Kepler's Laws of

Planetary Motion

BRAIN MAP **CLASS XI**

GRAVITATION

Newton's Law of Gravitation

Gravitational force (F) between two bodies is directly proportional to product of masses and inversely proportional to square of the distance between them.

$$\vec{F} = -\frac{Gm_1m_2}{r^2} \cdot \hat{r}$$

Law of orbits: Every planet revolves around the sun in an elliptical orbit and the sun is situated at one of its

> Law of areas: The areal velocity of the planet around the sun is constant

i.e.,
$$\frac{dA}{dt}$$
 = a constant

Acceleration due to gravity

- For a body falling freely under gravity, the acceleration in the body is called acceleration due to gravity.
- Relationship between g and G $g = \frac{GM_e}{R_e^2} = \frac{4}{3}\pi GR_e \rho$

where G = gravitational constant ρ = density of earth

 M_{ρ} and R_{ρ} be the mass and radius of earth

Characteristics of gravitational force

- It is always attractive.
- It is independent of the medium.
- It is a conservative and central force.
- It holds good over a wide range of distance.

Gravitational potential

Work done in bringing a unit mass from infinity to a point in the gravitational

$$V = \frac{-GM}{r}$$

Law of periods: The square of the time period of revolution of a planet is directly proportional to the cube of semi major axis of the elliptical orbit. $T^2 \propto a^3$

Gravitational Potential Energy

Work done in bringing the given body from infinity to a point in the gravitational field.

$$U = -GMm/r$$

Escape speed

The minimum speed of projection of a body from surface of earth so that it just crosses the gravitational field of earth.

$$v_e = \sqrt{\frac{2GM}{R}}$$

Variation of acceleration due to gravity (g)

Due to altitude (h)

$$g_h = g \left(1 - \frac{2h}{R_e} \right)$$

The value of g goes on decreasing with height.

Due to depth (d)

$$g_d = g \left(1 - \frac{d}{R_e} \right)$$

The value of g decreases with depth.

Due to rotation of earth

$$g_{\lambda} = g - R_e \omega^2 \cos^2 \lambda$$

At equator, $\lambda = 0^\circ$

$$g_{\lambda_{\min}} = g - R_e \omega^2$$

At poles, $\lambda = 90^\circ$

 $g_{\lambda_{\text{max}}} = g_p = g$

Types of Satellite

Polar satellilte

- Time period: 100 min
- Revolves in polar orbit around the earth.
- Height: 500-800 km.
- Uses: Weather forecasting, military spying

Geostationary satellite

- Time period: 24 hours
- Same angular speed in same direction with earth.
- Height: 36000 km.
- Uses: GPS, satellite communication (TV)

Earth's

Satellite

Orbital speed of satellite

The minimum speed required to put the satellite into a given orbit.

$$v_0 = R_c \sqrt{\frac{g}{R_c + h}}$$

For satellite orbiting close to the earth's surface

$$v_0 = \sqrt{gR_c}$$

Time period of satellite

$$T = \frac{2\pi}{R_e} \sqrt{\frac{(R_e + h)^3}{g}}$$

For satellite orbiting close to the earth's surface

$$T = 2\pi \sqrt{\frac{R_e}{g}} = 84.6 \text{ min}$$

Energy of satellite

- Kinetic energy $K = \frac{GM_e m}{2(R_e + h)}$
- Potential energy $U = \frac{-GM_e m}{R_e + h}$
- Total energy $E = K + U = -\frac{GM_c}{2(R_c + h)}$

