \frac{-kqR}{4\pi \in_0 (R+d)d}$$



Since the potential difference between plates (1) and (4) is zero.

$$\Rightarrow \frac{-x.d}{A \in_0} + \frac{Q - x(2d)}{A \in_0} + \frac{(Q - x)d}{A \in_0} = 0$$
$$\Rightarrow x = \frac{3Q}{4} \therefore \text{ Option B}$$

 \Rightarrow Charge on right side of plate 3 = Q - x = Q/4

Sol 18: (B) Also Charge is conserved on plate 1 and 4 $\Rightarrow y + (-x) + Q - x + y = 0 + 0$ $\Rightarrow y = \frac{Q}{4} \therefore \text{ Option B}$

:. Charge on right side of plate 4 = $\frac{Q}{2}$

Sol 19: (C) Potential difference between (i) and (ii)

$$= \frac{x(d)}{A \in_0} = \frac{3Qd}{4A \in_0}$$

/ \

Sol 20: (B) Obviously, both statements are correct. But, Statement-II is not a correct explanation of statement-I.

Sol 21: Refer theory on Superposition of electric field & Ampere's Loop Law.

Sol 22: (A, D) $Q = KQ_0 \quad V \rightarrow Constant$

$$U = \frac{1}{2} (KC) V^{2} = \left(\frac{1}{2} CV^{2}\right) k = K U_{0}$$
$$E = E_{0} / k$$

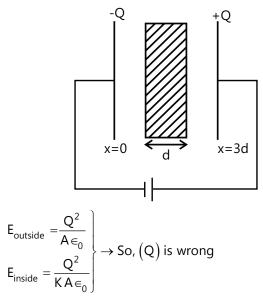
Sol 23: (B, D) $C \propto \frac{1}{d}$

Sol 24: (A, C, D) Q - remains constant.

C changes from $\frac{\epsilon_0 A}{d}$ to $\frac{k \epsilon_0 A}{d}$

Hence, other variable also change.

Sol 25: (B, C)



(B) is correct as the direction of field remain the same.

(C) As we are going in the opposite direction of electric field, potential would rise.

Sol 26: (C, D) Using Gauss's Law

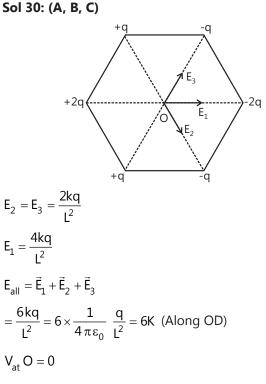
Net Flux = $\int \vec{E} \cdot \vec{ds} = \frac{q_{in}}{\epsilon_0}$

It electric field is same at all the points of a surface, it is knows as equipotential surface.

Sol 27: (A, B, C, D) Refer Theory.

Sol 28: (C, D) Refer Theory.

Sol 29: (C) $2\mu F \& 3\mu F$ are in parallel combination.



 $\rm V_{at}$ line PR is zero because this line is equatorial axis for three dipole.

Sol 31: (B, D) After switch S_1 is closed, C_1 is charged by $2CV_0$ when switch S_2 is closed, C_1 and C_2 both have upper plate charge CV_0 .

When $\rm S_3$ is closed, the upper plate of $\rm C_2$ becomes charged by $-\rm CV_0$ and lower plate by $+\rm CV_0$.

Sol 32: (A, D) As $E = V/d E_1/E_2 = 1$ (both parts have common potential difference)

Assume C_0 be the capacitance without dielectric for whole capacitor.

$$k \frac{C_0}{3} + \frac{2C_0}{3} = C$$
$$\frac{C}{C_1} = \frac{2+k}{k}$$

 $\frac{Q_1}{Q_2} = \frac{k}{2}.$



