# **CURRENT ELECTRICITY**



#### **Electric Current**

- $\bullet \quad I = \frac{q}{t} = \frac{ne}{t}$
- In case of an electron revolving in a circle of radius r with speed v, period of revolution is  $T = \frac{2\pi r}{r}$
- Frequency of revolution  $v = \frac{v}{2\pi r}$
- Current at any point of the orbit is  $I = \frac{e}{T} = \frac{ev}{2\pi r}$

#### **Ohm's Law, Resistance and Resistivity**

- $\bullet$  V = IR
- Resistance of uniform conductor of length l and cross sectional area A,  $R = \frac{\rho l}{A}$
- Resistivity or specific resistance,  $\rho = \frac{RA}{l}$
- Effective specific resistance in series combination is

$$\frac{\rho_1 l_1 + \rho_2 l_2}{l_1 + l_2}$$
 (A is same).

• Effective specific resistance in parallel combination is

$$\frac{\left(A_1 + A_2\right)\rho_1\rho_2}{A_1\rho_2 + A_2\rho_1}$$
 (lis same).

## Current Density, Conductance and Conductivity

- Conductance,  $G = \frac{1}{R}$
- Conductivity,  $\sigma = \frac{1}{\rho} = \frac{l}{RA}$
- Current density,  $J = \frac{I}{A} = \sigma E = nev_d$

#### **Electric Power**

 $P = VI = I^2 R = \frac{V^2}{R}$ 

### **Current Electricity**

#### Kirchhoff's Laws

- Law of conservation of charge applied at a junction, *i.e.*,  $\Sigma I = 0$
- Law of conservation of energy applied in closed loop,

$$i.e., \Sigma \varepsilon = \Sigma IR$$

#### **Drift Velocity and Mobility of Charge**

- Drift speed,  $v_d = \frac{eE}{m}\tau$
- Mobility,  $\mu_e = \frac{v_d}{E}$
- Current in terms of drift velocity,

$$I = neAv_d = \frac{ne^2 A \tau E}{m} = neA\mu_e E = neA\mu_e \frac{V}{l}$$

• In terms of relaxation time τ,

$$R = \frac{ml}{ne^2 \tau A}$$
 and  $\rho = \frac{m}{ne^2 \tau}$ 

#### Variation of Resistance with Temperature

- Temperature coefficient of resistance,  $\alpha = \frac{R_2 R_1}{R_1(T_2 T_1)}$
- If  $T_1 = 0$ °C and  $T_2 = T$ °C then  $\alpha = \frac{R_T R_0}{R_0 \times T}$  or  $R_T = R_0 (1 + \alpha T)$

#### **Combination of Resistances**

- In series, equivalent resistance,  $R_s = R_1 + R_2 + R_3 + \dots$
- In parallel, equivalent resistance,  $\frac{1}{R_P} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$
- For two resistances in parallel current through the two resistances will be,  $I_1 = \frac{R_2 I}{R_1 + R_2}$ ,  $I_2 = \frac{R_1 I}{R_1 + R_2}$
- When resistances are connected in series, the current through each resistance is same. In parallel combination voltage is same.

### Emf, Internal Resistance, Current in case of Grouping of Cells

- Emf of a cell,  $\varepsilon = \frac{W}{q}$
- Terminal potential difference where current is being drawn from the cell,  $V = \varepsilon Ir$
- Terminal potential difference when the cell is being charged  $V = \varepsilon + Ir$
- Internal resistance of a cell,  $r = R \left[ \frac{\varepsilon V}{V} \right]$
- Grouping of identical cells:
  - O Cells in series,  $I = \frac{n\varepsilon}{R + nr}$  (*n* cells)
  - O Cells in parallel,  $I = \frac{m\varepsilon}{mR + r}$  (*m* cells)
  - O Cells in mixed grouping,  $I = \frac{mn\epsilon}{mR + nr}$

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